

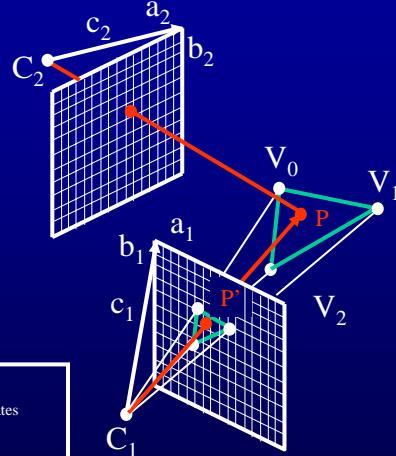
Projective texture mapping. Shadow maps

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Mapping from desired to reference image

$$\begin{aligned}
 C_1 + (\bar{c}_1 + u_1 \bar{a}_1 + v_1 \bar{b}_1) w_1 &= C_2 + (\bar{c}_2 + u_2 \bar{a}_2 + v_2 \bar{b}_2) w_2 \\
 \begin{bmatrix} \bar{a}_2 & \bar{b}_2 & \bar{c}_2 \\ w_2 u_2 \\ w_2 v_2 \\ w_2 \end{bmatrix} &= C_1 - C_2 + \begin{bmatrix} \bar{a}_1 & \bar{b}_1 & \bar{c}_1 \\ w_1 u_1 \\ w_1 v_1 \\ w_1 \end{bmatrix} \\
 \begin{bmatrix} w_2 u_2 \\ w_2 v_2 \\ w_2 \end{bmatrix} &= \begin{bmatrix} \bar{a}_2 & \bar{b}_2 & \bar{c}_2 \\ w_2 \end{bmatrix}^{-1} (C_1 - C_2) + \begin{bmatrix} \bar{a}_2 & \bar{b}_2 & \bar{c}_2 \\ w_2 \end{bmatrix}^{-1} \begin{bmatrix} \bar{a}_1 & \bar{b}_1 & \bar{c}_1 \\ w_1 v_1 \\ w_1 \end{bmatrix} \\
 \begin{bmatrix} w_2 u_2 \\ w_2 v_2 \\ w_2 \end{bmatrix} &= \begin{bmatrix} q_{00} \\ q_{10} \\ q_{20} \end{bmatrix} + \begin{bmatrix} q_{01} & q_{02} & q_{03} \\ q_{11} & q_{12} & q_{13} \\ q_{21} & q_{22} & q_{23} \end{bmatrix} \begin{bmatrix} w_1 u_1 \\ w_1 v_1 \\ w_1 \end{bmatrix} \\
 u_2 &= \frac{\frac{q_{00}}{w_1} + q_{01} u_1 + q_{02} v_1 + q_{03}}{\frac{q_{20}}{w_1} + q_{21} u_1 + q_{22} v_1 + q_{23}} \\
 \frac{1}{w_1} &= Au_1 + Bu_1 + C \\
 u_2 &= \frac{Du_1 + Ev_1 + F}{Ju_1 + Kv_1 + L} \\
 v_2 &= \frac{Gu_1 + Hv_1 + I}{Ju_1 + Kv_1 + L}
 \end{aligned}$$

(C_2, a_2, b_2, c_2) – reference view
 (u_2, v_2) – reference pixel coordinates
 (C_1, a_1, b_1, c_1) – desired view
 (u_1, v_1) – desired view pixel coordinates
 (u_2, v_2, w_2) – unknowns
 w_1 – computed using triangle $V_0V_1V_2$



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Shadow Maps

- Efficient implementation of shadows
- Essentially a zbuffer rendered from the light
 - if a point is behind the map as seen from the light, it is in shadow
 - the z-values model the first-surfaces seen from the light

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Shadow Map Implementation

- Step 1: construction
 - one per light
 - updated when light or objects move
 - does not need to be updated when only the camera moves
 - resolution according to
 - scene geometry
 - desired image resolution
 - desired shadow quality
 - budget
 - view should
 - cover all light rays
 - cover all scene (cube maps if needed)
 - near / far plane according to scene bounding box

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Shadow Map Implementation

- Step 2: shadow computation
 - project scene point visible at current pixel onto shadow map(s)
 - if hidden, pixel is in shadow
 - else light contributes to pixel color
 - soft shadows
 - pixels close to the shadow border are partially in shadow (penumbra)
 - many methods, see literature