

CS535

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• Calculating the overall light propagation within a scene is a very difficult problem.

• With a standard ray tracing algorithm, this is a very time consuming task, since a huge number of rays have to be shot.



- For this reason, the radiosity method was invented.
- The main idea of the method is

**to store illumination values on the surfaces of the objects, as the light is propagated starting at the light sources.**



• Radiosity is inspired by ideas from heat transfer and is an application of a finite element method to solving the rendering equation for scenes with purely diffuse surfaces

$$
L_o(\mathbf{x}, \omega, \lambda, t) = L_e(\mathbf{x}, \omega, \lambda, t) + \int_{\Omega} f_r(\mathbf{x}, \omega', \omega, \lambda, t) L_i(\mathbf{x}, \omega', \lambda, t) (-\omega' \cdot \mathbf{n}) d\omega'
$$
  
no equation)

(rendering equation)



[Radiosity slides heavily based on Dr. Mario Costa Sousa, Dept. of of CS, U. Of Calgary]



• Equation:  $B_i dA_i = E_i dA_i + R_i \int_i B_j F_{ji} dA_j$ 













#### Diffuse Interreflection

### Radiosity Assumptions



- #1: surfaces are diffuse emitters and reflectors of energy, emitting and reflecting energy uniformly over their entire area.
- $\frac{\#2:}{\#2:}$  an equilibrium solution can be reached; that all of the energy in an environment is accounted for, through absorption and reflection.
- #3: solution can-be/will-be viewpoint independent; i.e., the solution will be the same regardless of the viewpoint of the image.



- The "radiosity equation" describes the **amount of energy** which can be emitted from a surface
	- Is a sum of the energy inherent in the surface (e.g., a light source) plus energy which strikes the surface (e.g., from another surface)
- The energy which leaves a surface (surface "j") and strikes another surface (surface "i") is attenuated by two factors:
	- the **"form factor"** between surfaces "i" and "j" (physical relationship)
	- the **reflectivity of surface "i"** (material property)

















**Classic Radiosity Algorithm**



![](_page_14_Figure_2.jpeg)

![](_page_14_Figure_3.jpeg)

![](_page_14_Figure_4.jpeg)

![](_page_14_Picture_5.jpeg)

![](_page_14_Picture_6.jpeg)

![](_page_14_Figure_7.jpeg)

![](_page_14_Picture_33.jpeg)

![](_page_14_Picture_9.jpeg)

**Classic Radiosity Algorithm**

![](_page_15_Picture_1.jpeg)

**Mesh Surfaces into Elements**

![](_page_15_Figure_3.jpeg)

![](_page_15_Figure_4.jpeg)

![](_page_15_Picture_5.jpeg)

![](_page_15_Picture_6.jpeg)

![](_page_15_Picture_7.jpeg)

![](_page_15_Picture_33.jpeg)

![](_page_15_Picture_9.jpeg)

![](_page_16_Picture_0.jpeg)

Between differential areas, the form factor equals:

![](_page_17_Figure_1.jpeg)

Between differential areas, the form factor equals:

![](_page_18_Picture_1.jpeg)

=

The overall form factor between i and j is found by integrating

![](_page_18_Figure_3.jpeg)

### Form Factors in (More) Detail

![](_page_19_Picture_1.jpeg)

![](_page_19_Figure_2.jpeg)

# Form Factors in (More) Detail

![](_page_20_Picture_1.jpeg)

- Several ways to find form factors
- Hemicube was original method + Hardware acceleration + Gives  $F_{dA/A}$  for all *j* in one pass
	- Aliasing
- Area sampling methods now preferred  $\rightarrow$  Slower than hemicube but GPU-able  $\rightarrow$  As accurate as desired since adaptive

![](_page_21_Picture_0.jpeg)

### Area Sampling

![](_page_21_Figure_2.jpeg)

We have now  $F_{dA/A}$ 

**Classic Radiosity Algorithm**

![](_page_22_Picture_1.jpeg)

![](_page_22_Figure_2.jpeg)

![](_page_22_Figure_3.jpeg)

![](_page_22_Figure_4.jpeg)

![](_page_22_Picture_5.jpeg)

![](_page_22_Picture_6.jpeg)

![](_page_22_Figure_7.jpeg)

![](_page_22_Picture_33.jpeg)

![](_page_22_Picture_9.jpeg)

![](_page_23_Picture_0.jpeg)

# Solving for radiosity solution

- The "Full Matrix" Radiosity Algorithm
- Gathering & Shooting
- Progressive Radiosity

![](_page_24_Figure_0.jpeg)

$$
\begin{bmatrix}\n1 - \rho_1 F_{11} & -\rho_1 F_{12} & \cdots & -\rho_1 F_{1n} \\
-\rho_2 F_{21} & 1 - \rho_2 F_{22} & \cdots & -\rho_2 F_{2n} \\
\vdots & \vdots & \ddots & \vdots \\
-\rho_n F_{n1} & -\rho_n F_{n2} & \cdots & 1 - \rho_n F_{nn}\n\end{bmatrix}\n\begin{bmatrix}\nB_1 \\
B_2 \\
\vdots \\
B_n\n\end{bmatrix} =\n\begin{bmatrix}\nE_1 \\
E_2 \\
\vdots \\
E_n\n\end{bmatrix}
$$

### Radiosity Matrix

![](_page_25_Picture_1.jpeg)

• The "full matrix" radiosity solution calculates the form factors between each pair of surfaces in the environment, then forms a series of simultaneous linear equations.

$$
\begin{bmatrix}\n1 - \rho_1 F_{11} & -\rho_1 F_{12} & \cdots & -\rho_1 F_{1n} \\
-\rho_2 F_{21} & 1 - \rho_2 F_{22} & \cdots & -\rho_2 F_{2n} \\
\vdots & \vdots & \ddots & \vdots \\
-\rho_n F_{n1} & -\rho_n F_{n2} & \cdots & 1 - \rho_n F_{nn}\n\end{bmatrix}\n\begin{bmatrix}\nB_1 \\
B_2 \\
\vdots \\
B_n\n\end{bmatrix} =\n\begin{bmatrix}\nE_1 \\
E_2 \\
\vdots \\
E_n\n\end{bmatrix}
$$

• This matrix equation is solved for the "B" values, which can be used as the final intensity (or color) value of each surface.

![](_page_26_Picture_0.jpeg)

### Radiosity Matrix

- This method produces a complete solution, at the substantial cost of
	- first calculating form factors between each pair of surfaces
	- and then the solution of the matrix equation.
- This leads to substantial costs not only in computation time but in storage.

![](_page_27_Picture_0.jpeg)

# Solving for radiosity solution

- The "Full Matrix" Radiosity Algorithm
- Gathering & Shooting
- Progressive Radiosity

### Gathering

• In a sense, the light leaving patch i is determined by *gathering* in the light from the rest of the environment

$$
B_i = E_i + \rho_i \sum_{j=1}^n B_j F_{ij}
$$

 $B_i$  *due* to  $B_j = \rho_i B_j F_{ij}$ 

![](_page_28_Picture_4.jpeg)

### Gathering

**Gathering light through a** hemi-cube allows one patch radiosity to be updated.

![](_page_29_Picture_2.jpeg)

#### **GATHERING**

![](_page_29_Figure_4.jpeg)

### **Gathering**

![](_page_30_Picture_1.jpeg)

![](_page_30_Figure_2.jpeg)

Row of  $F$  times  $B$ 

Calculate one row of  $F$  and discard

### **Successive Approximation**

![](_page_31_Picture_1.jpeg)

![](_page_31_Picture_2.jpeg)

 $L_e$ 

![](_page_31_Picture_4.jpeg)

 $\overline{K \circ L_{\rho}}$ 

![](_page_31_Picture_6.jpeg)

 $K \circ K \circ L_{\rho}$ 

![](_page_31_Picture_8.jpeg)

 $\overline{K\circ K\circ K\circ L_{\rho}}$ 

![](_page_31_Picture_10.jpeg)

 $L_e$ 

![](_page_31_Picture_12.jpeg)

![](_page_31_Picture_14.jpeg)

![](_page_31_Picture_16.jpeg)

 $L_e + K \circ L_e$   $L_e + \cdots K^2 \circ L_e$   $L_e + \cdots K^3 \circ L_e$ 

# Shooting

**Shooting light through a** single hemi-cube allows the whole environment's radiosity values to be updated simultaneously.

![](_page_32_Figure_2.jpeg)

### **Shooting**

![](_page_33_Picture_1.jpeg)

![](_page_33_Figure_2.jpeg)

![](_page_33_Figure_3.jpeg)

**Brightness order** 

Column of  $F$  times  $B$ 

### **Progressive Radiosity**

![](_page_34_Picture_1.jpeg)

![](_page_34_Picture_2.jpeg)

 $(a)$ 

 $(b)$ 

(a) Traditional Gauss-Seidel iteration of 1, 2, 24 and 100. (b) Progressive Refinement (PR) iteration of 1, 2, 24 and 100.

From Cohen, Chen, Wallace, Greenberg 1988

**Classic Radiosity Algorithm**

![](_page_35_Picture_1.jpeg)

**Mesh Surfaces into Elements**

**Compute Form Factors**

**Between Elements**

![](_page_35_Figure_3.jpeg)

![](_page_35_Figure_4.jpeg)

![](_page_35_Figure_5.jpeg)

**Display Solution**

![](_page_35_Figure_7.jpeg)

![](_page_35_Picture_8.jpeg)

![](_page_36_Picture_0.jpeg)

![](_page_36_Picture_1.jpeg)

![](_page_36_Picture_2.jpeg)

**Reference Solution Uniform Mesh** 

Table in room sequence from Cohen and Wallace

![](_page_37_Picture_0.jpeg)

### **Artifacts – What can we do?**

![](_page_37_Picture_2.jpeg)

#### **Error Image**

- A. Blocky shadows
- **B. Missing features**
- C. Mach bands
- D. Inappropriate shading discontinuities
- **E. Unresolved discontinuities**

# **Option 1: Increasing Resolution4**

![](_page_38_Picture_1.jpeg)

![](_page_38_Picture_2.jpeg)

![](_page_38_Picture_3.jpeg)

![](_page_38_Picture_4.jpeg)

![](_page_38_Picture_5.jpeg)

### **Option 2: Adaptive Meshing**

![](_page_39_Picture_1.jpeg)

![](_page_39_Picture_2.jpeg)

![](_page_40_Picture_0.jpeg)

### Example Radiosity Results

![](_page_40_Picture_2.jpeg)

![](_page_40_Picture_3.jpeg)

### The Cornell Box

![](_page_41_Picture_1.jpeg)

- This is the original Cornell box, as simulated by Cindy M. Goral, Kenneth E. Torrance, and Donald P. Greenberg for the 1984 paper *Modeling the interaction of Light Between Diffuse Surfaces*, Computer Graphics (SIGGRAPH '84 Proceedings), Vol. 18, No. 3, July 1984, pp. 213-222.
- Because form factors were computed analytically, no occluding objects were included inside the box.

![](_page_41_Picture_4.jpeg)

![](_page_42_Picture_0.jpeg)

### The Cornell Box

- This simulation of the Cornell box was done by Michael F. Cohen and Donald P. Greenberg for the 1985 paper *The Hemi-Cube, A Radiosity Solution for Complex Environments*, Vol. 19, No. 3, July 1985, pp. 31-40.
- The hemi-cube allowed form factors to be calculated using scan conversion algorithms (which were available in hardware), and made it possible to calculate shadows from occluding objects.

![](_page_42_Picture_4.jpeg)

![](_page_43_Picture_0.jpeg)

![](_page_44_Picture_0.jpeg)

![](_page_45_Picture_0.jpeg)

![](_page_46_Picture_0.jpeg)

![](_page_47_Picture_0.jpeg)

### Discontinuity Meshing

![](_page_47_Picture_2.jpeg)

![](_page_48_Picture_0.jpeg)

# Opera Lighting

- This scene from *La Boheme* demonstrates the use of focused lighting and angular projection of predistorted images for the background.
- It was rendered by Julie O'B. Dorsey, Francois X. Sillion, and Donald P. Greenberg for the 1991 paper *Design and Simulation of Opera Lighting and Projection Effects*.

![](_page_49_Picture_4.jpeg)

![](_page_50_Picture_0.jpeg)

![](_page_51_Picture_0.jpeg)

### Radiosity Factory

- These two images were rendered by Michael F. Cohen, Shenchang Eric Chen, John R. Wallace and Donald P. Greenberg for the 1988 paper *A Progressive Refinement Approach to Fast Radiosity Image Generation*.
- The factory model contains 30,000 patches, and was the most complex radiosity solution computed at that time.
- The radiosity solution took approximately 5 hours for 2,000 shots, and the image generation required 190 hours; each on a VAX8700.

![](_page_51_Picture_5.jpeg)

![](_page_52_Picture_0.jpeg)

### Museum

![](_page_53_Picture_1.jpeg)

- Most of the illumination that comes into this simulated museum arrives via the baffles on the ceiling.
- As the progressive radiosity solution executed, users could witness each of the baffles being illuminated from above, and then reflecting some of this light to the bottom of an adjacent baffle.
- A portion of this reflected light was eventually bounced down into the room.
- The image appeared on the proceedings cover of SIGGRAPH 1988.

![](_page_53_Picture_6.jpeg)

![](_page_54_Picture_0.jpeg)

![](_page_55_Picture_0.jpeg)

![](_page_56_Picture_0.jpeg)

![](_page_57_Picture_0.jpeg)

![](_page_57_Picture_1.jpeg)

![](_page_57_Picture_2.jpeg)

![](_page_58_Picture_0.jpeg)

![](_page_58_Picture_1.jpeg)

![](_page_58_Picture_2.jpeg)

![](_page_59_Picture_0.jpeg)

![](_page_60_Picture_0.jpeg)