



# Plenoptic Modeling and Lightfields

Daniel G. Aliaga

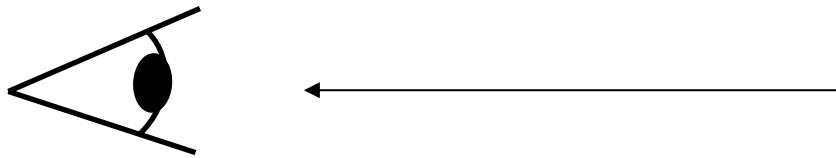
CS635

(slides based on Richard Szeliski, Michael Cohen, Marc Levoy, Leonard McMillan, Jian Huang, Jin-Xiang Chai, and Heung-Yeung Shum)

# Recall: Light is...



- Electromagnetic radiation (EMR) moving along rays in space
  - $R(\lambda)$  is EMR, measured in units of power (watts)
    - $\lambda$  is wavelength

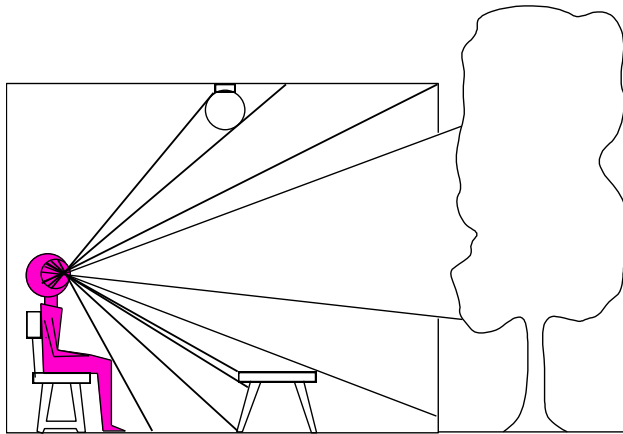


- Useful things:
- Light travels in straight lines
- In vacuum, radiance emitted = radiance arriving
  - i.e. there is no transmission loss

# What do we see?

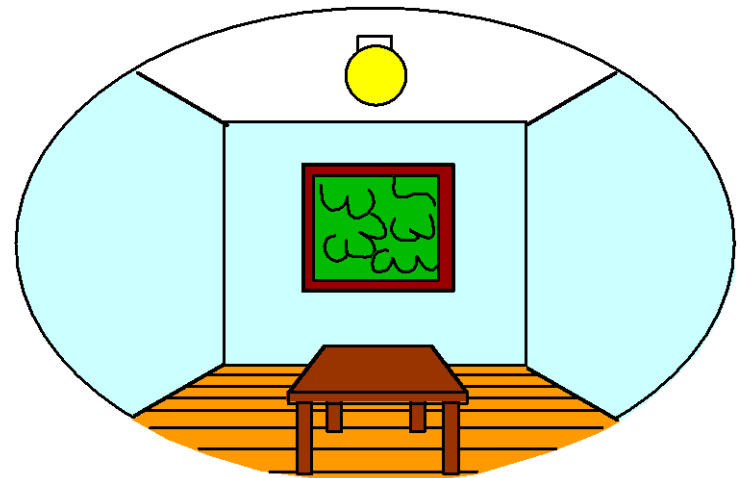


*3D world*



Point of observation

*2D image*

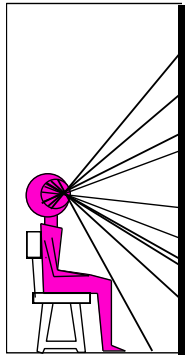


# What do we see?

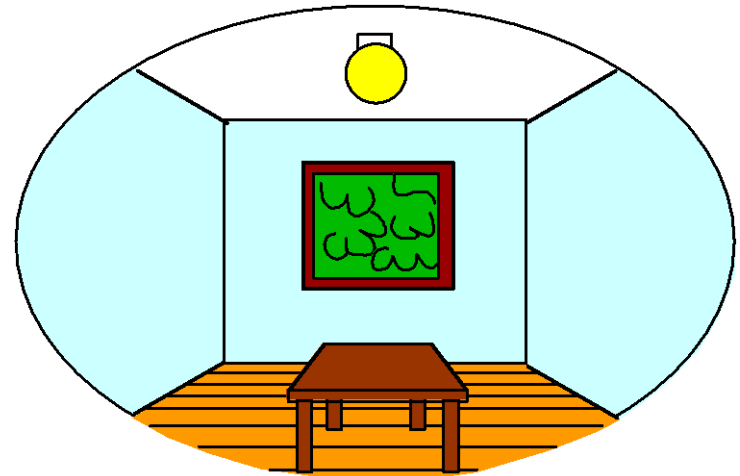


*3D world*

*2D image*



Painted  
backdrop



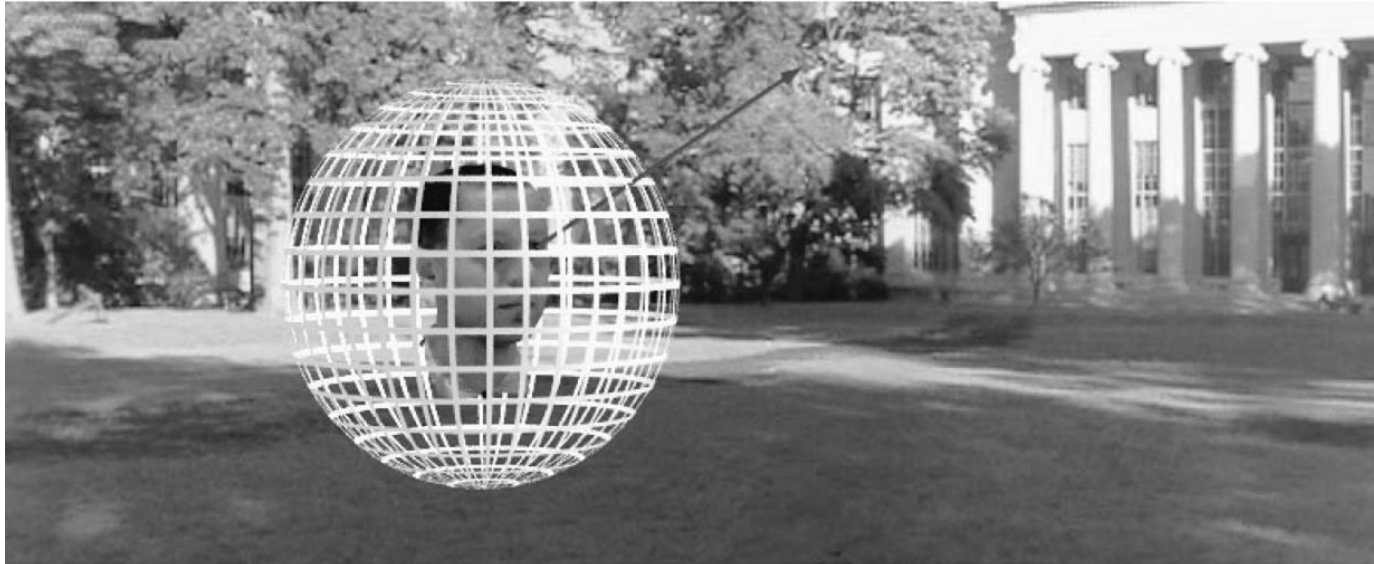
# The Plenoptic Function



Figure by Leonard McMillan

- Q: What is the set of all things that we can ever see?
- A: The Plenoptic Function (Adelson & Bergen)
- Let's start with a stationary person and try to parameterize everything that she can see...

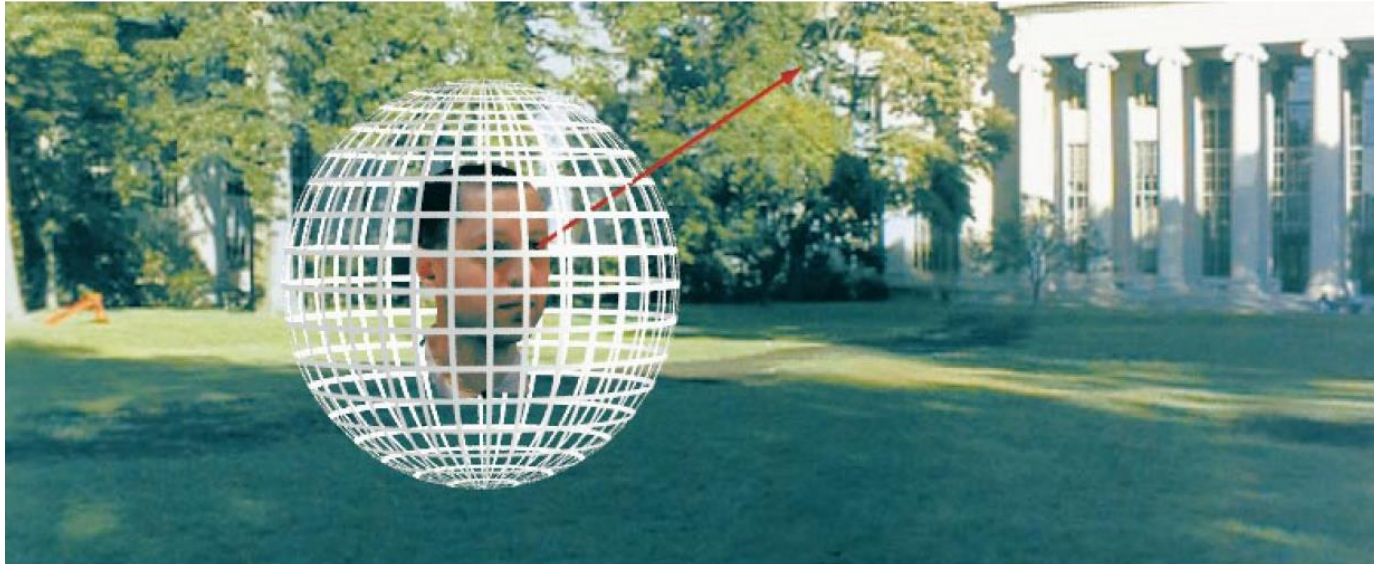
# Grayscale snapshot



$$P(\theta, \phi)$$

- is intensity of light
  - Seen from a single view point
  - At a single time
  - Averaged over the wavelengths of the visible spectrum
- (can also do  $P(x,y)$ , but spherical coordinate are nicer)

# Color snapshot



$$P(\theta, \phi, \lambda)$$

- is intensity of light
  - Seen from a single view point
  - At a single time
  - As a function of wavelength

# A movie

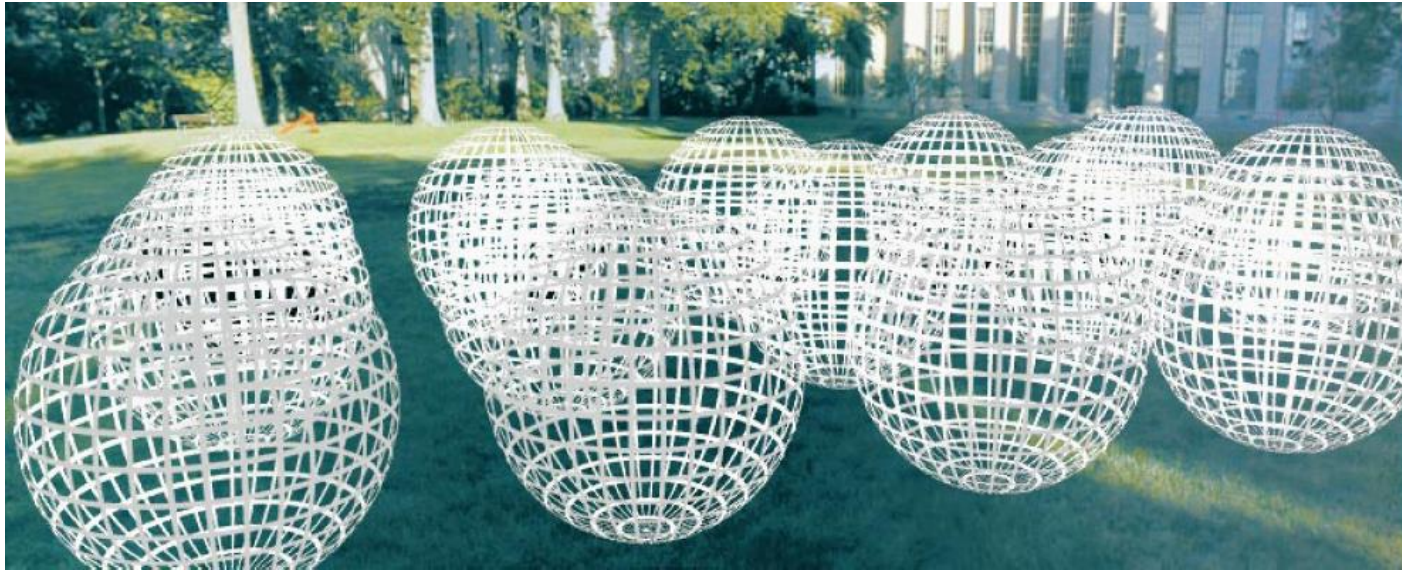
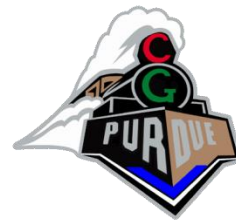


$$P(\theta, \phi, \lambda, t)$$

- is intensity of light
  - Seen from a single view point
  - Over time
  - As a function of wavelength



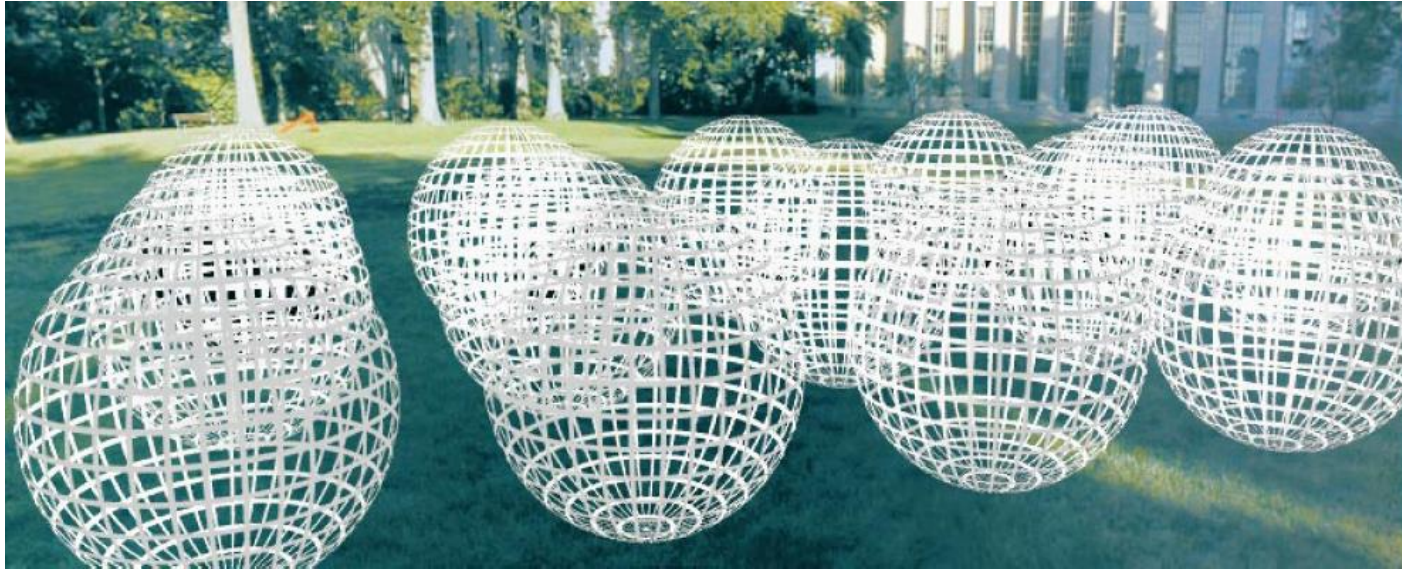
# Holographic movie



$$P(\theta, \phi, \lambda, t, V_x, V_y, V_z)$$

- is intensity of light
  - Seen from ANY viewpoint
  - Over time
  - As a function of wavelength

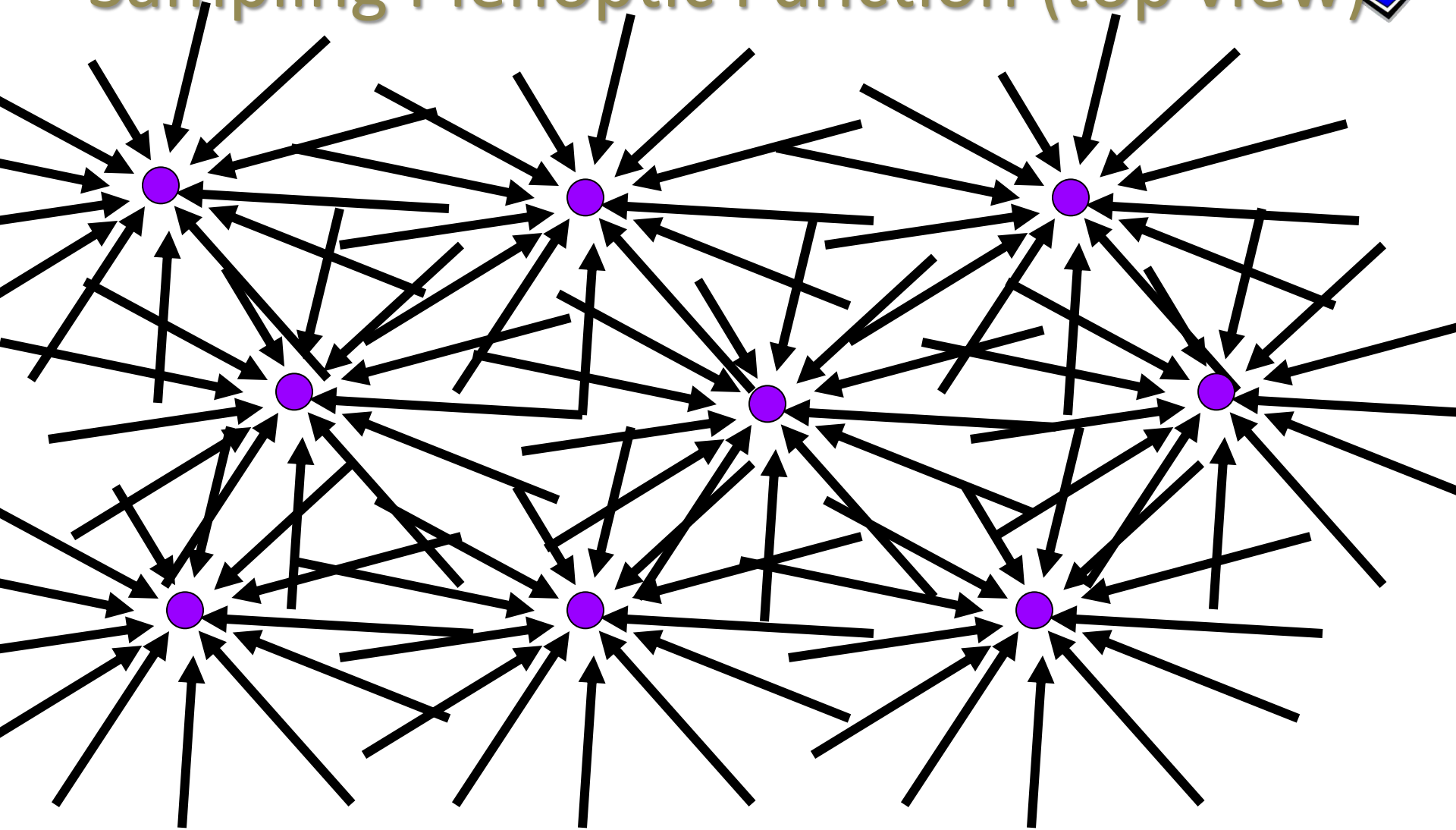
# The Plenoptic Function



$$P(\theta, \phi, \lambda, t, V_x, V_y, V_z)$$

- Can reconstruct every possible view, at every moment, from every position, at every wavelength
- Contains every photograph, every movie, everything that anyone has ever seen.

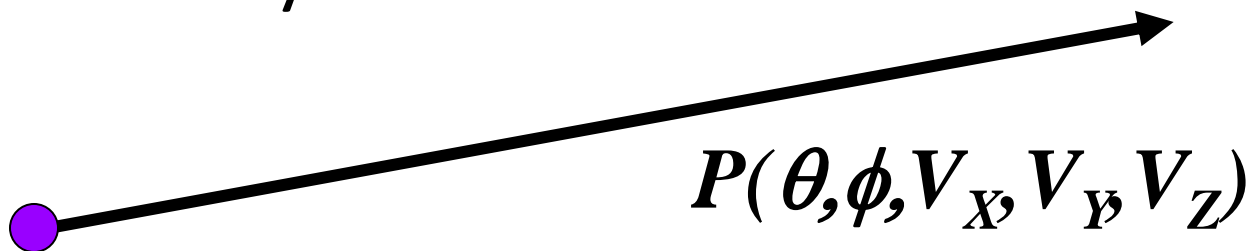
# Sampling Plenoptic Function (top view)





# Ray

- Let's not worry about time and color:



- 5D
  - 3D position
  - 2D direction



# Plenoptic Function

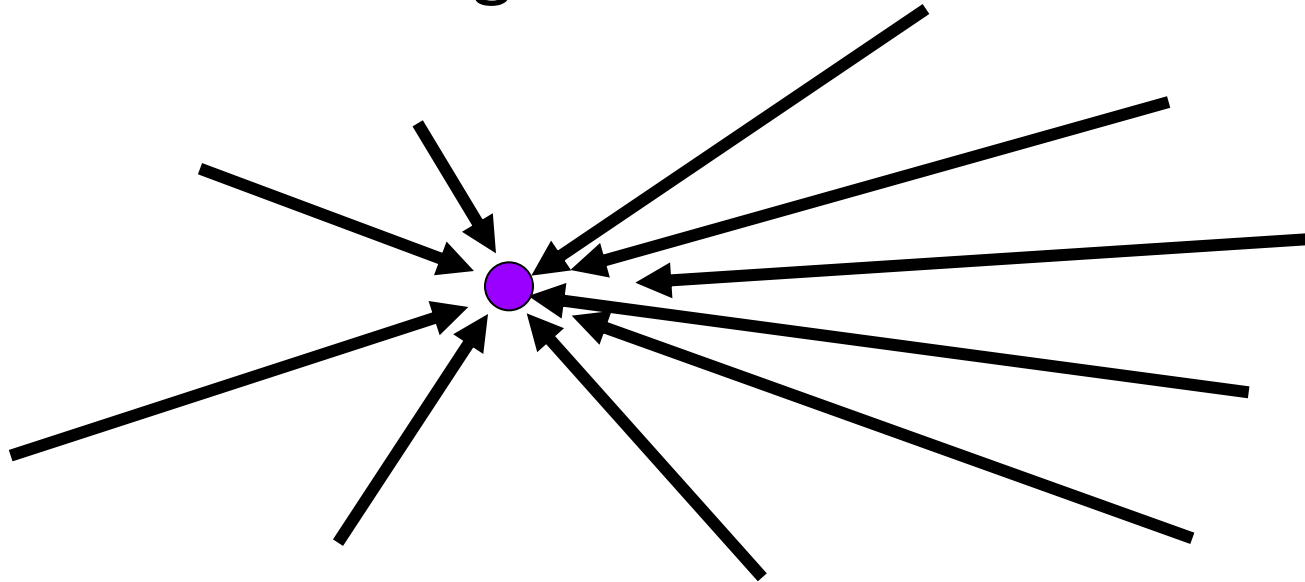
- “Holodeck” (Star Trek)
- Layered Depth Images [Shade98]
- 3D Image Warping [Max95, McMillan95, ...]
- View Interpolation [Chen93]
- Sea of Images [Aliaga01]
- Lightfield/Lumigraph [Levoy96, Gortler96]
- Plenoptic Stitching [Aliaga99]
- Concentric Mosaics [Shum99]
- Panoramic Images [Szeliski97, ...]





# 2D: Image

- What is an image?

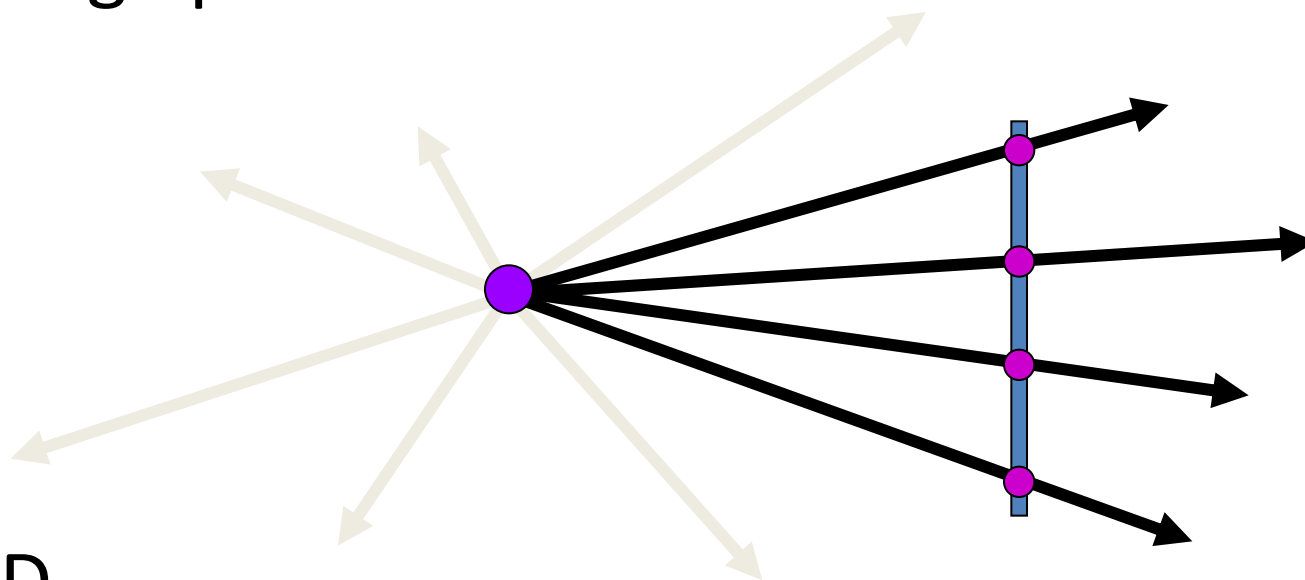


- All rays through a point



# 2D: Image

- Image plane



- 2D
  - position



# 2D: Spherical Panorama



See also: 2003 New Years Eve  
<http://www.panoramas.dk/fullscreen3/f1.html>

- All light rays through a point form a panorama
- Totally captured in a 2D array --  $P(\theta, \phi)$





# 3D: Space-Time

- Moving in time:
  - Spatio-temporal volume:  $P(\theta, \phi, t)$
  - Useful to study temporal changes
  - Long an interest of artists:

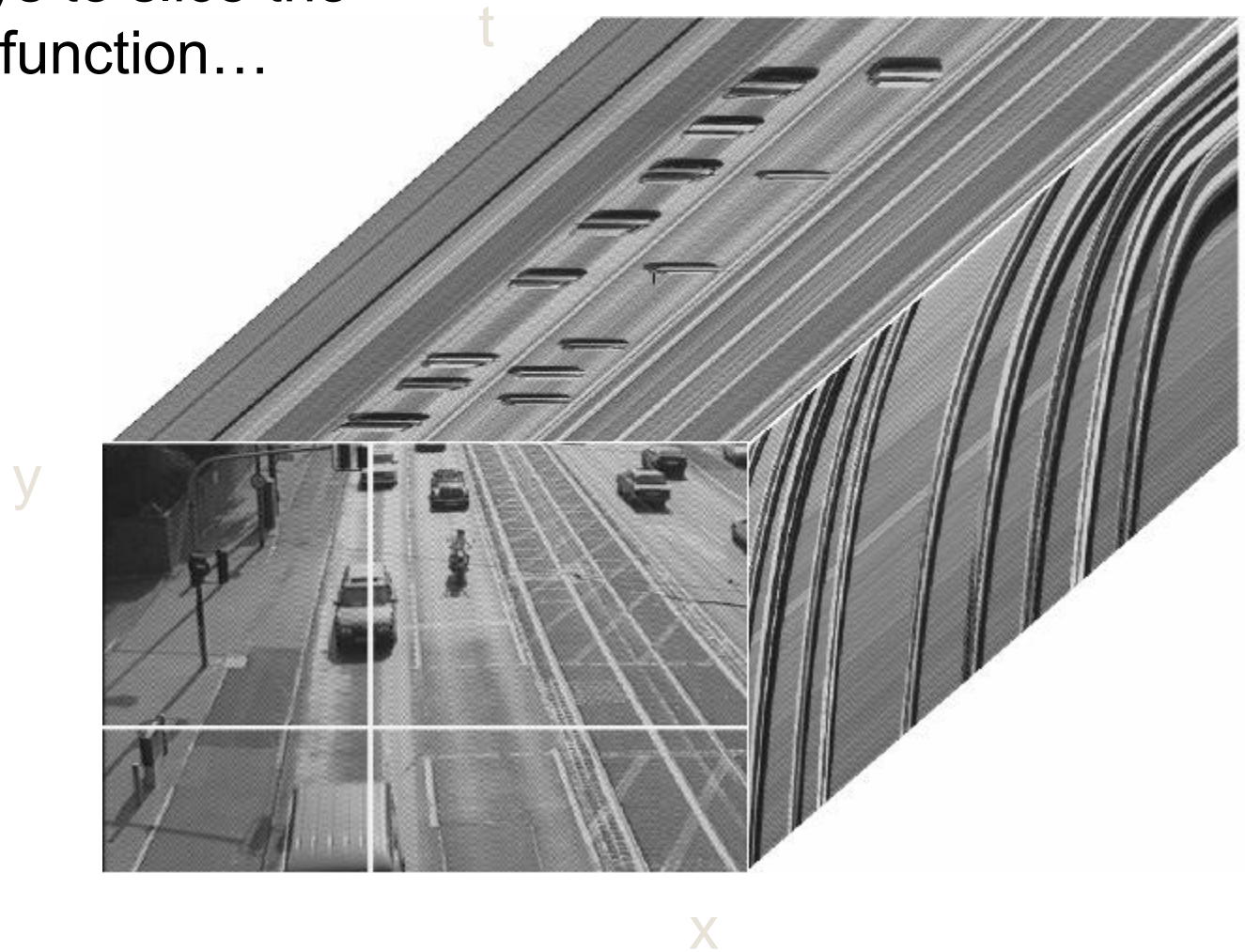


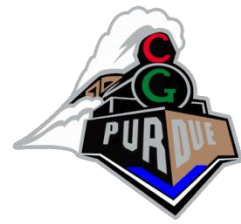
Claude Monet, Haystacks studies



# 3D: Space-Time

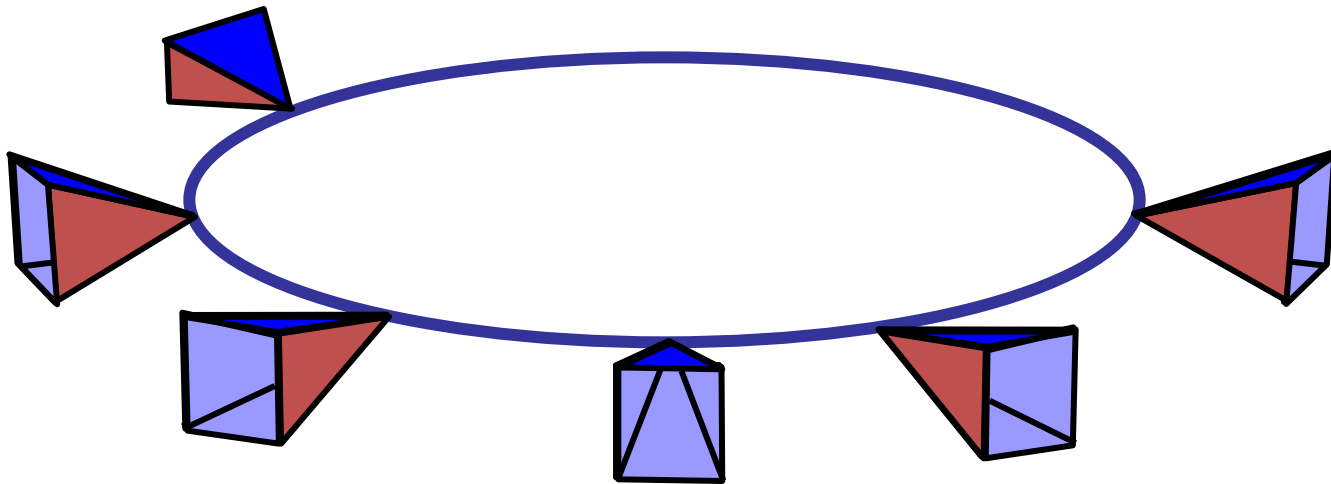
Other ways to slice the plenoptic function...





## 3.5D: Concentric Mosaics

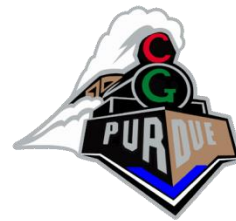
- Replace “row” with “circle” of images





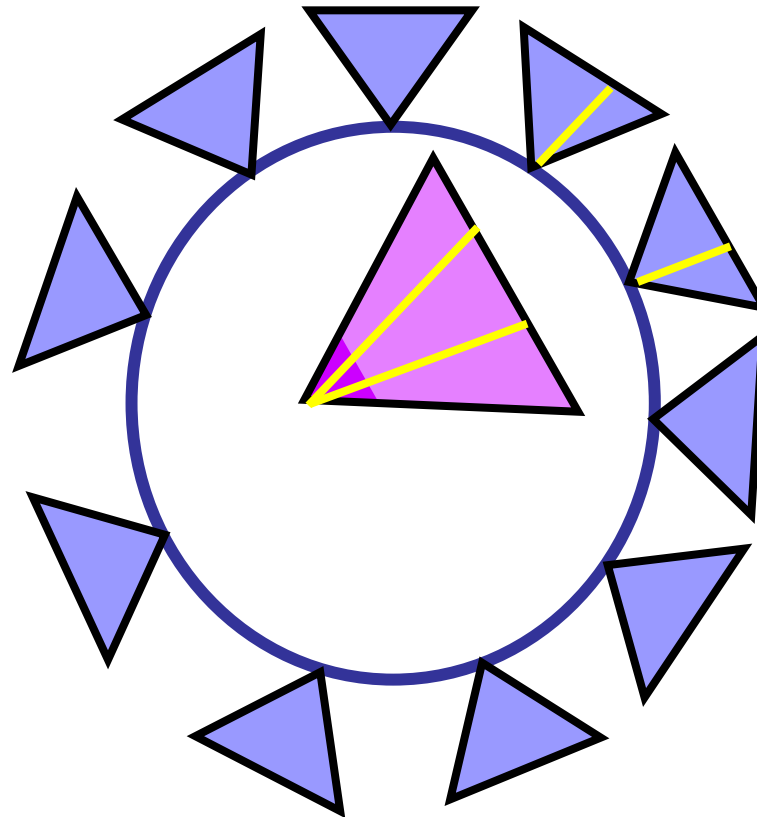
# 3.5D: Concentric Mosaics





# 3.5D: Concentric Mosaics

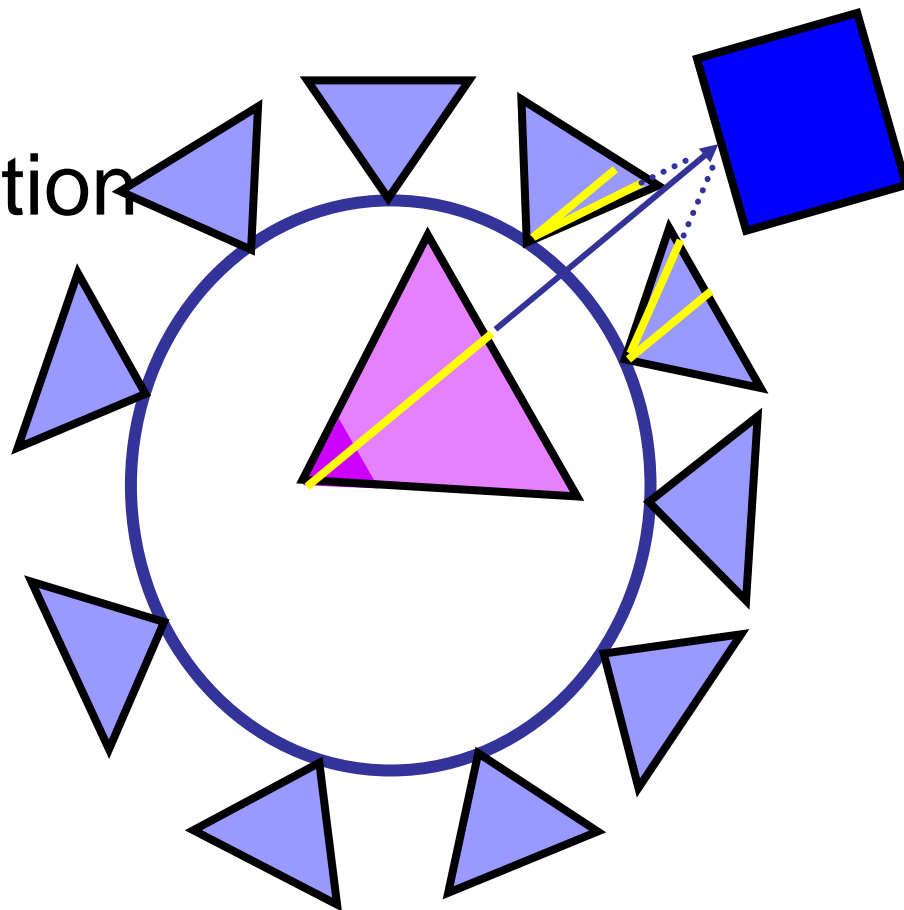
- From above





# Concentric Mosaics

Depth correction





# Concentric Mosaics

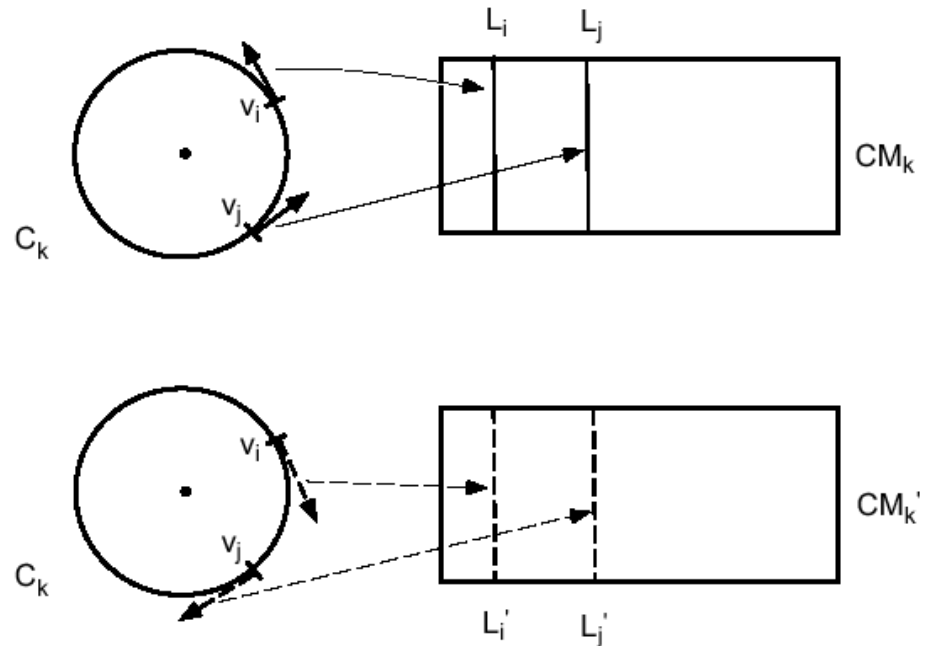
## □ Panorama





# Concentric Mosaics

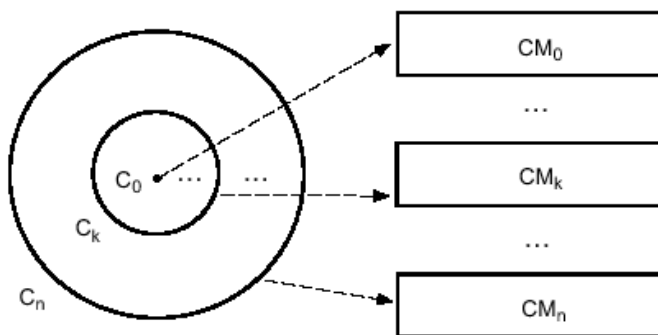
- A set of manifold mosaics constructed from slit images taken by cameras rotating on concentric circles





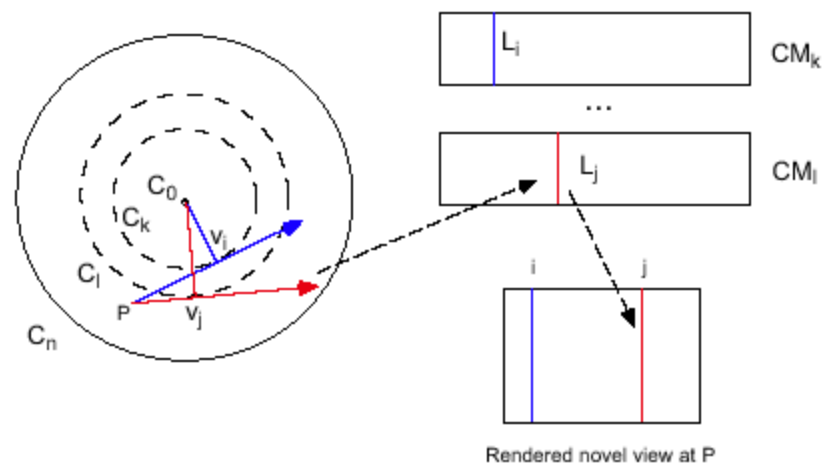


# Sample Images

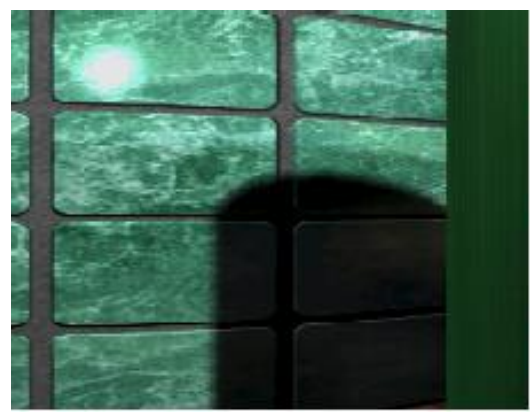
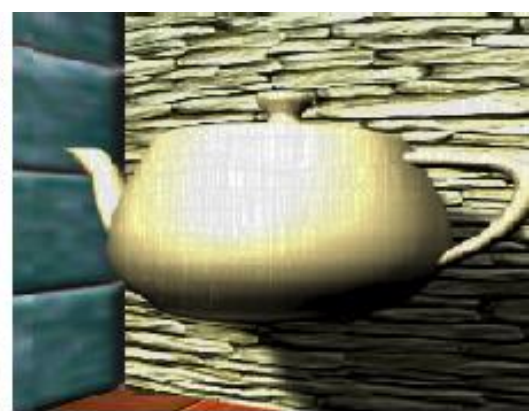
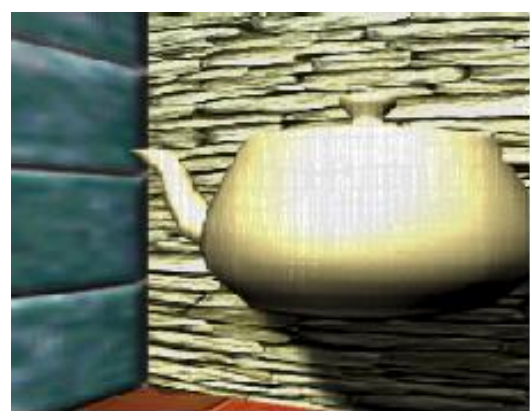




# Rendering a Novel View



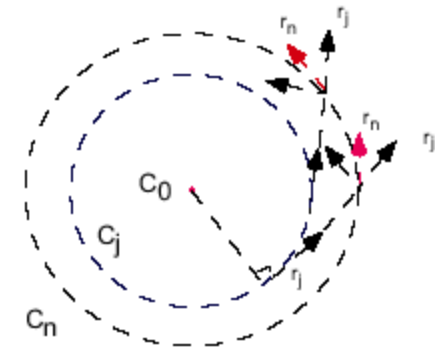
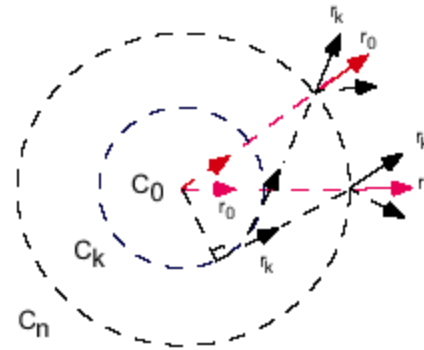
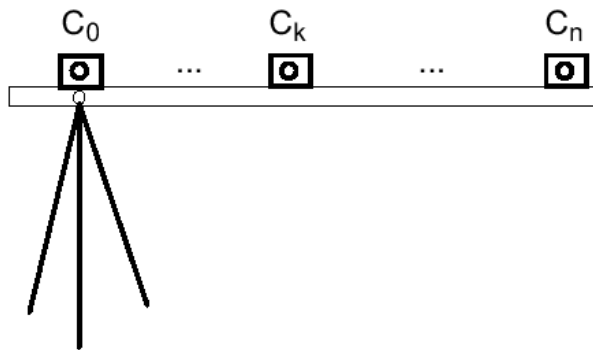
Rendered novel view at P





# Construction of Concentric Mosaics (2)

- Real scenes



(a)

(b)

Figure 10: Construction of concentric mosaics from one circle: camera along (a) normal direction; (b) tangential direction.

Bulky,  
costly

Cheaper,  
easier



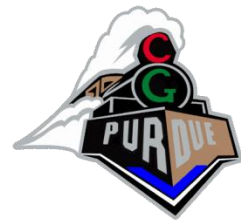
# Results



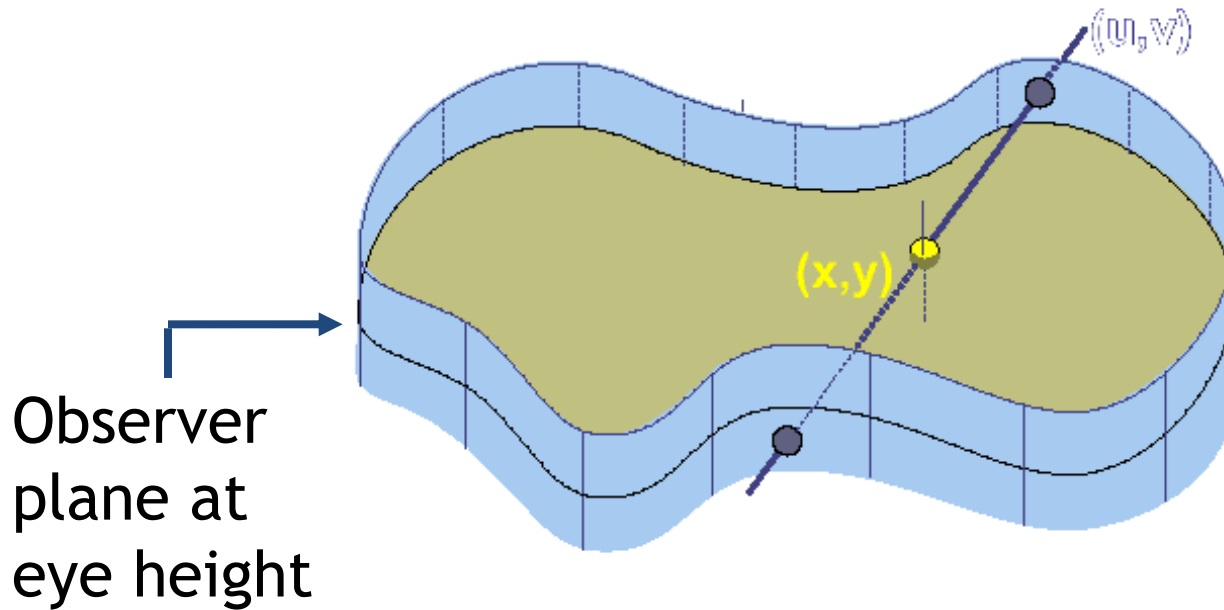
# Issues with Concentric Mosaics



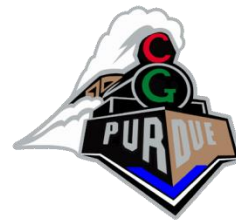
- **Only has horizontal parallax effects**
- Limited horizontal fov
- Non-uniform spatial horizontal resolution



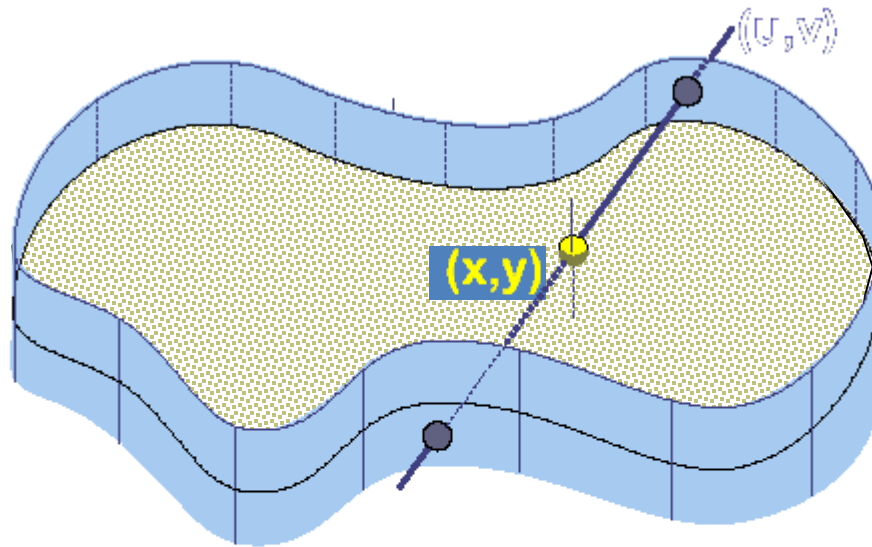
# 3.5D: Plenoptic Stitching



- 4D parameterization of the plenoptic function suitable for walkthrough applications



# 3.5D: Plenoptic Stitching

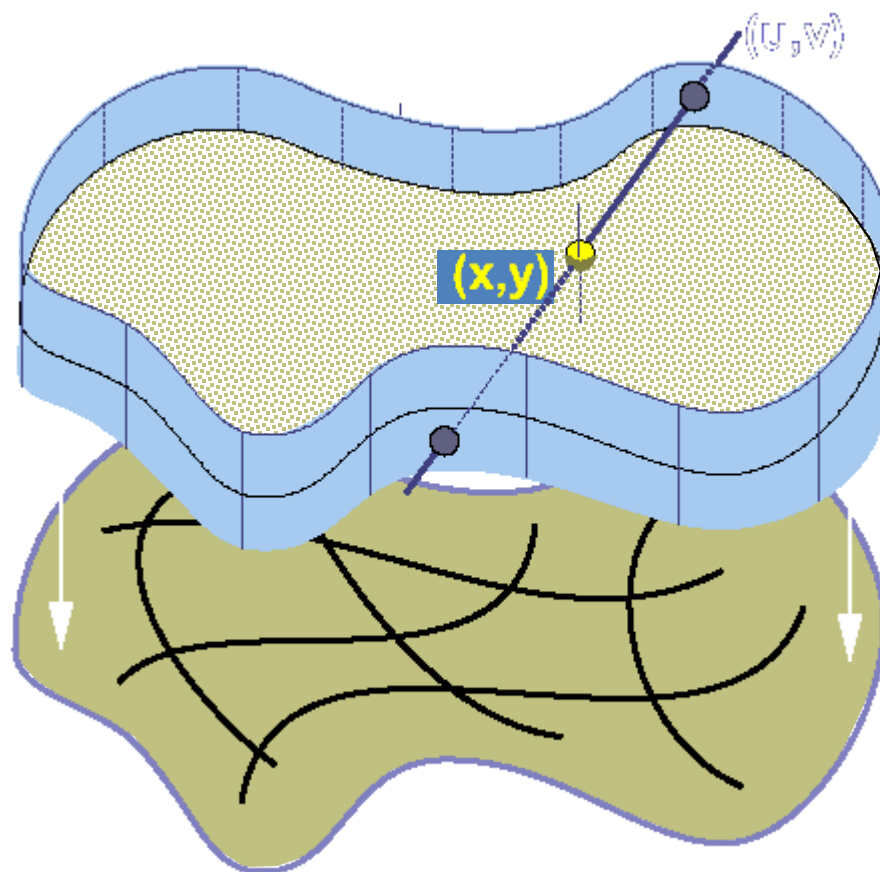


Ideally:

Dense  
Sampling



# 3.5D: Plenoptic Stitching



Ideally:

Dense  
Sampling

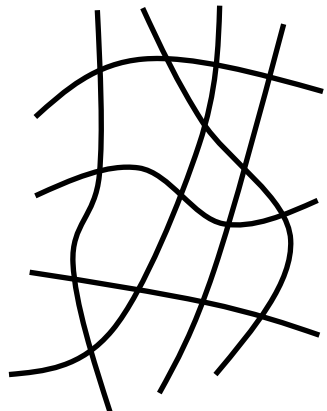
Instead:

Image Loop  
Sampling



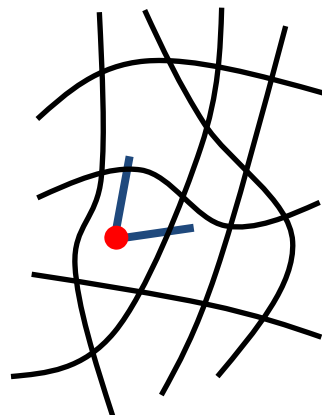


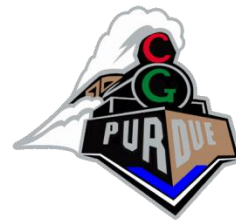
# 3.5D: Plenoptic Stitching





# 3.5D: Plenoptic Stitching





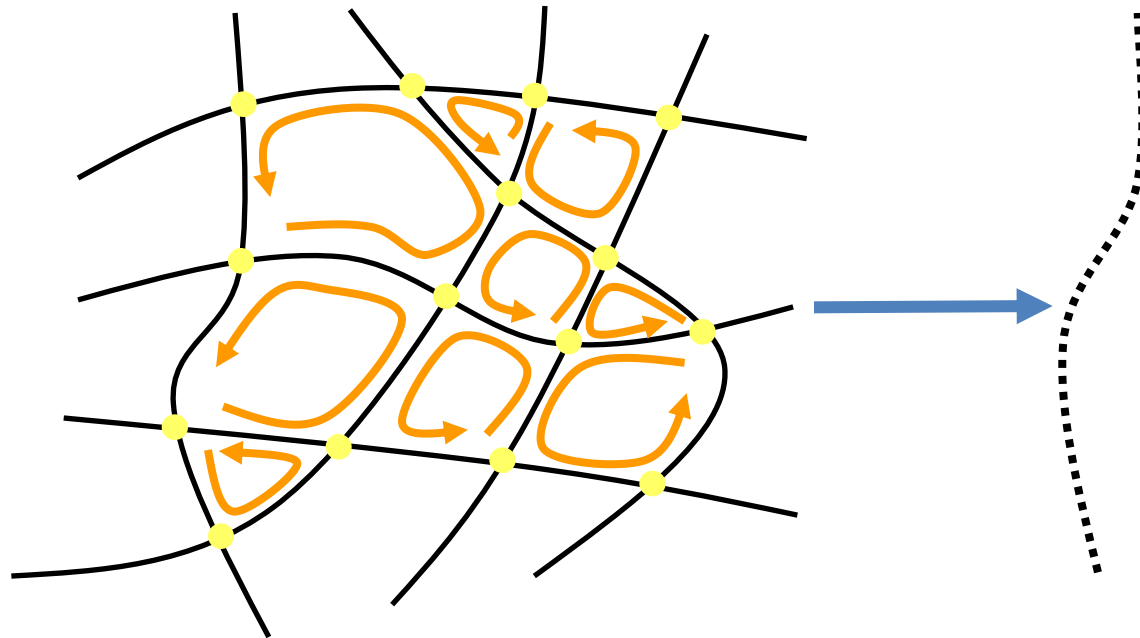
## 3.5D: Plenoptic Stitching

- Advantages:
  - **Gives horizontal and vertical parallax!**
- Problems:
  - How do we sample the environment with image loops?
  - How do we reconstruct the environment for a viewpoint within an image loop?



# Capture

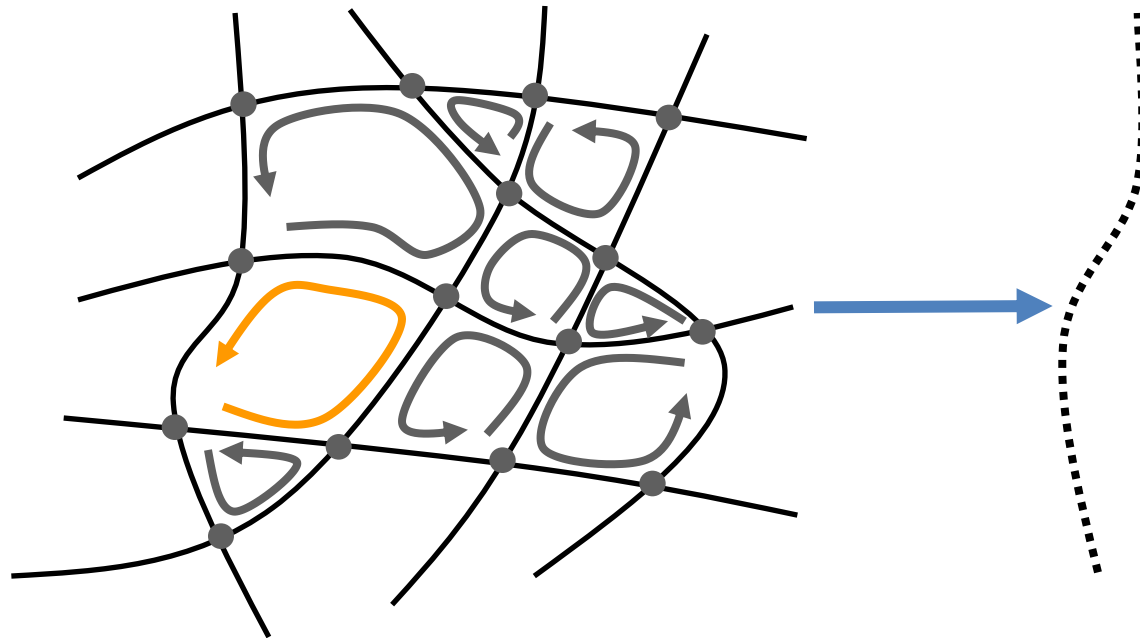
- Image loop creation
  - Each path is simply a sequence of images
  - We intersect the paths and determine image loops

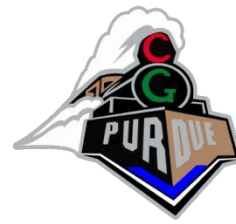




# Capture

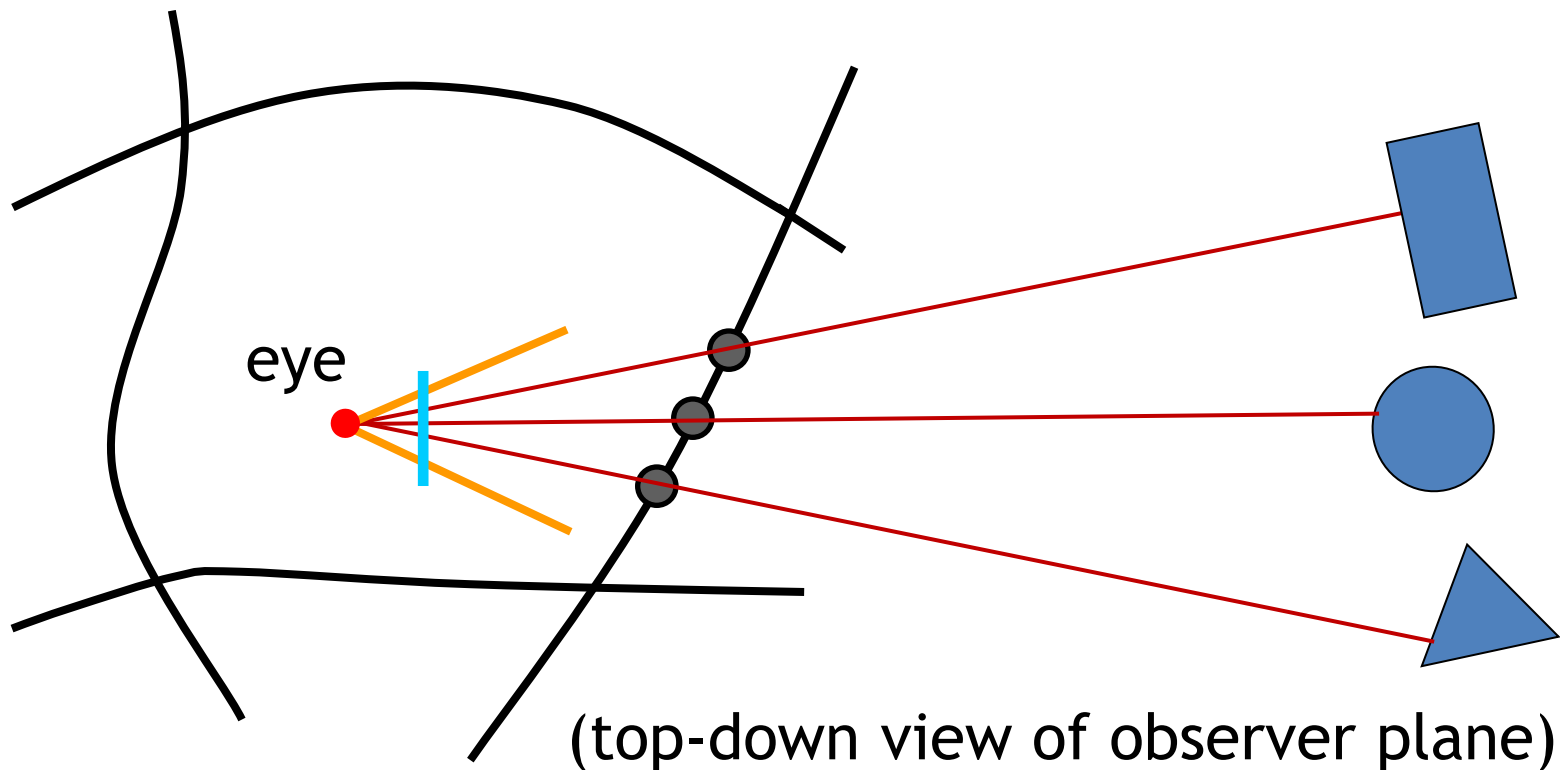
- Image loop creation
  - Each path is simply a sequence of images
  - We intersect the paths and determine image loops





# 2D Reconstruction

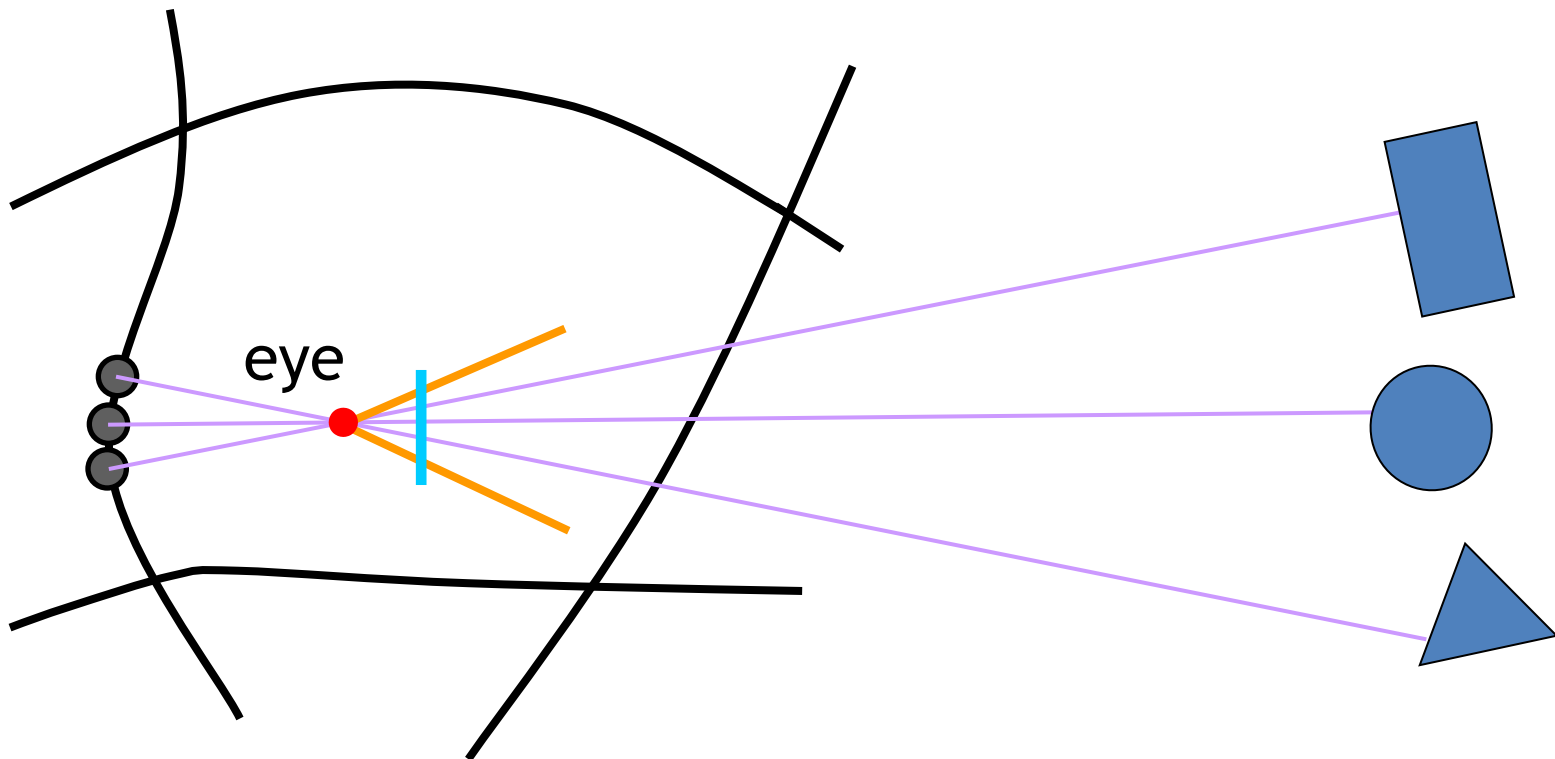
- Extract from the **front** omnidirectional images the desired light rays





# 2D Reconstruction

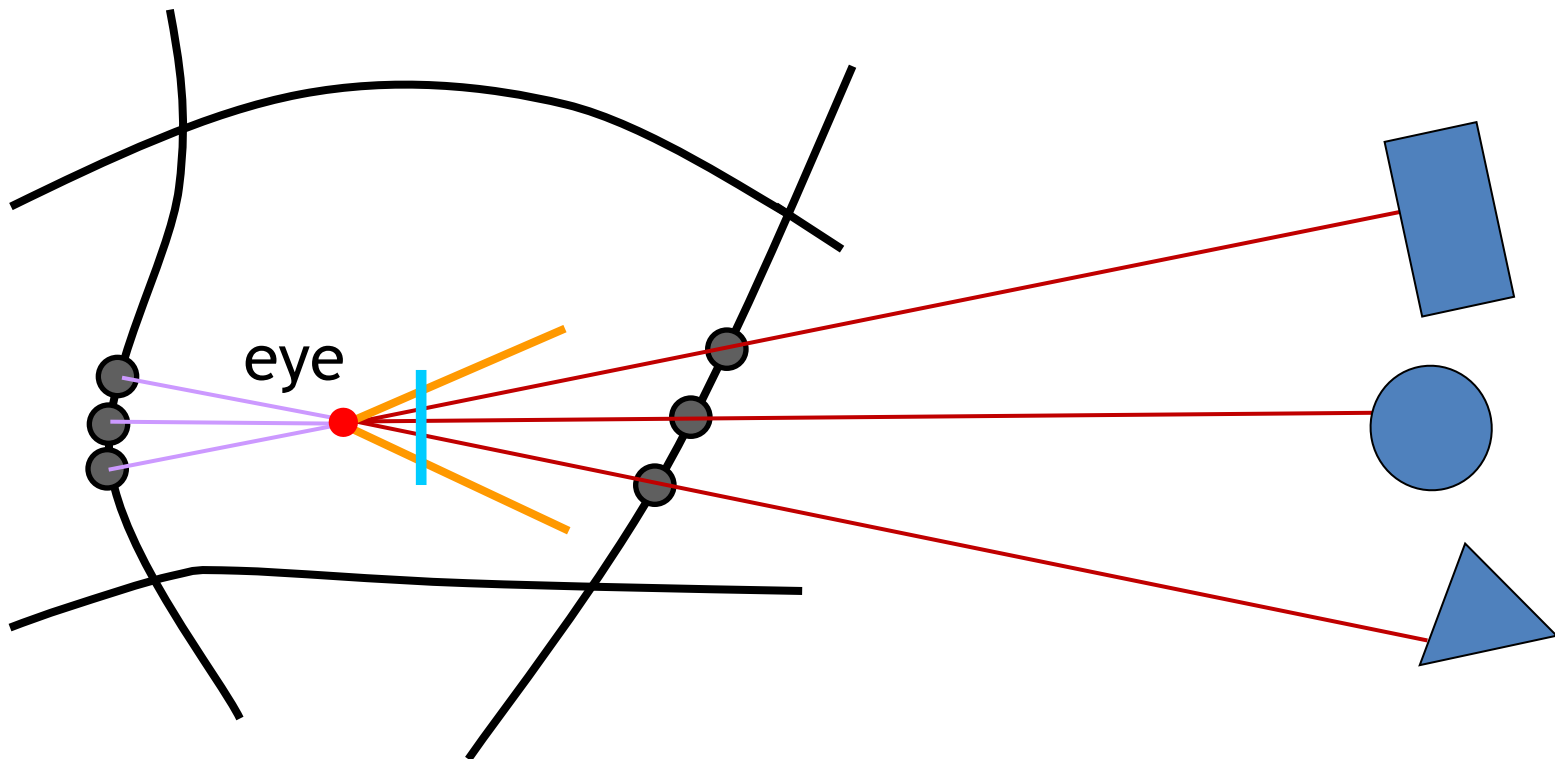
- Extract from the **back** omnidirectional images the desired light rays





# 2D Reconstruction

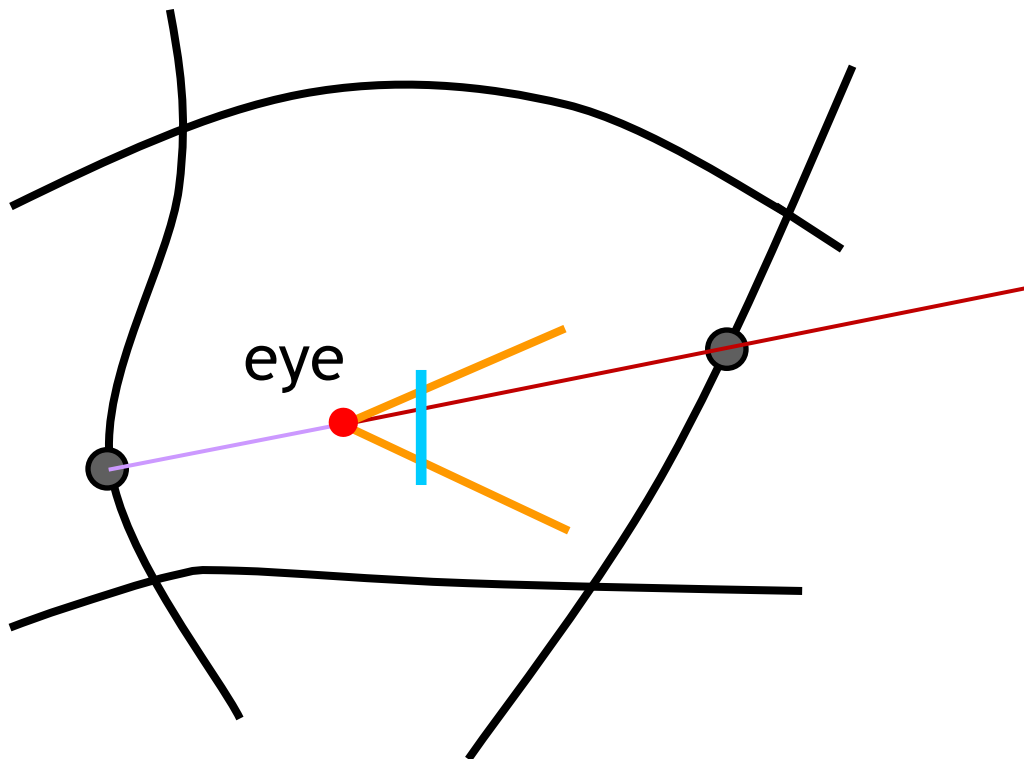
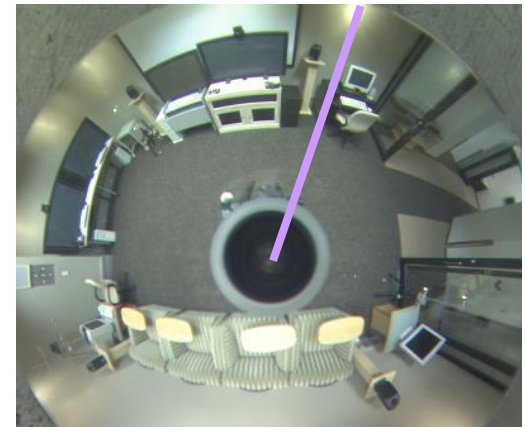
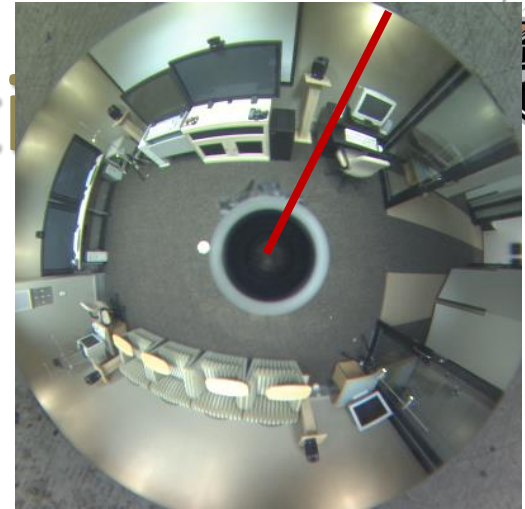
- Extract from the **front** and **back** omnidirectional images an average of the desired light rays





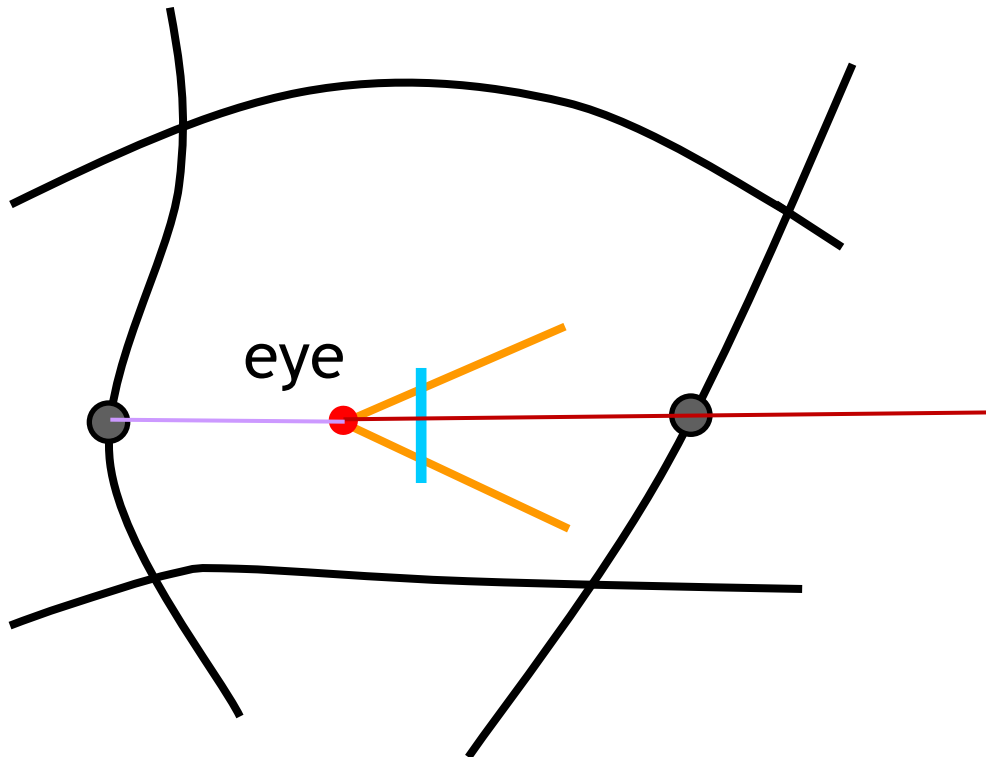
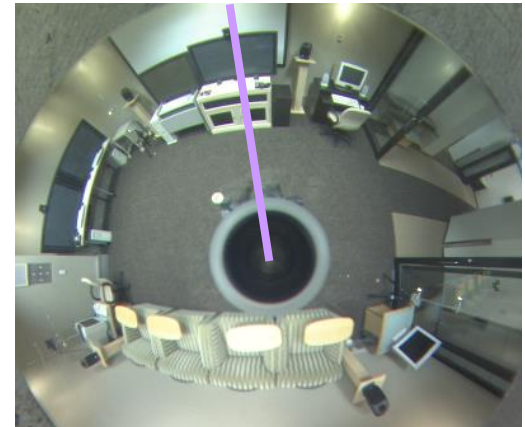
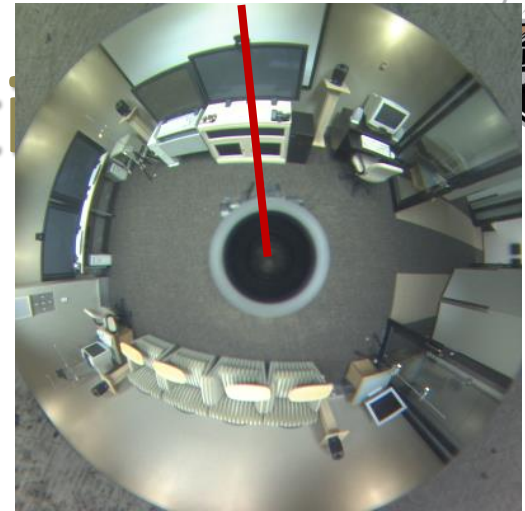
# 3D Reconstruction

- Extract from the omnidirectional images an average of the **columns** (or radial lines) of light rays



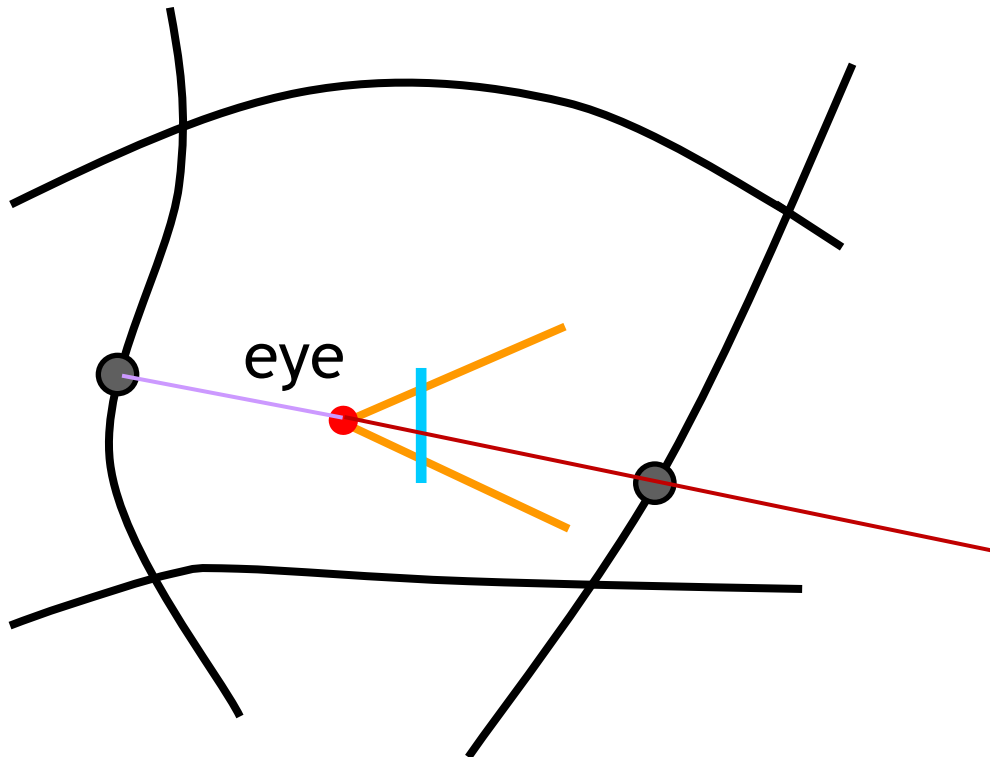
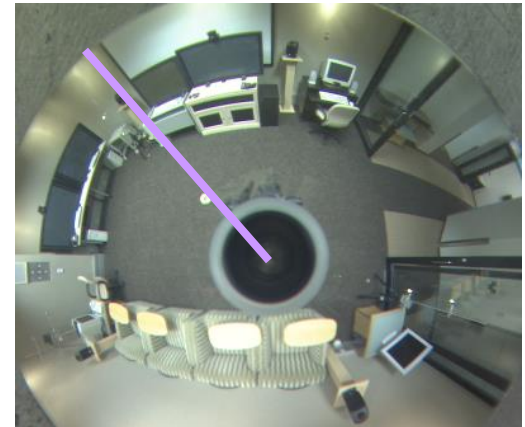
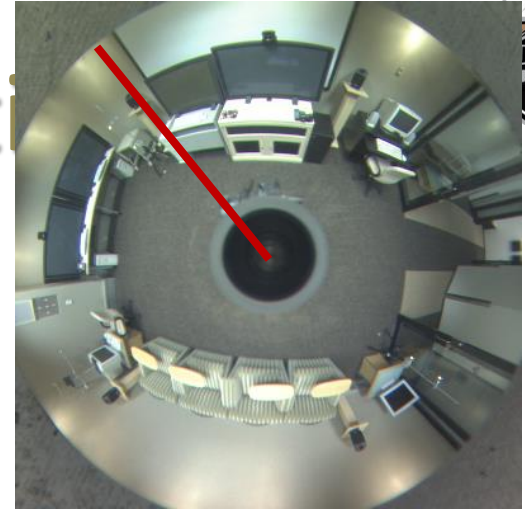
# 3D Reconstruction

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# 3D Reconstruction

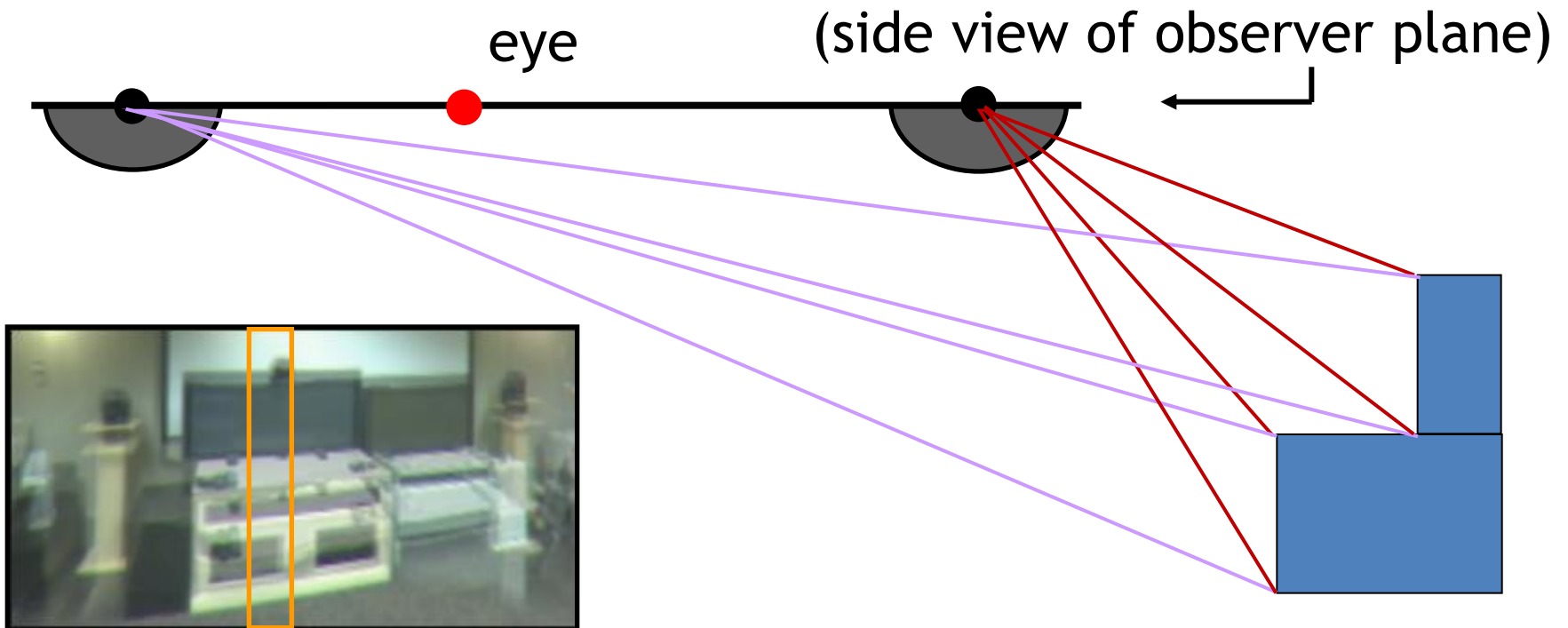
- Extract from the omnidirectional images an average of the **columns** (or radial lines) of light rays





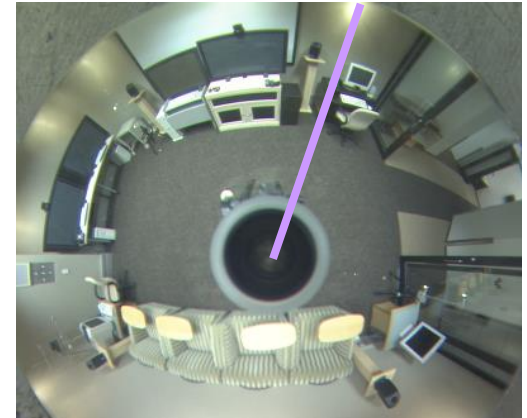
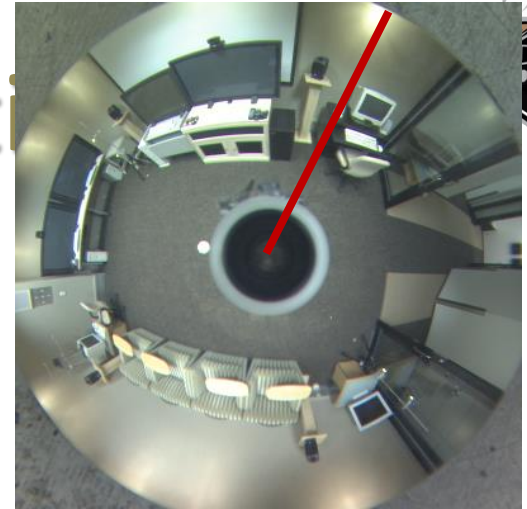
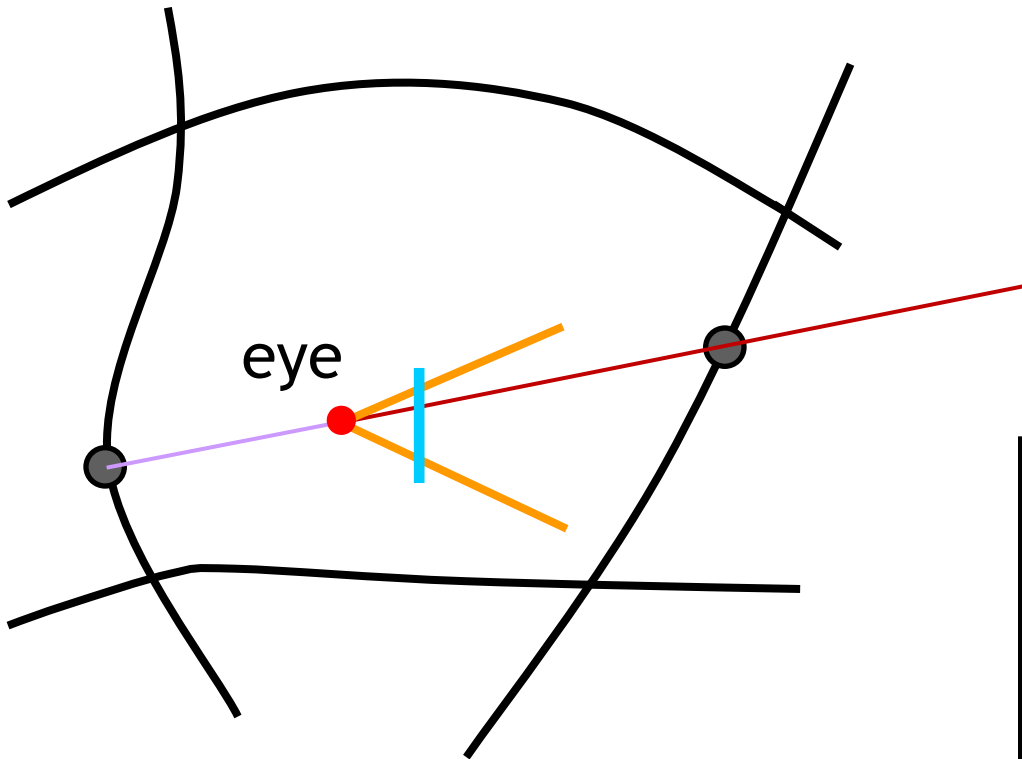
# 3D Reconstruction

- Why does this not work?
  - Because we do not have samples of the desired **column** of light rays



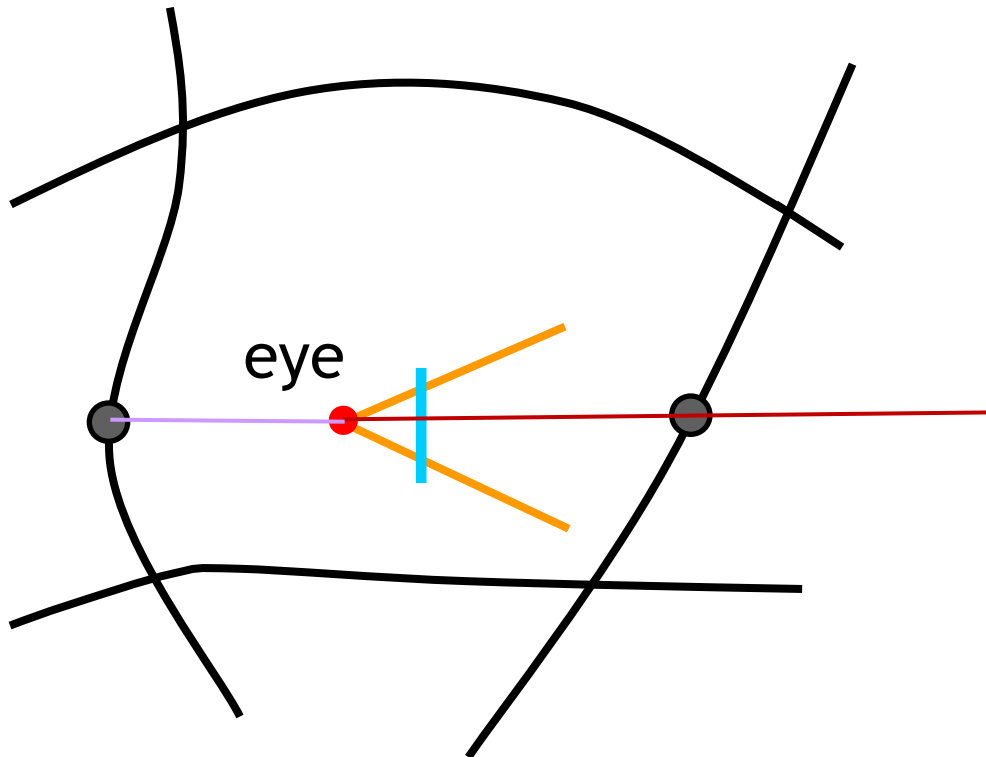
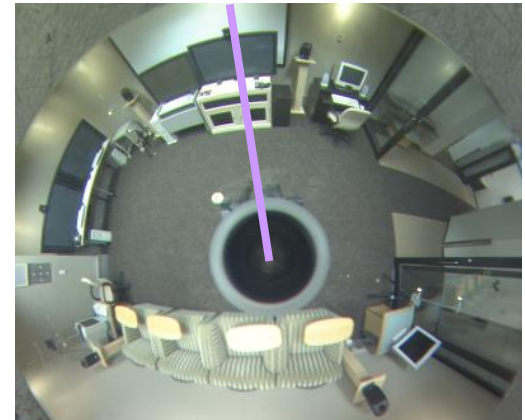
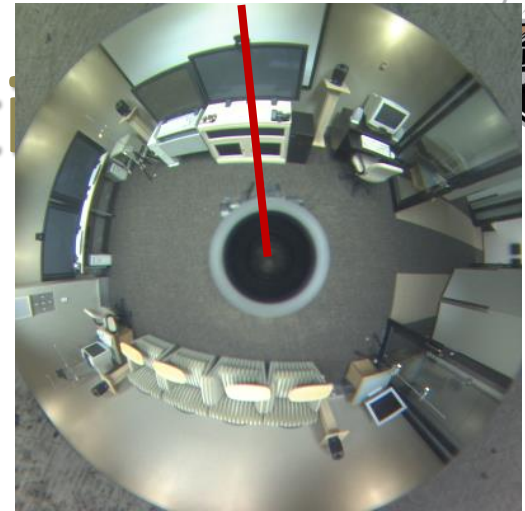
# 3D Reconstruction

- We perform a nonlinear interpolation between columns (or radial lines) of light rays



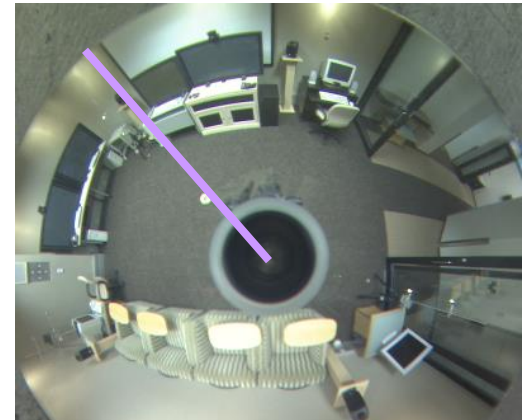
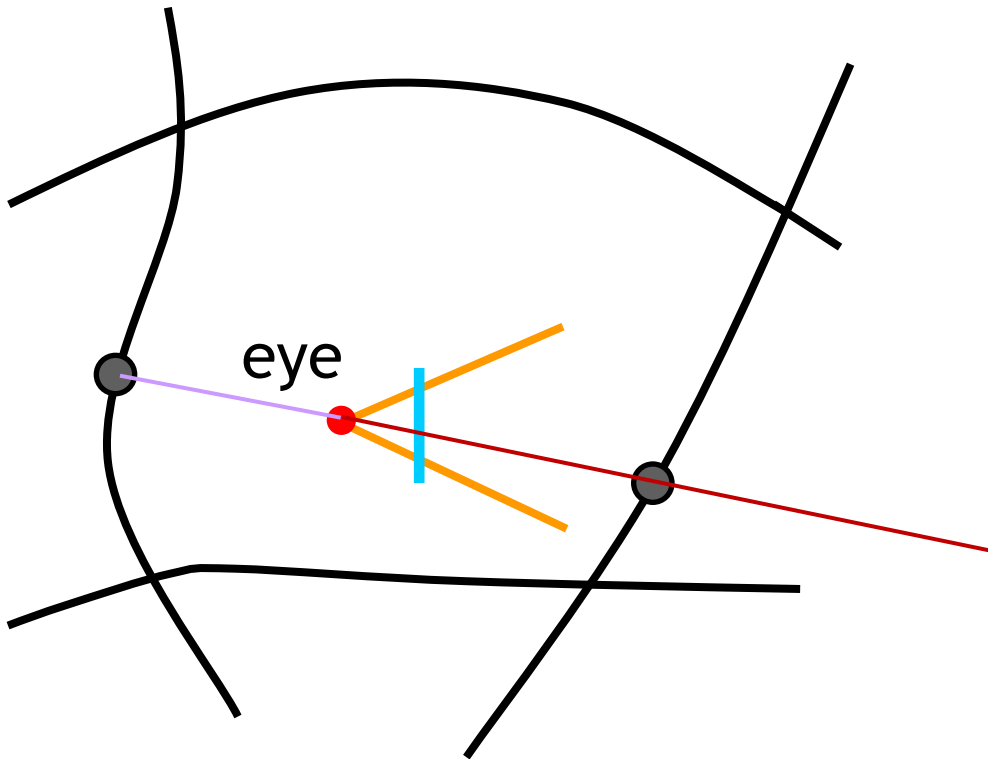
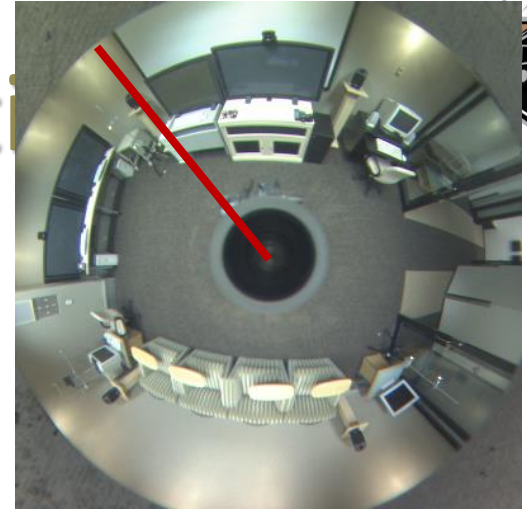
# 3D Reconstruction

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# 3D Reconstruction

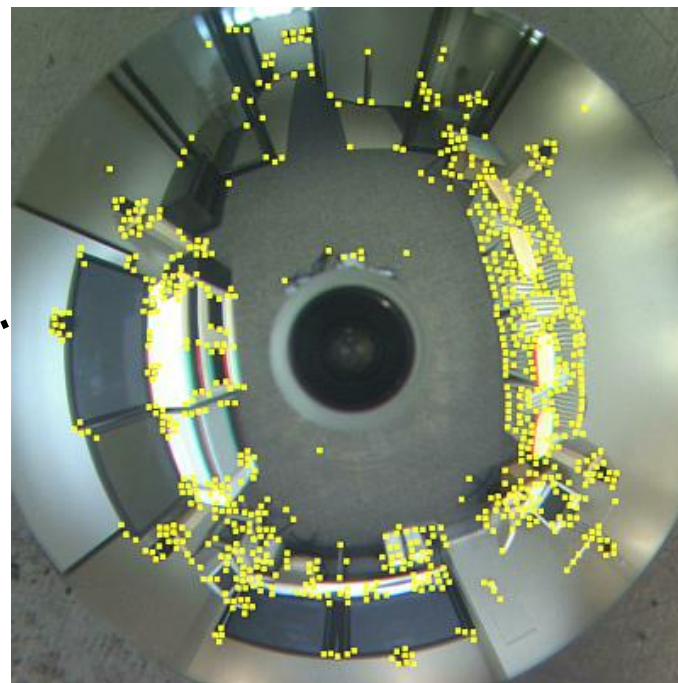
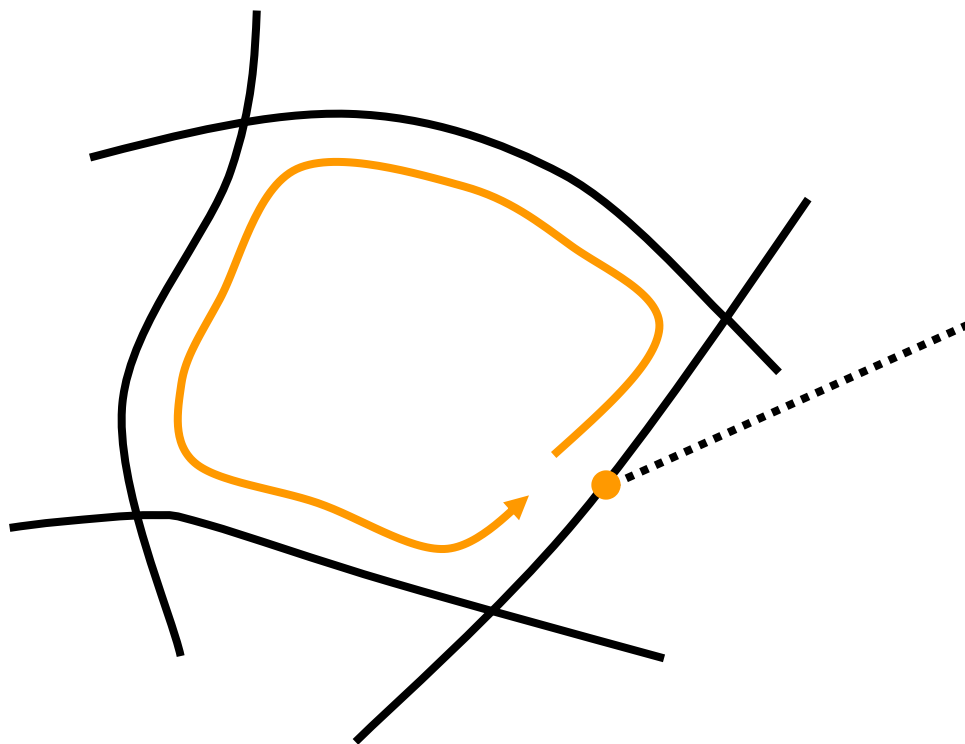
- We perform a nonlinear interpolation between columns (or radial lines) of light rays





# Reconstruction

- To interpolate, we first track features from frame-to-frame around the loop

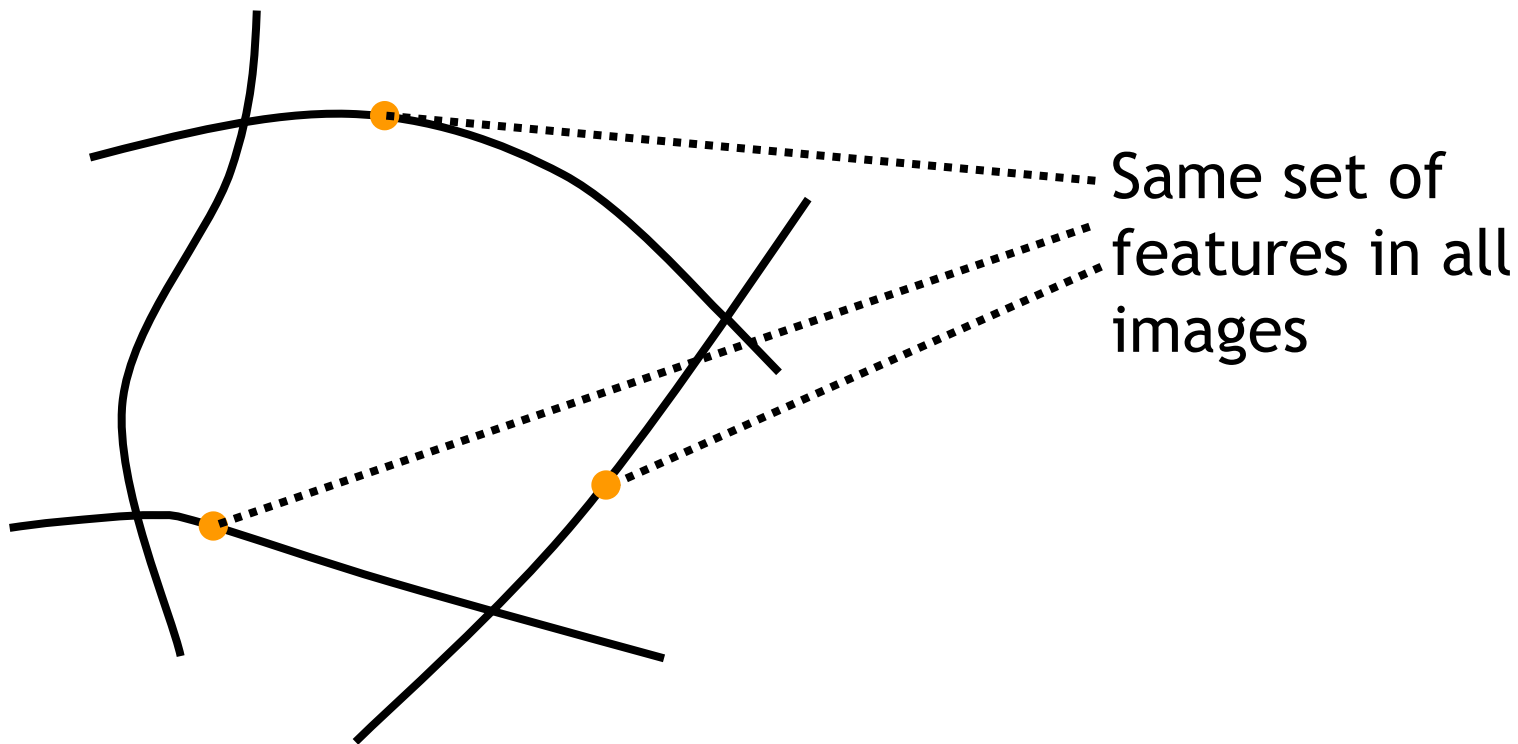






# Reconstruction

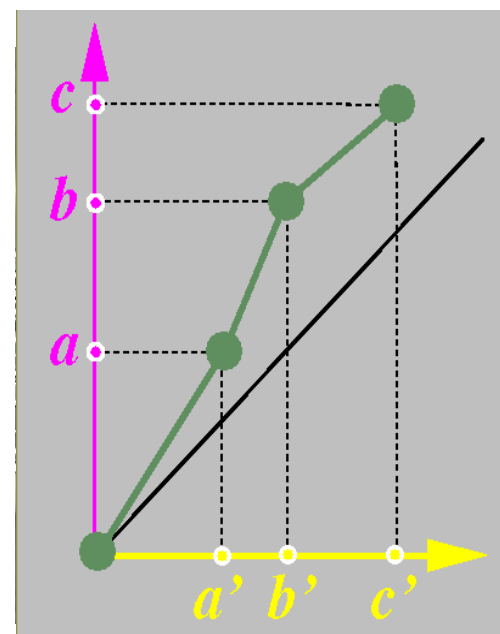
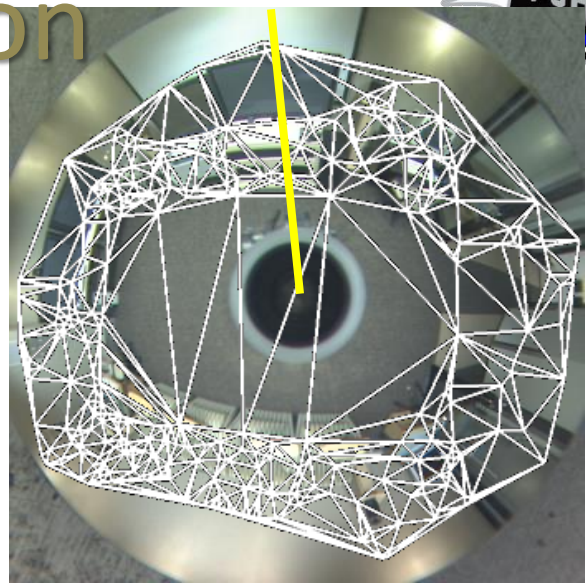
- Keeping only those features successfully tracked all the way around the loop

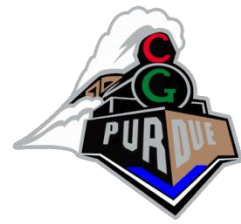




# Reconstruction

- For each omnidirectional image pair, **triangulate** tracked features
- **Intersect** the triangulation edges with the radial lines
- Establish a **mapping** between segments of the radial line pairs and use this to warp pixels to the intermediate viewpoint



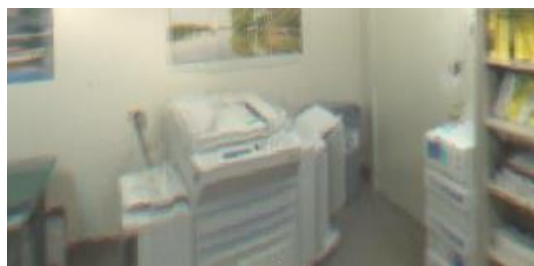


# Implementation Issues

- Optimizations
  - Compensate for horizontal (angular) misalignment
  - Compensate for vertical misalignment
- Reconstruction Acceleration
  - Pre-compute radial line mappings
  - Optionally warp pixels using lower-resolution information
- Caches and Compression
  - Data compressed using JPEG and Lempel-Ziv
  - Three LRU caches: (1) compressed bitstreams, (2) uncompressed image subsets, (3) uncompressed mappings



# Results: Examples



**Reconstructions for novel viewpoints near the middle of several image loops within various environments (generated at 5-10 fps)**

# Results: Image Comparison



**Reconstructed** image for a viewpoint near the middle of an image loop (where reconstruction is most difficult)

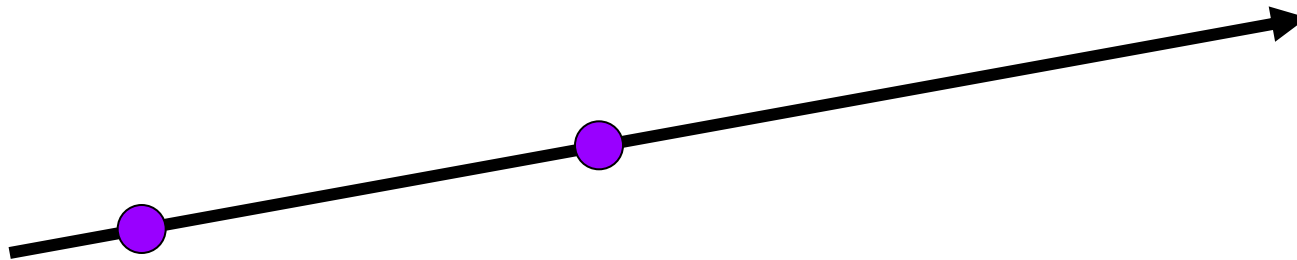


**Captured** image from approximately the same viewpoint



# 4D: Rays in a Vacuum

- Infinite line
  - Assume light is constant (vacuum)



- 4D
  - 2D direction
  - 2D position
  - non-dispersive medium



# Only need plenoptic surface

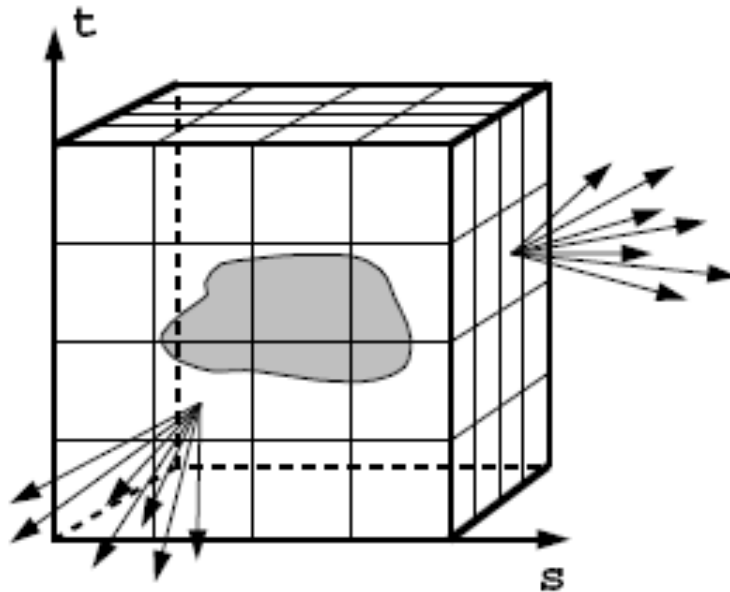
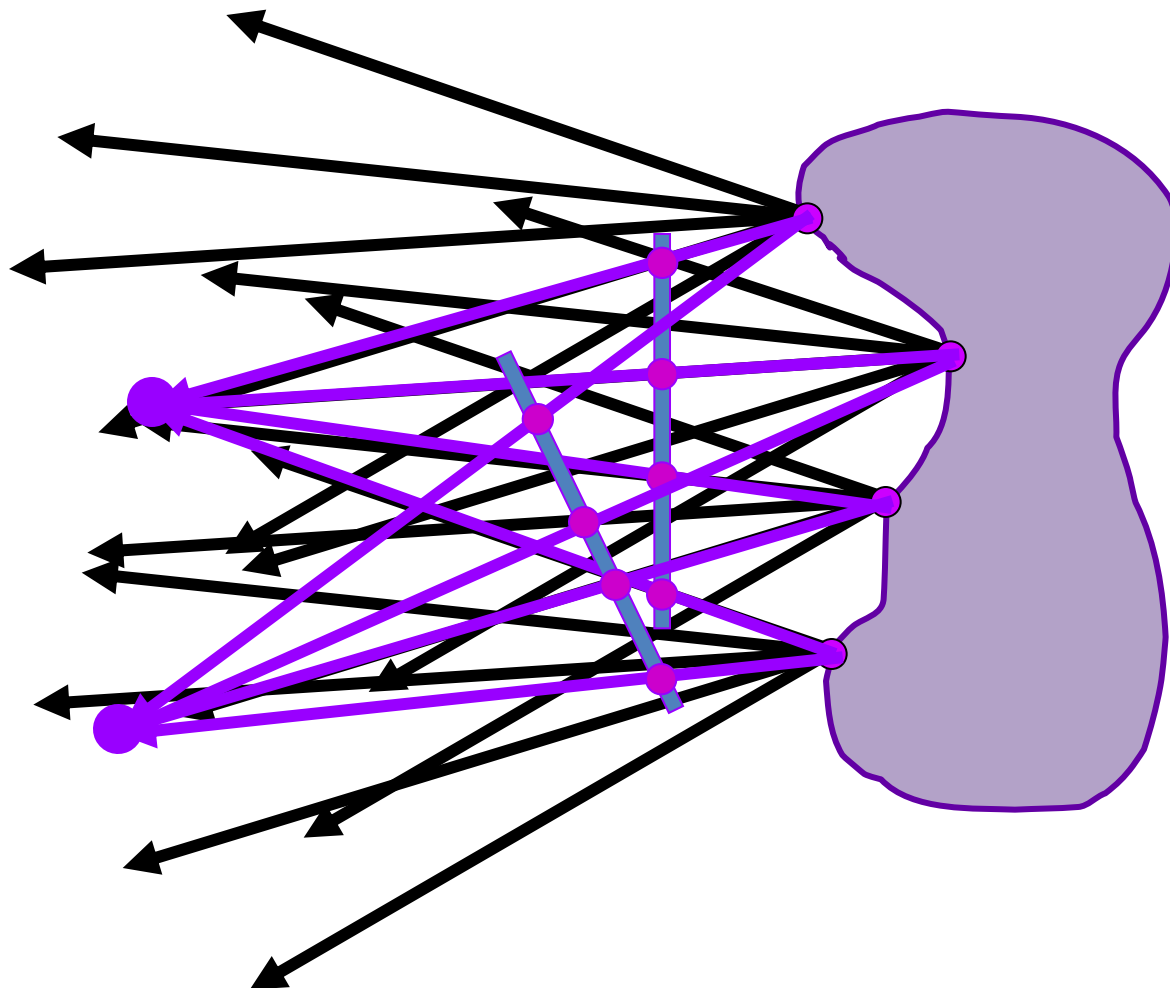


Figure 1: The surface of a cube holds all the radiance information due to the enclosed object.

# Synthesizing novel views

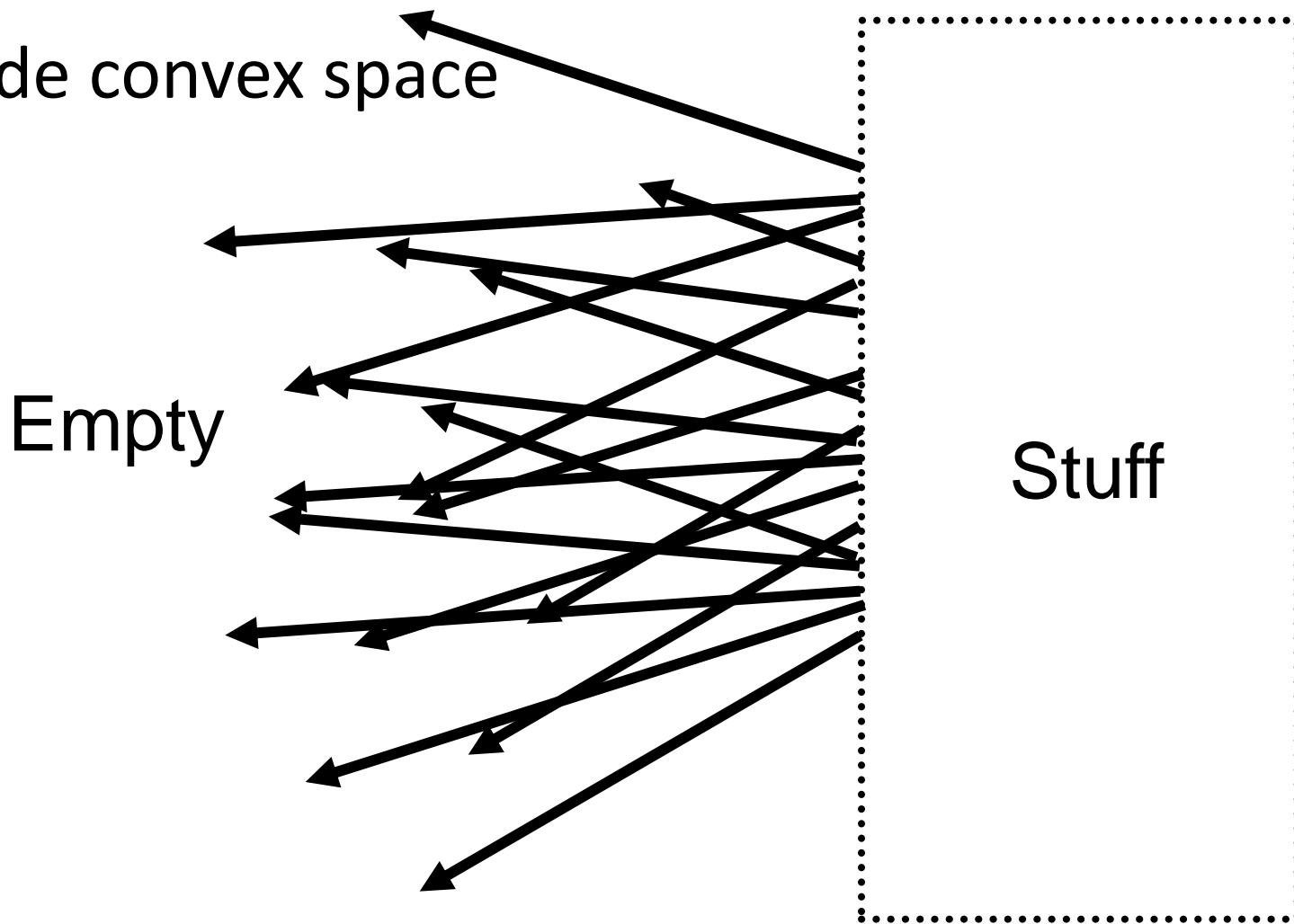






# Lumigraph / Lightfield

- Outside convex space

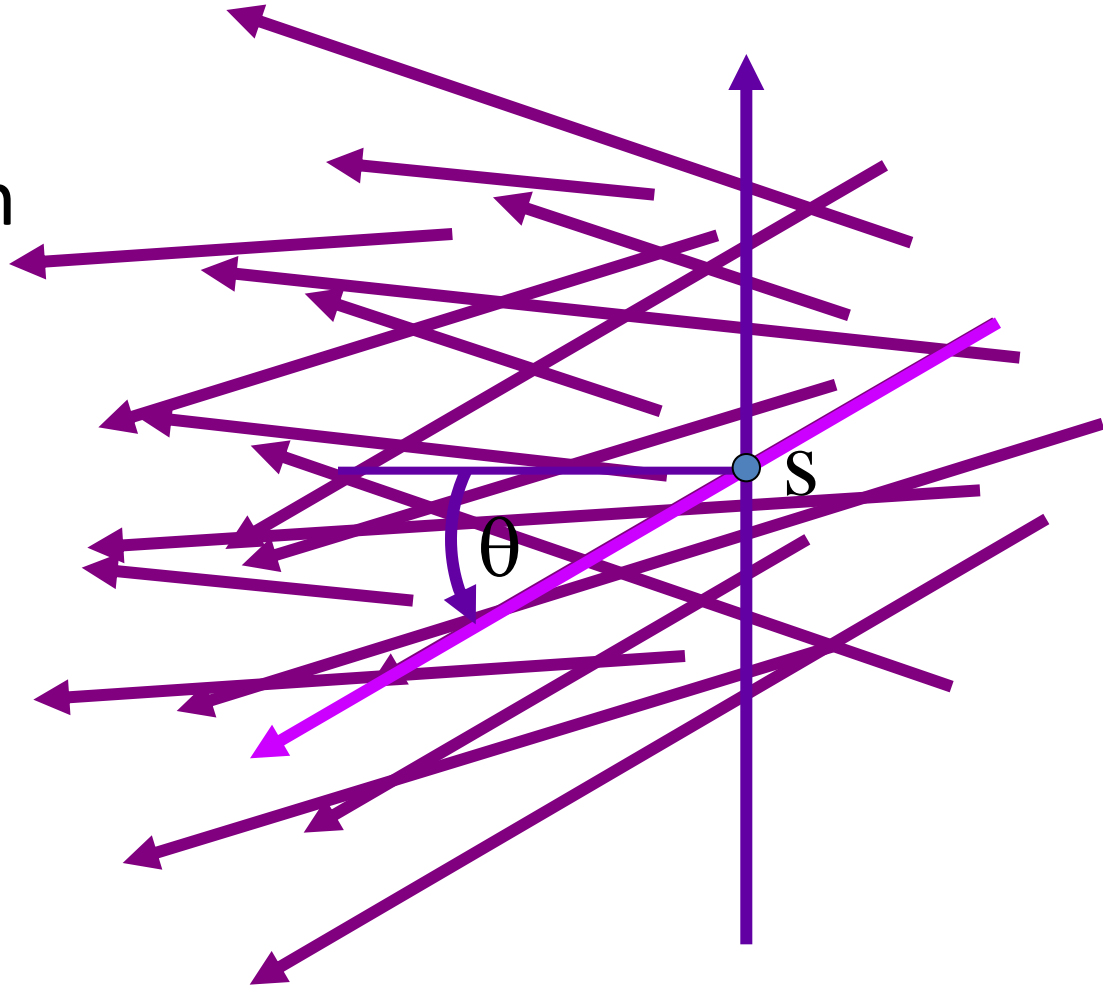


- 4D

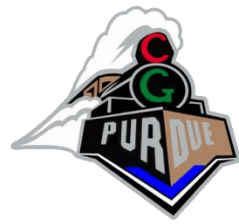


# Lumigraph / Lightfield

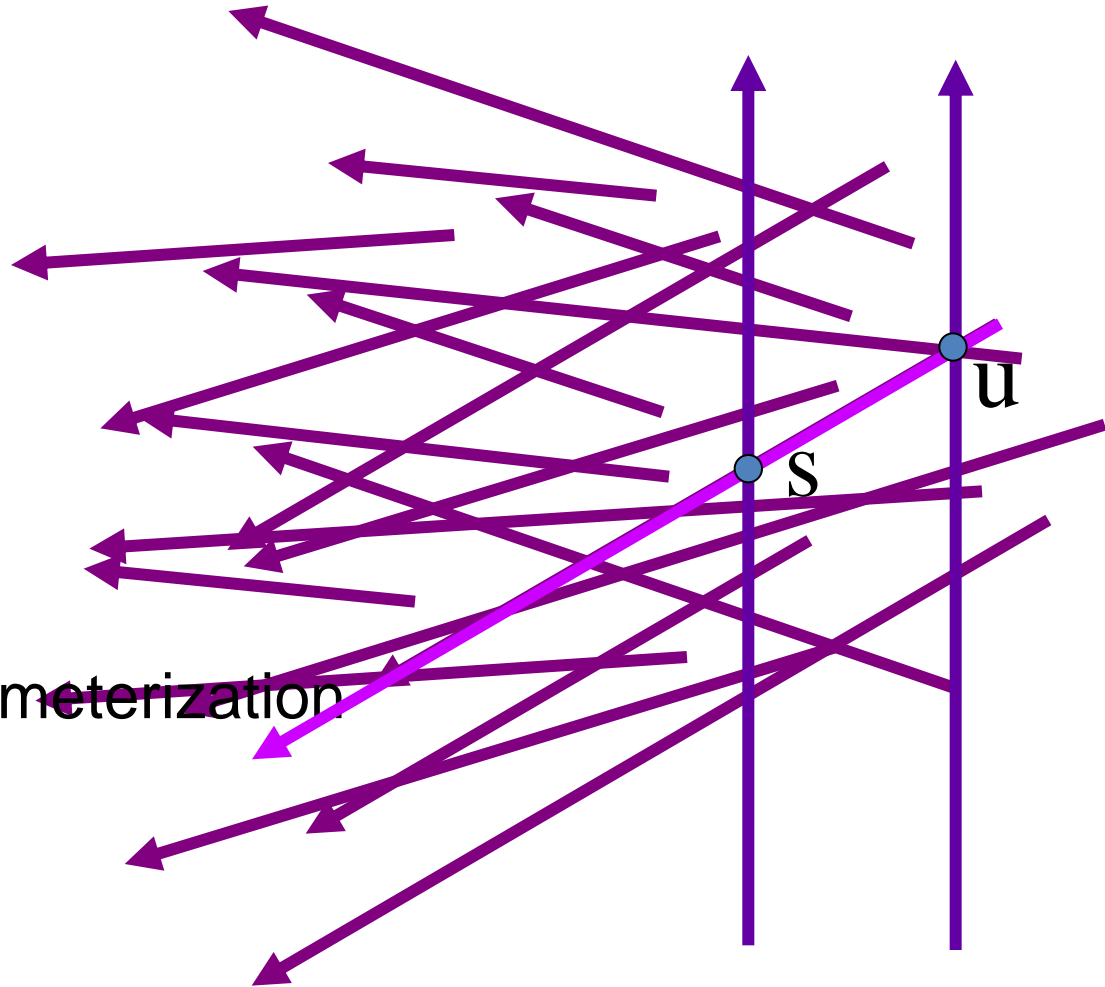
- 2D position
- 2D direction



# Lumigraph / Lightfield



- 2D position
- 2D position

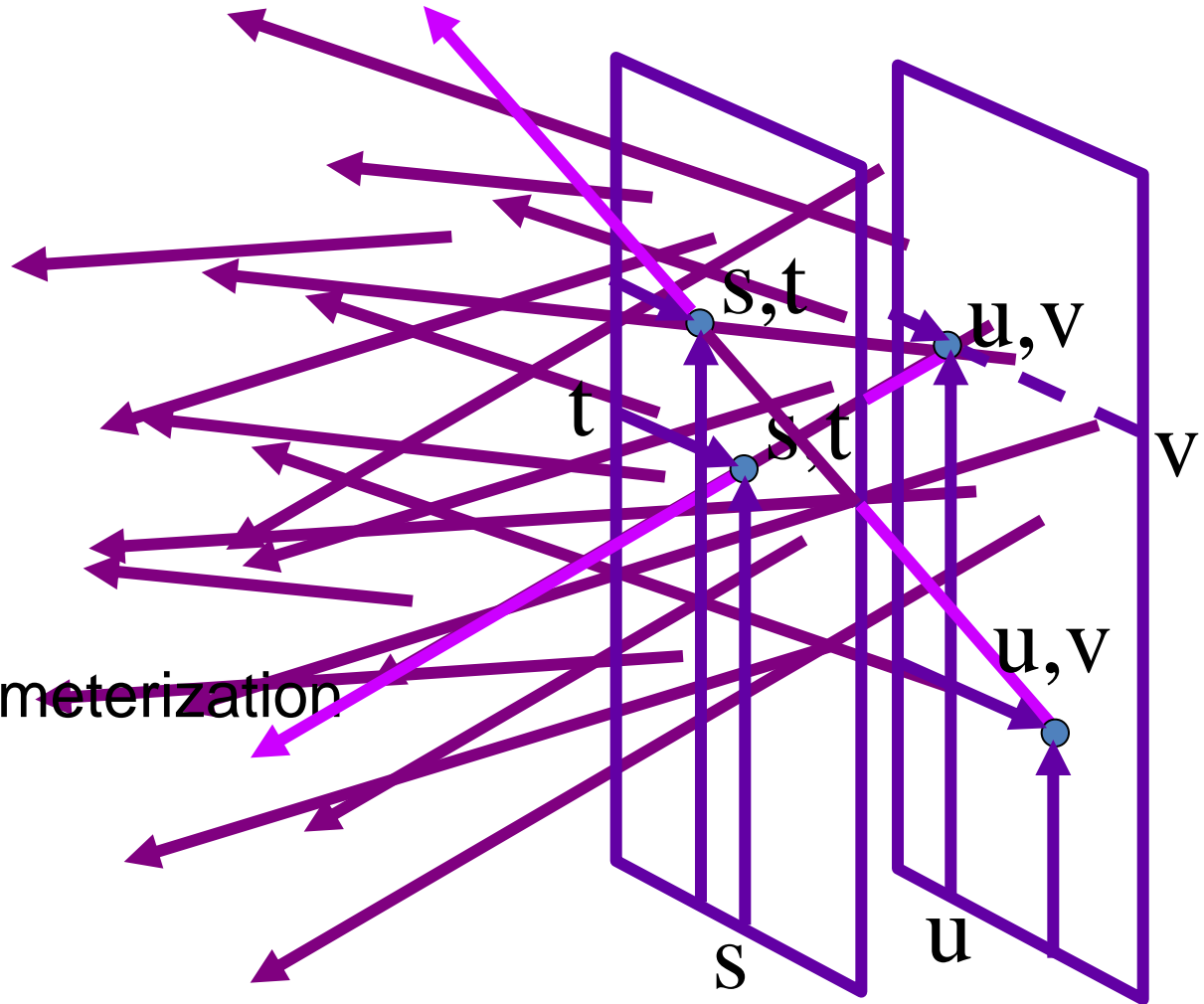


- 2 plane parameterization

# Lumigraph / Lightfield



- 2D position
- 2D position

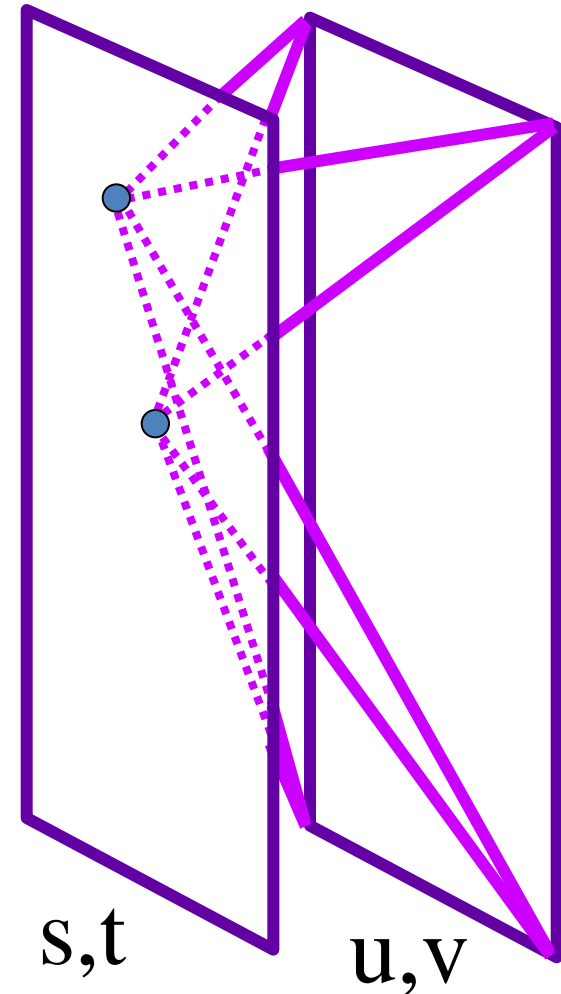


- 2 plane parameterization

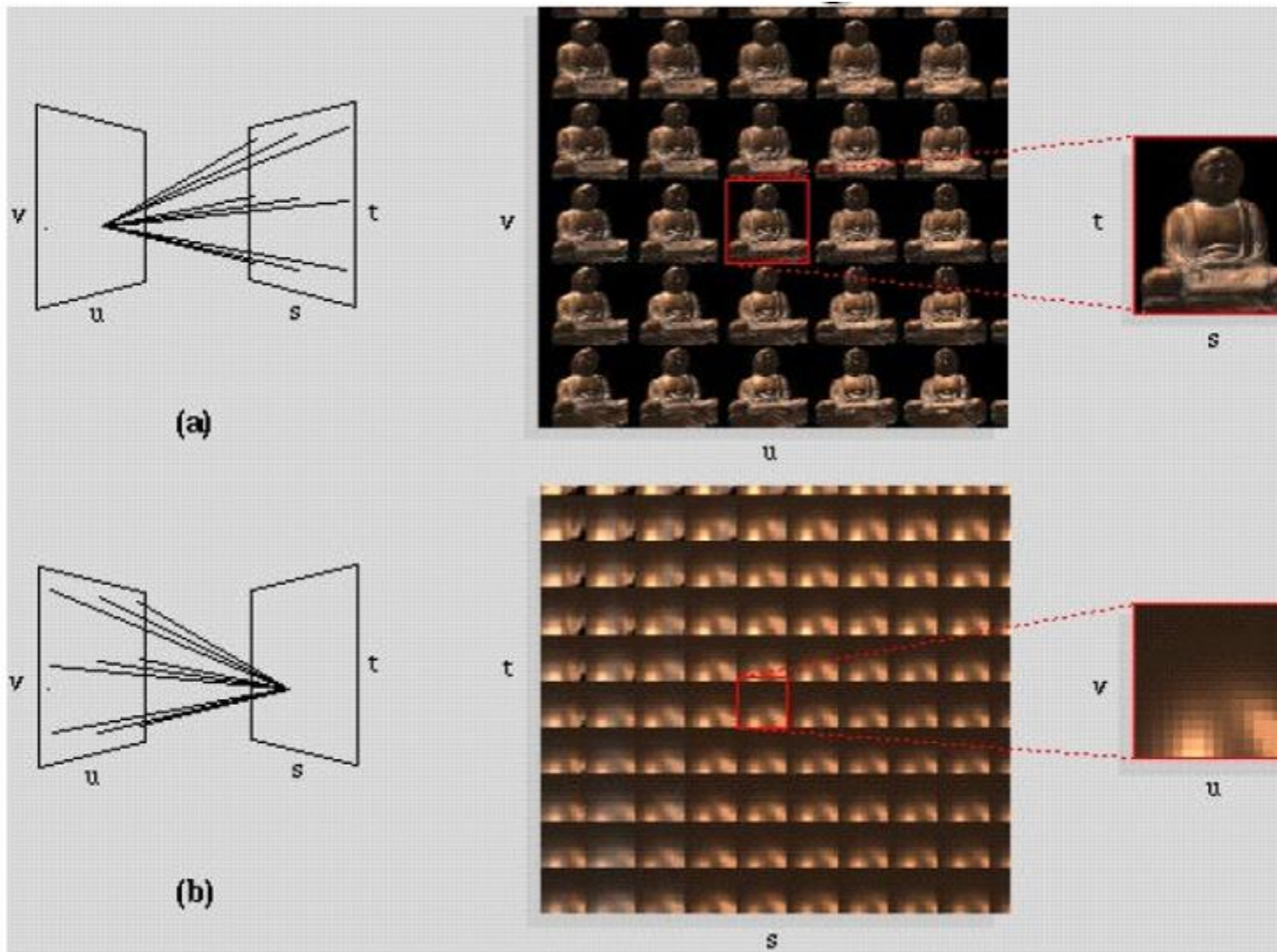
# Lumigraph / Lightfield



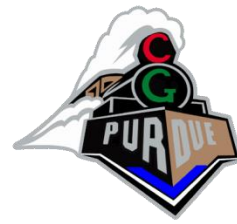
- Hold  $s, t$  constant
- Let  $u, v$  vary
- An image



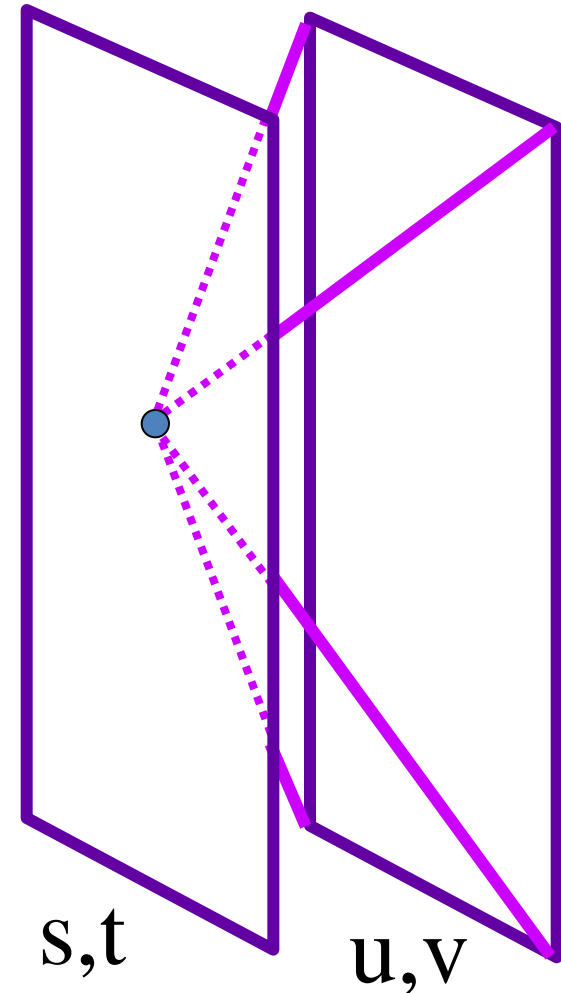
# Lumigraph / Lightfield



# Lightfield - Capture



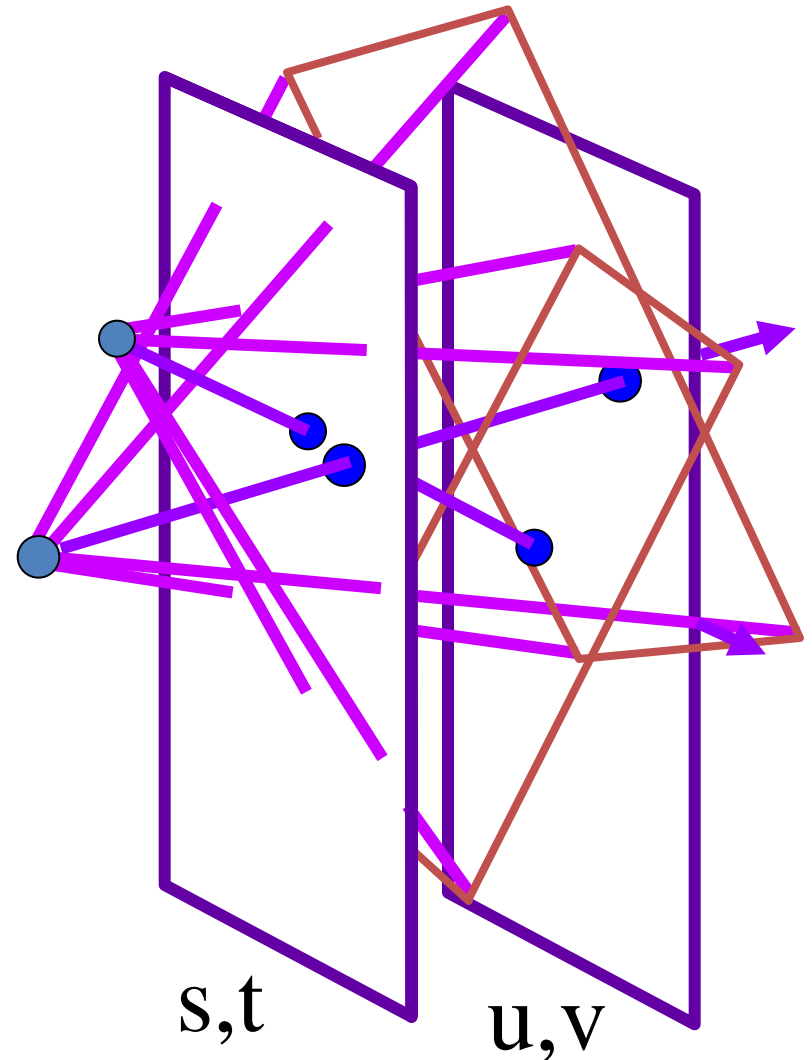
- Idea 1
  - Move camera carefully over  $s, t$  plane
  - Gantry
    - = Lightfield paper



# Lumigraph - Capture



- Idea 2
  - Move camera anywhere
  - Rebinning
    - = Lumigraph paper



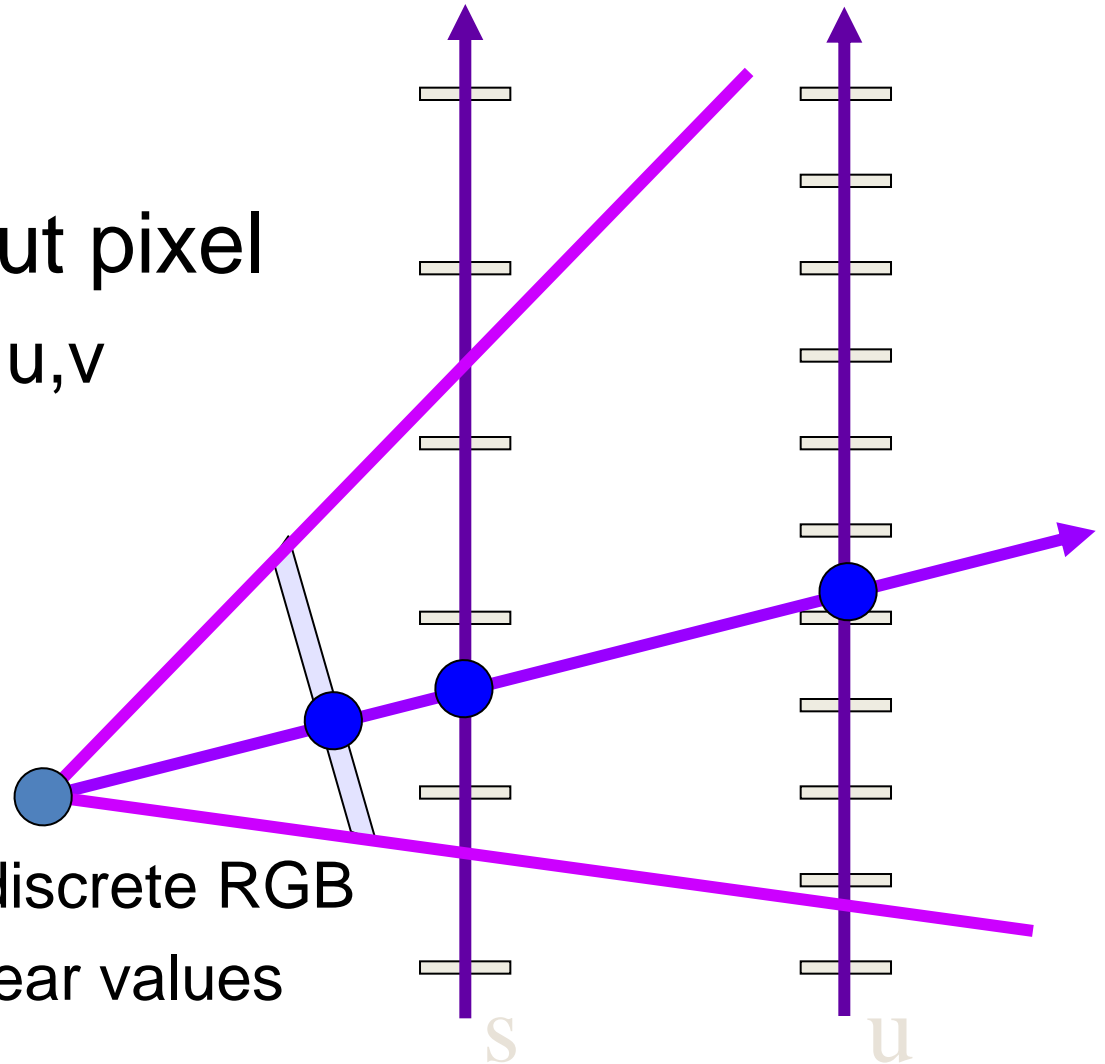


# Rendering



- For each output pixel
  - determine  $s, t, u, v$

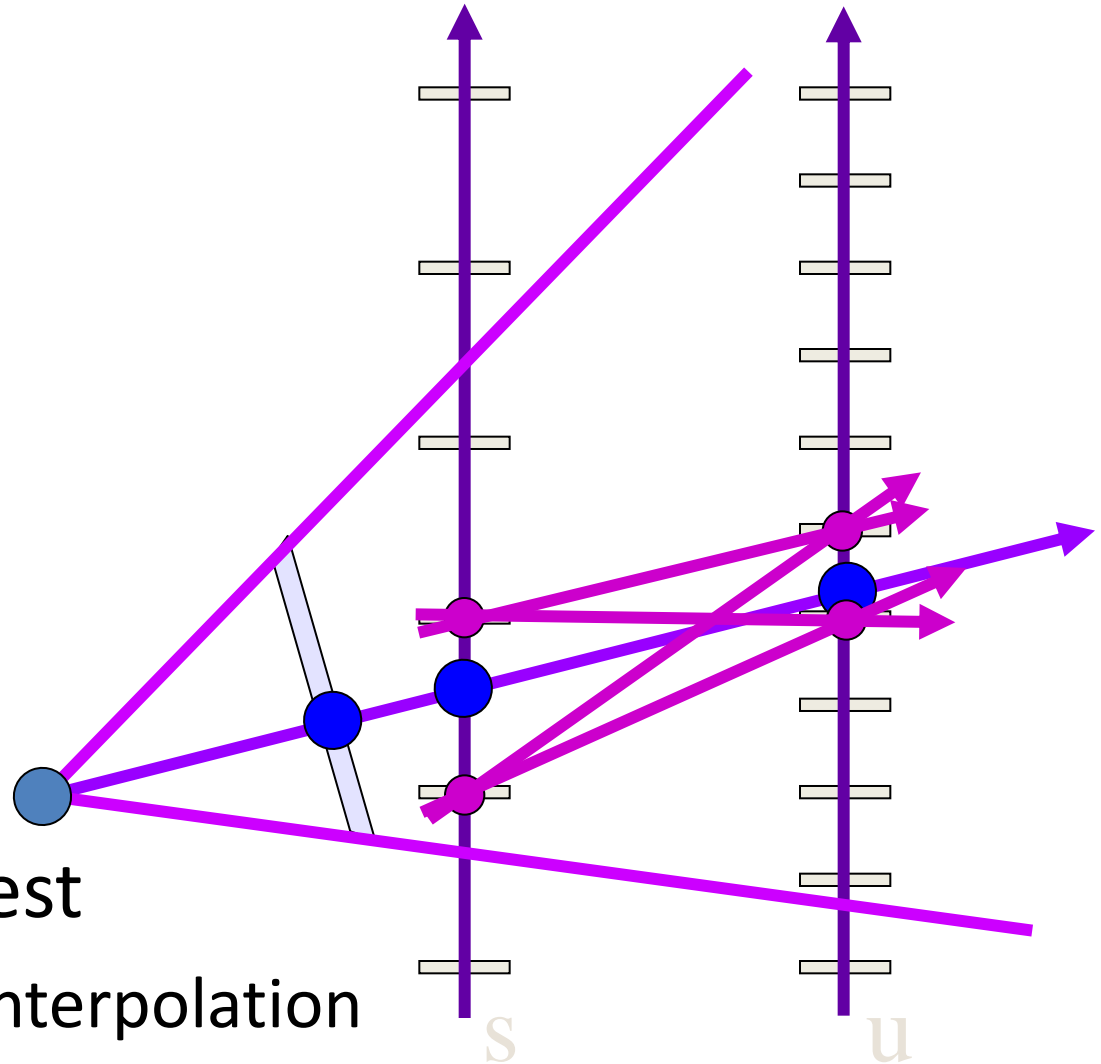
- either
  - use closest discrete RGB
  - interpolate near values





# Rendering

- Nearest
  - closest  $s$
  - closest  $u$
  - draw it

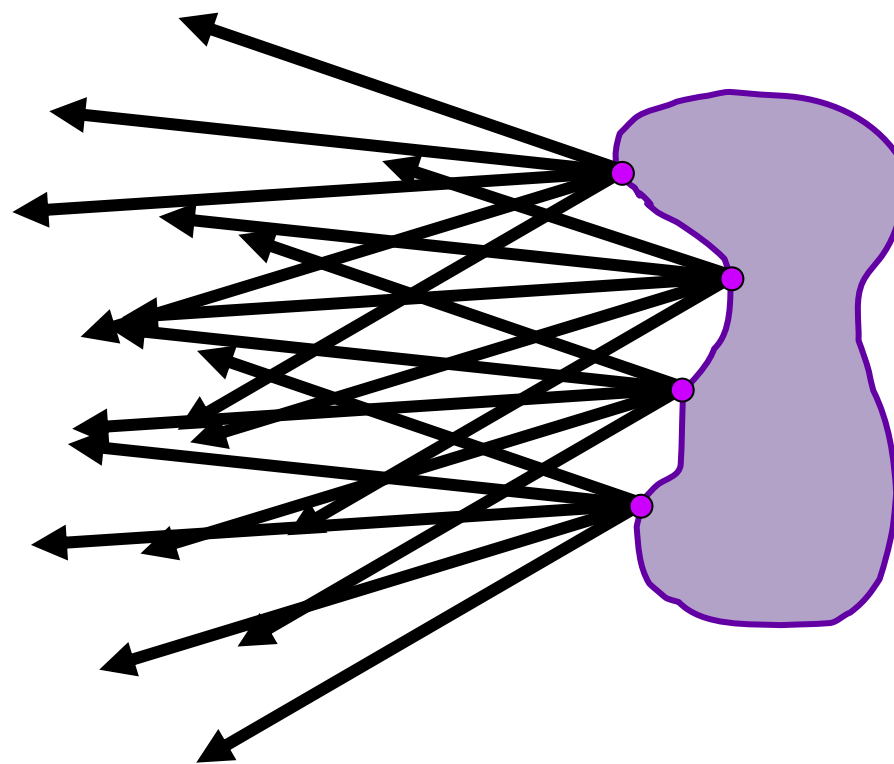


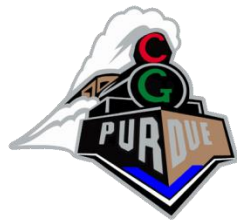
- Blend 16 nearest
  - quadrilinear interpolation



# 4D: Surface Lightfields

- Turn 4D parameterization around
- Leverage coherence





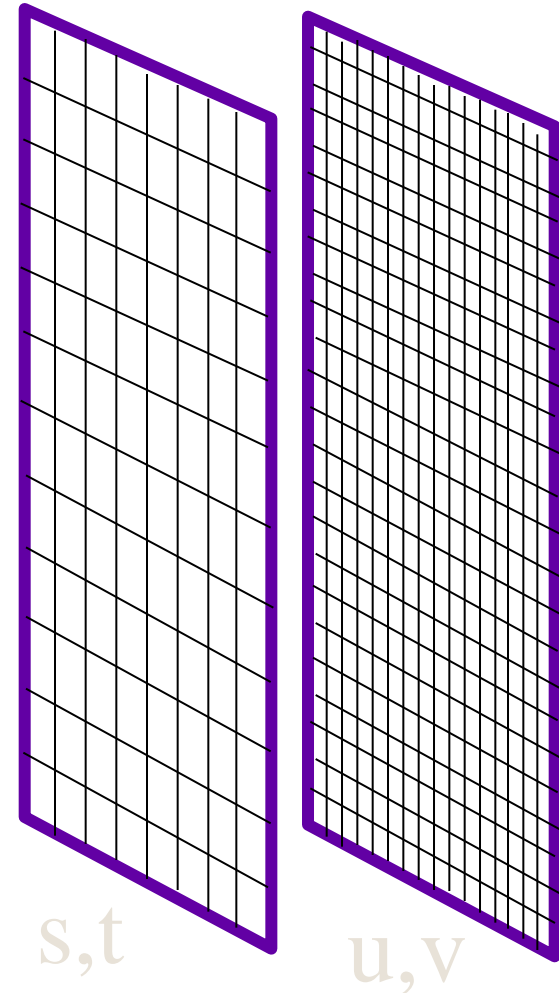
# 4D: Surface Lightfields



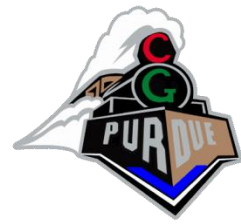
# (3D: Lumigraph/Lightfield)



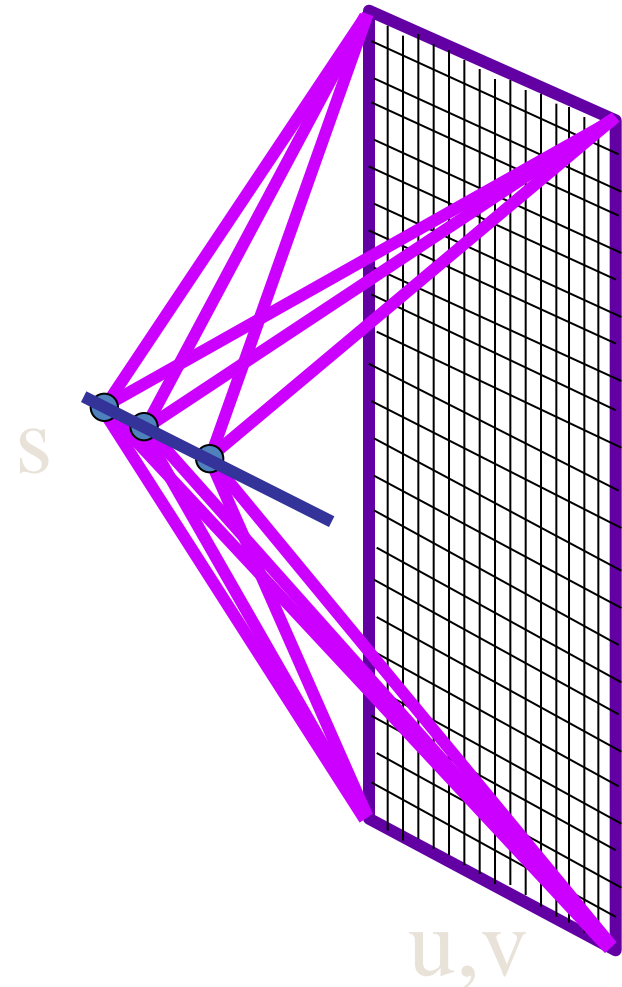
- One row of  $s,t$  plane  
– i.e., hold  $t$  constant



# (3D: Lumigraph/Lightfield)



- One row of  $s,t$  plane
  - i.e., hold  $t$  constant
  - thus  $s,u,v$
  - a “row of images”





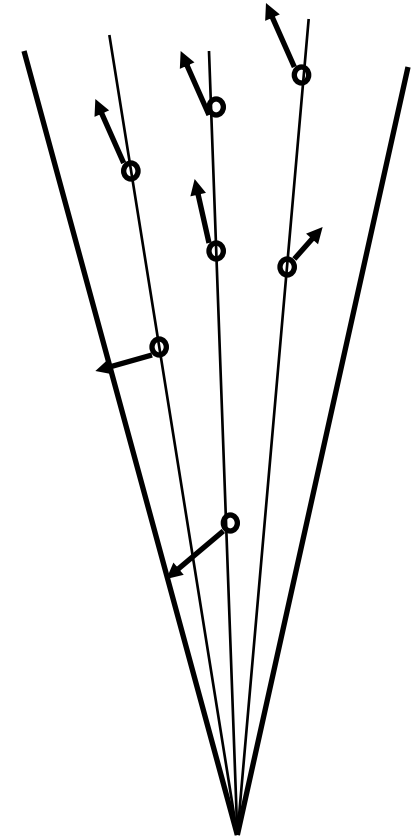
$P(x,t)$

by David Dewey

# (3-5D: Layered Depth Images)



- Idea:
  - Handle disocclusion
  - Store invisible geometry in depth images
- Data structure:
  - Per pixel list of depth samples
  - Per depth sample:
    - RGBA
    - Z
    - Encoded: Normal direction, distance
  - Pack into cache lines

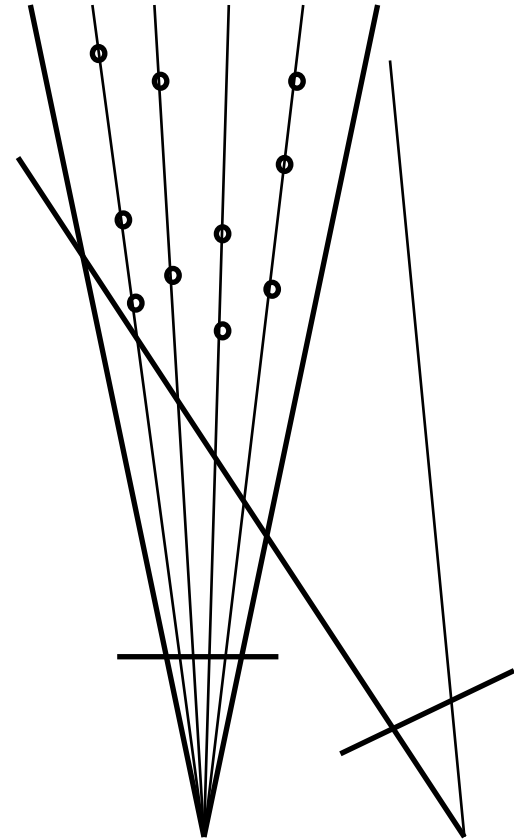




# (3-5D: Layered Depth Images)



- Computation:
  - Incremental warping computation
  - Implicit ordering information
    - Process in up to four quadrant
  - Splat size computation
    - Table lookup
    - Fixed splat templates
  - Clipping of LDIs



# (3-5D: Layered Depth Images)



# (3-5D: Layered Depth Images)



Plate 2. The first two layers of the LDI. Pixels without values are shown in red.

Plate 3. Savings due to recursive clipping of the LDI before warping.

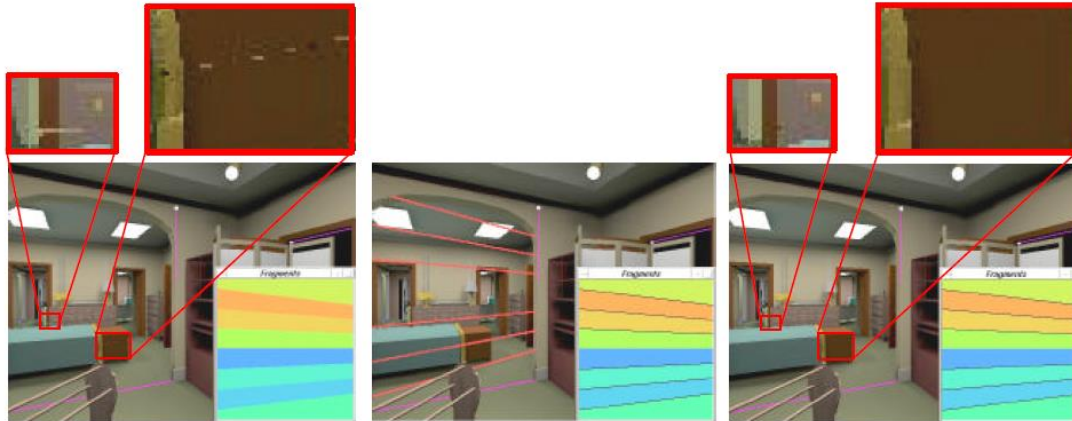
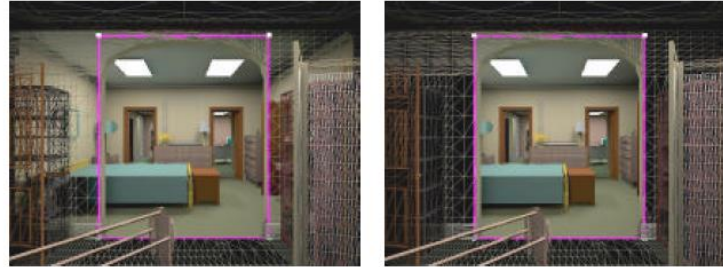


Plate 4. Images are rendered in parallel, one fragment per processor. a) Artifacts (highlighted in red) appear at the borders between fragments because of incorrect occlusion compatible traversal. b) Buffer zones between fragments are rendered during a second pass. c) Image rendered using two-pass traversal does not exhibit the artifacts of image (a).



## (3-5D: LDI Tree)

- “LDI Tree: A sampling-rate Preserving Hierarchical Representation for Image-based Rendering” by Chang et al.





# (~5D: LDC Cube)

- 3 orthogonal LDIs (or LDI Trees)
  - Part of “Surfels” paper

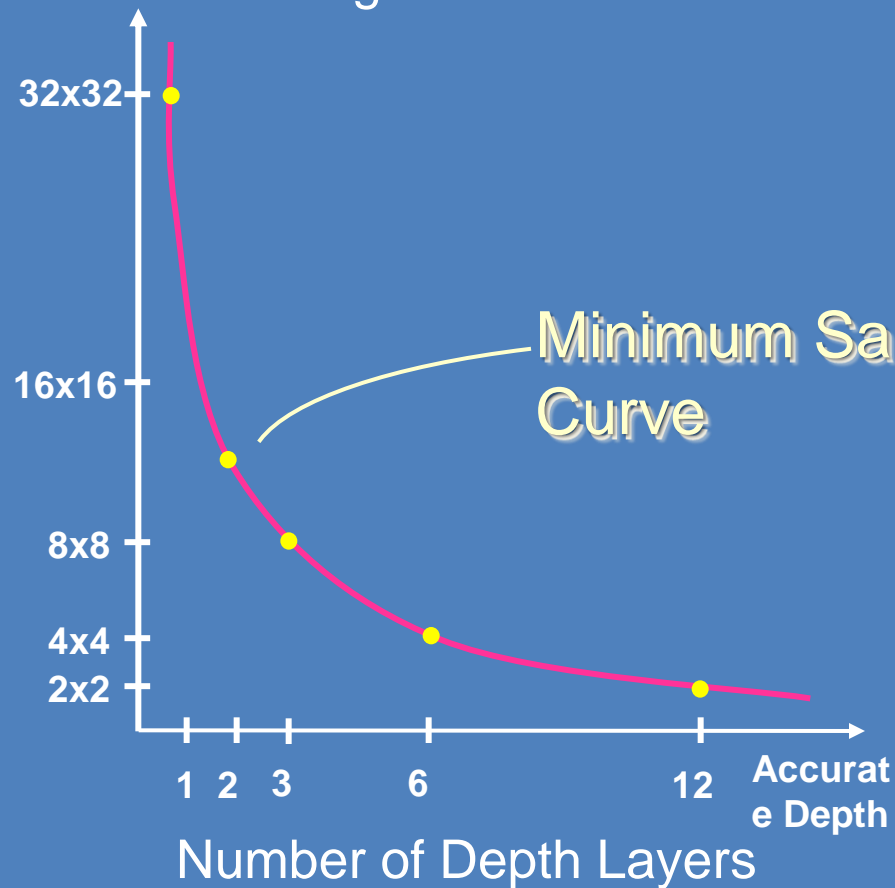




# Minimum Sampling Curve

Number of Images

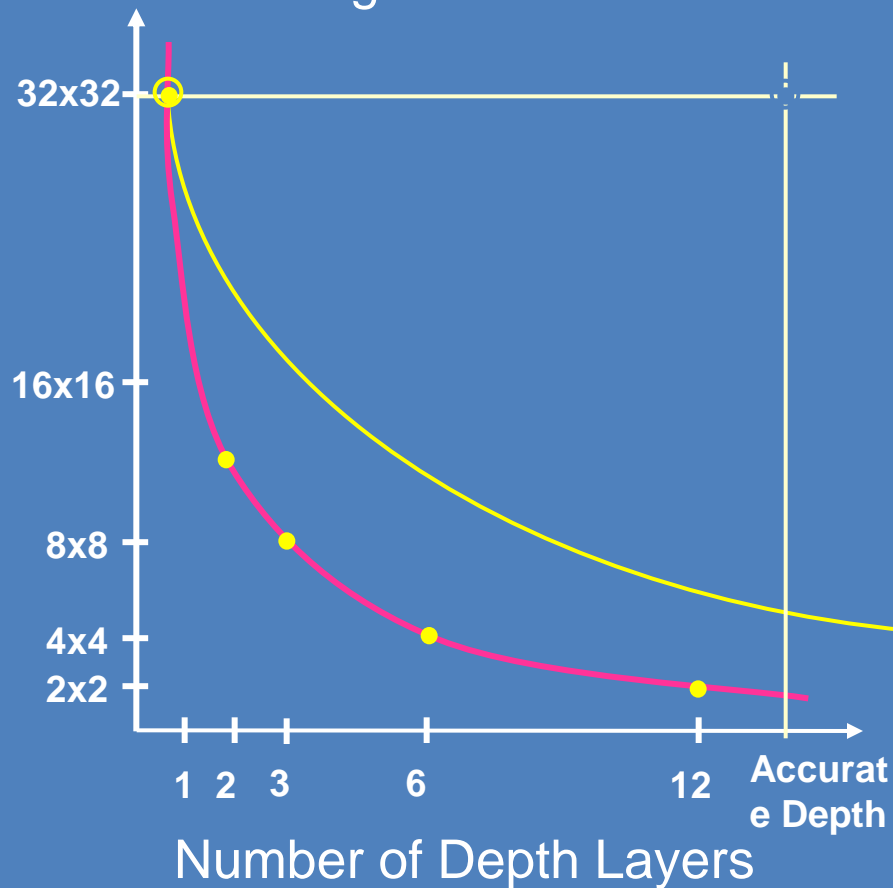
Joint Image  
and  
Geometry  
Space





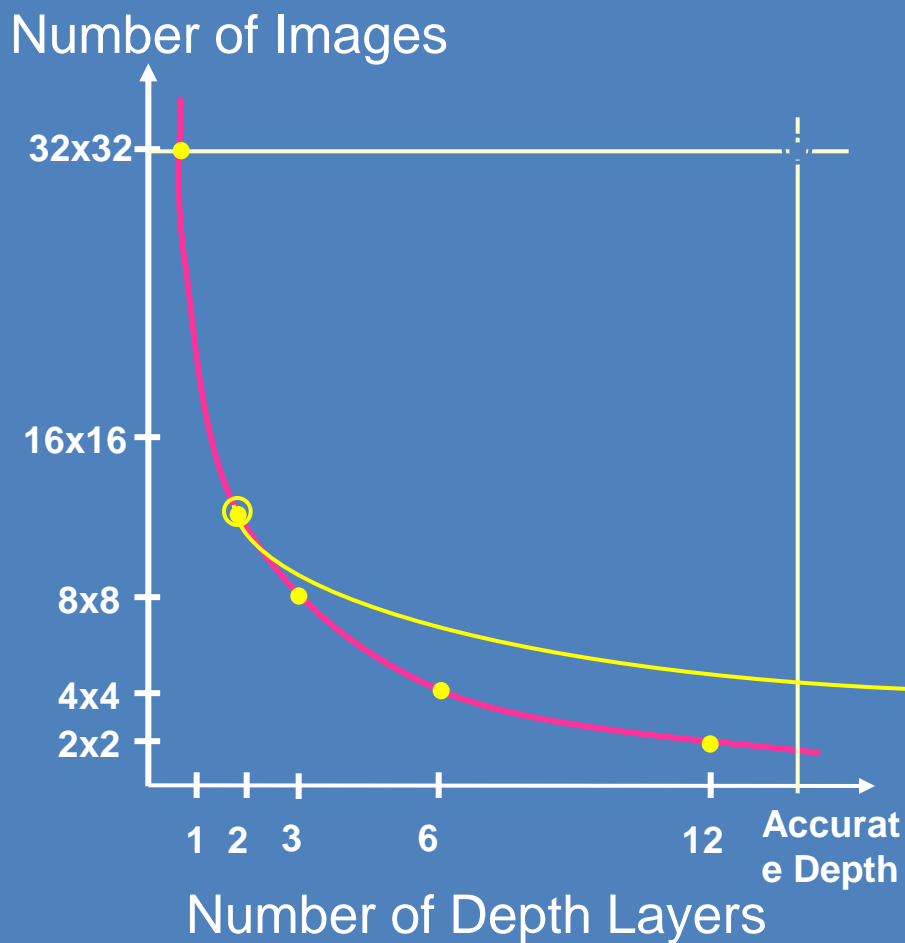
# Minimum Sampling Curve

Number of Images





# Minimum Sampling Curve

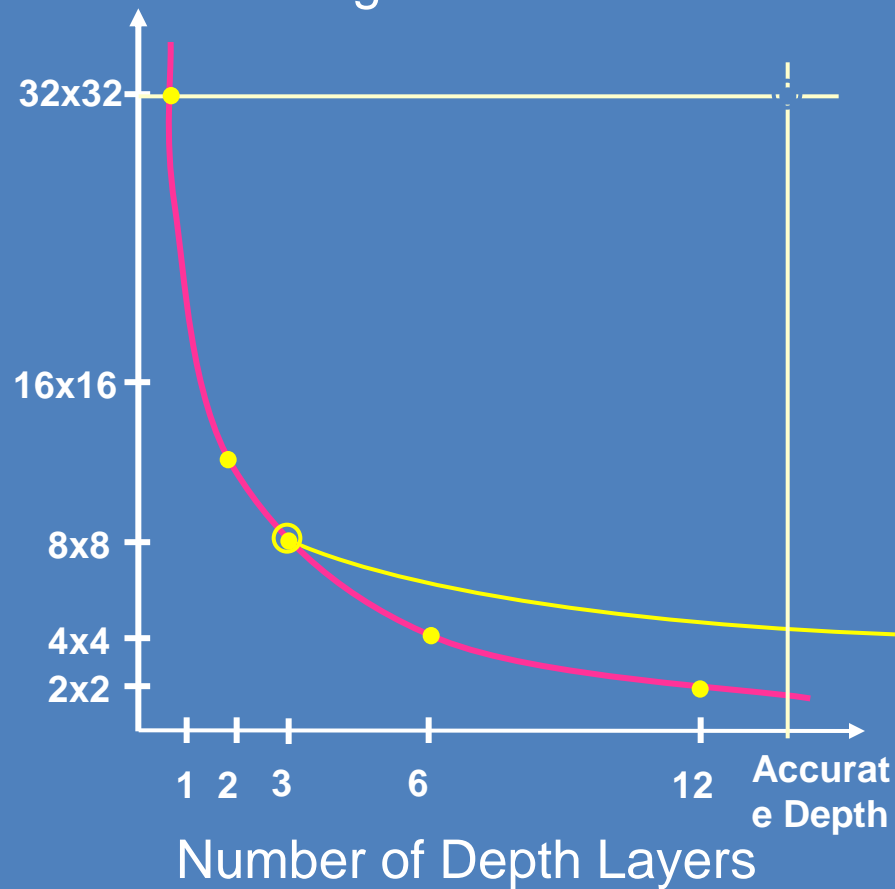






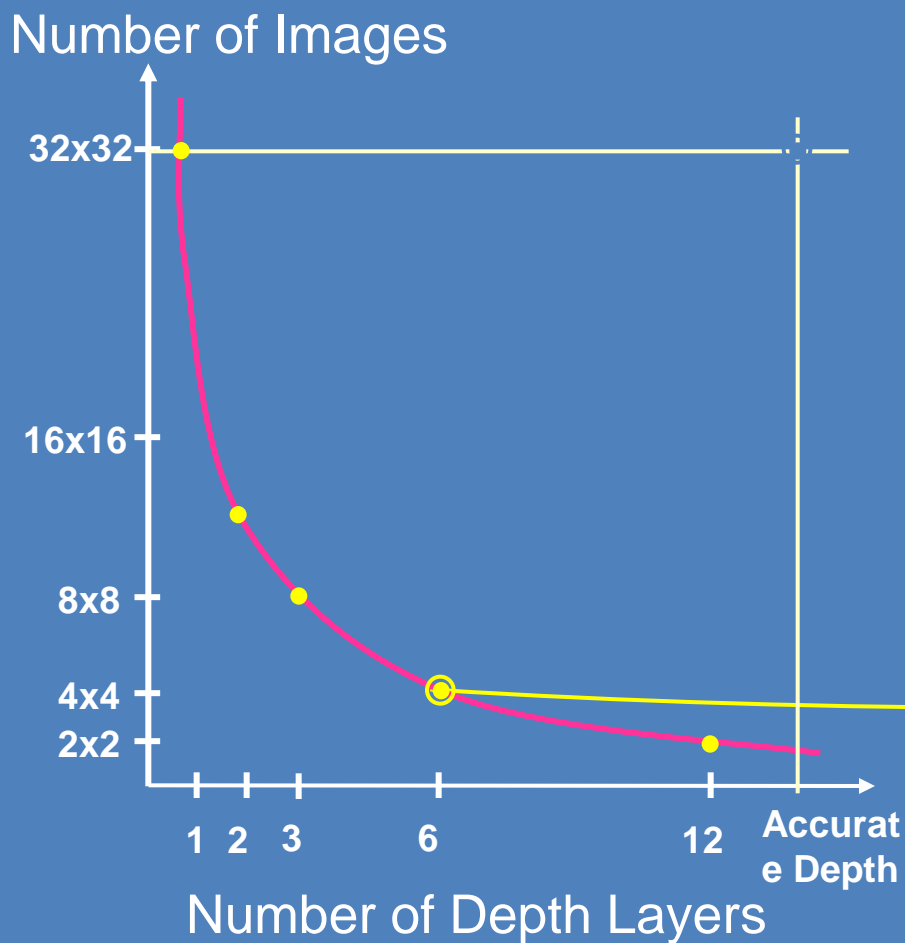
# Minimum Sampling Curve

Number of Images



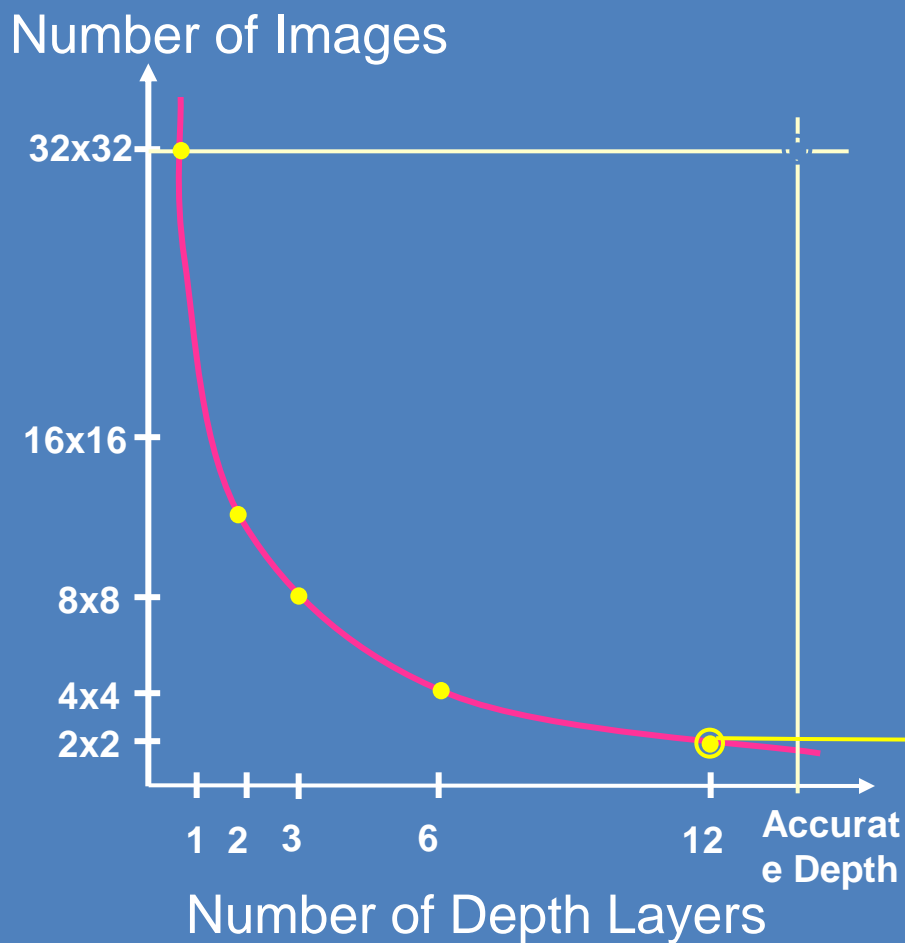


# Minimum Sampling Curve



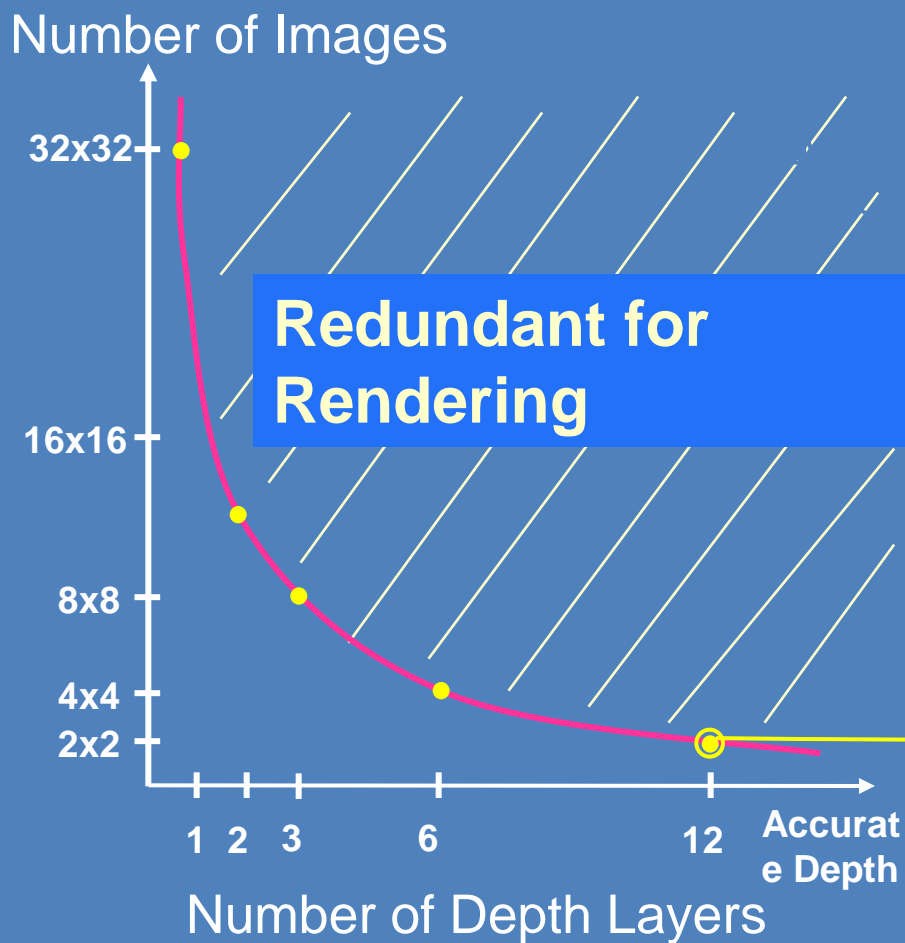


# Minimum Sampling Curve





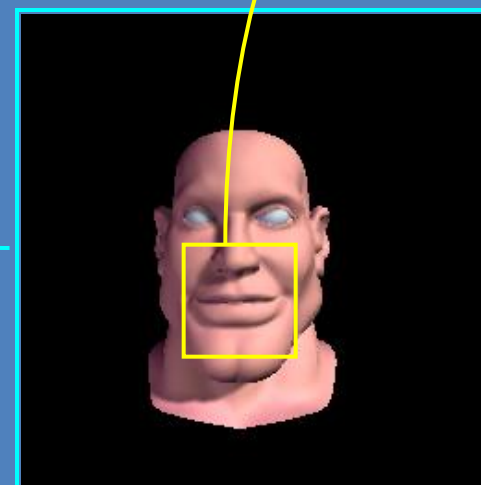
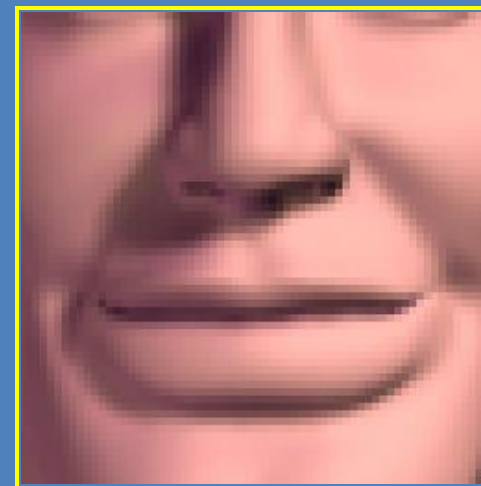
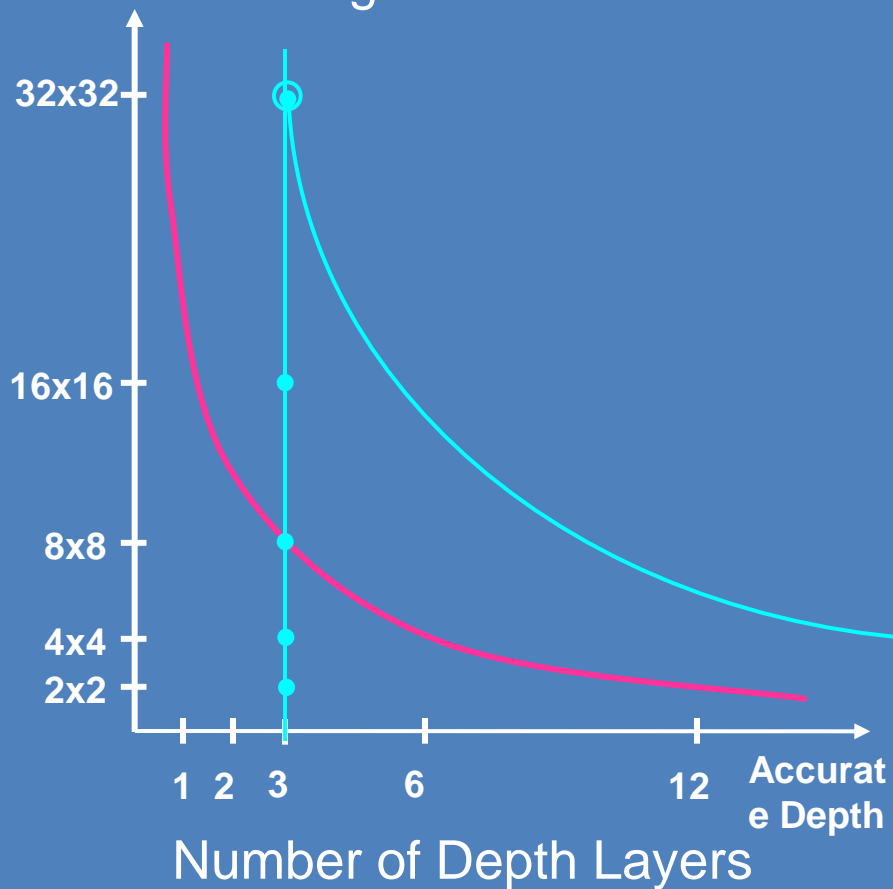
# Minimum Sampling Curve





# More Geometry: 3 Layers

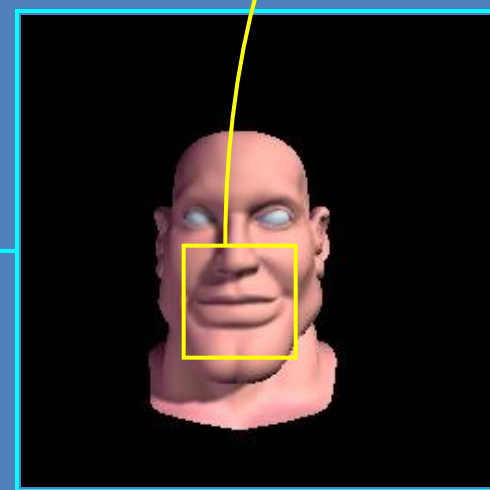
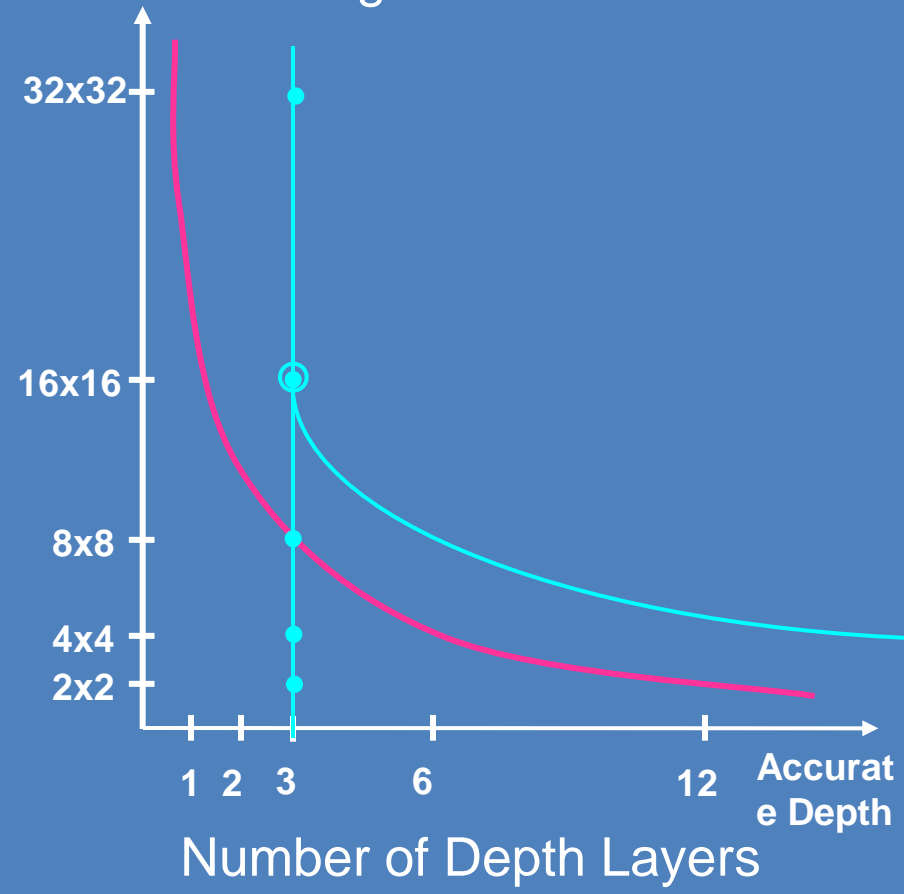
Number of Images





# 3 Layers

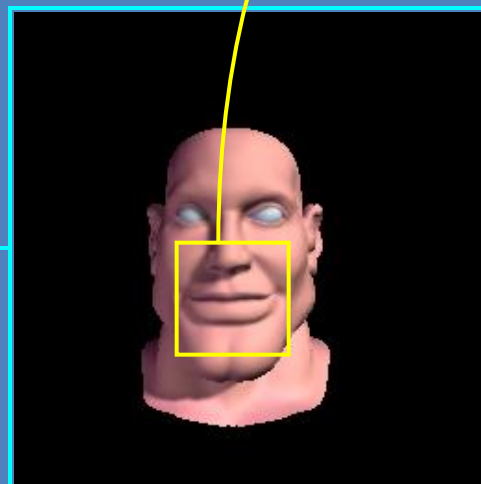
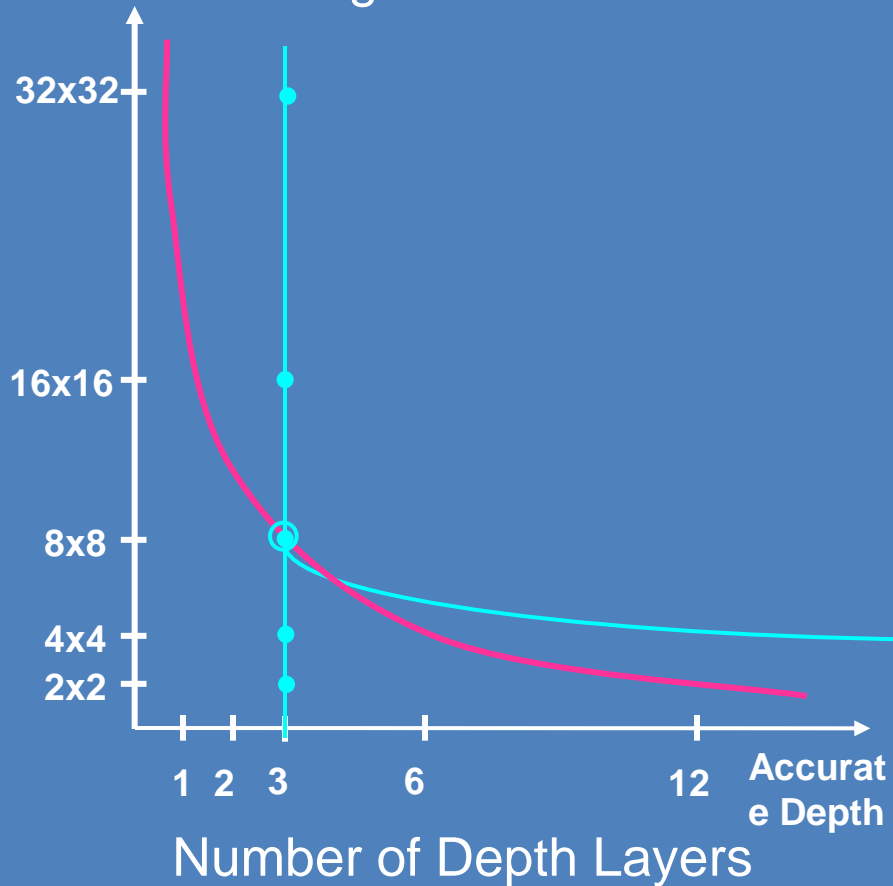
Number of Images





# 3 Layers

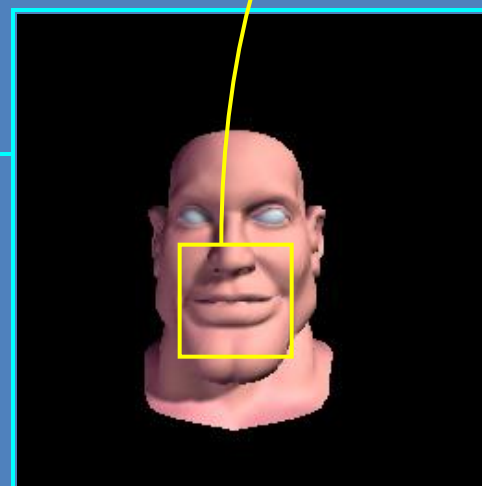
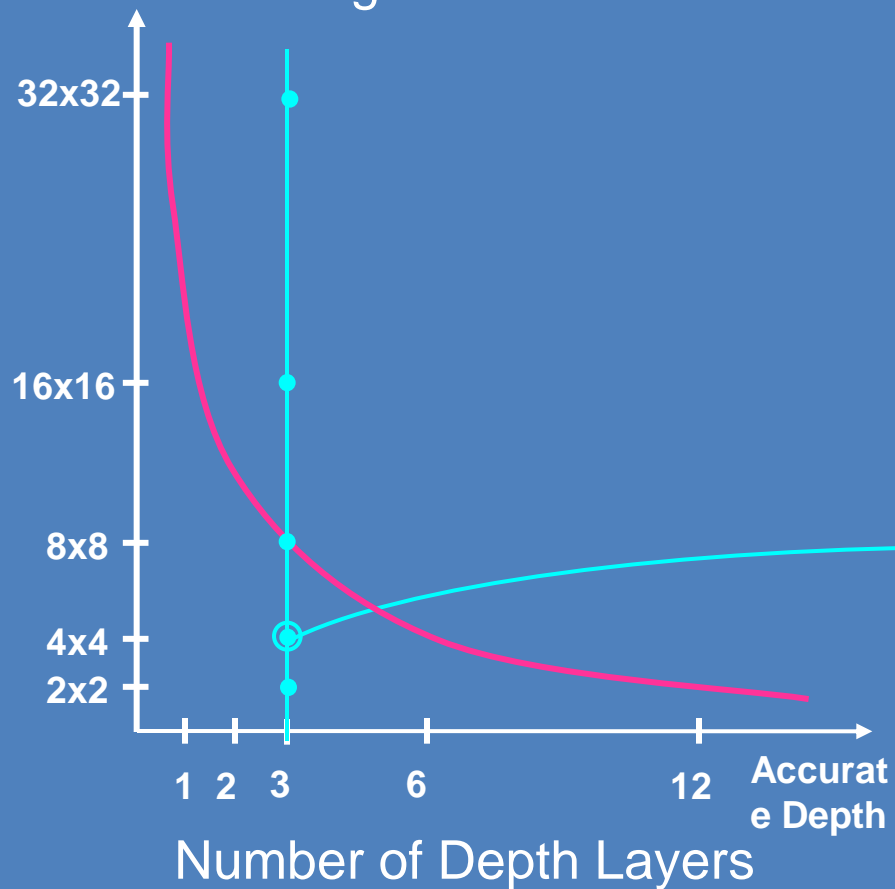
Number of Images





# 3 Layers

Number of Images

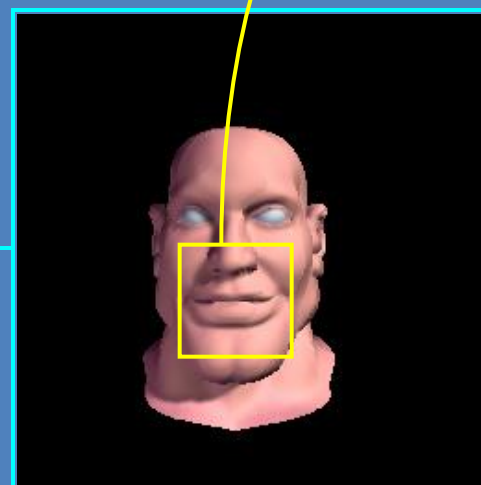
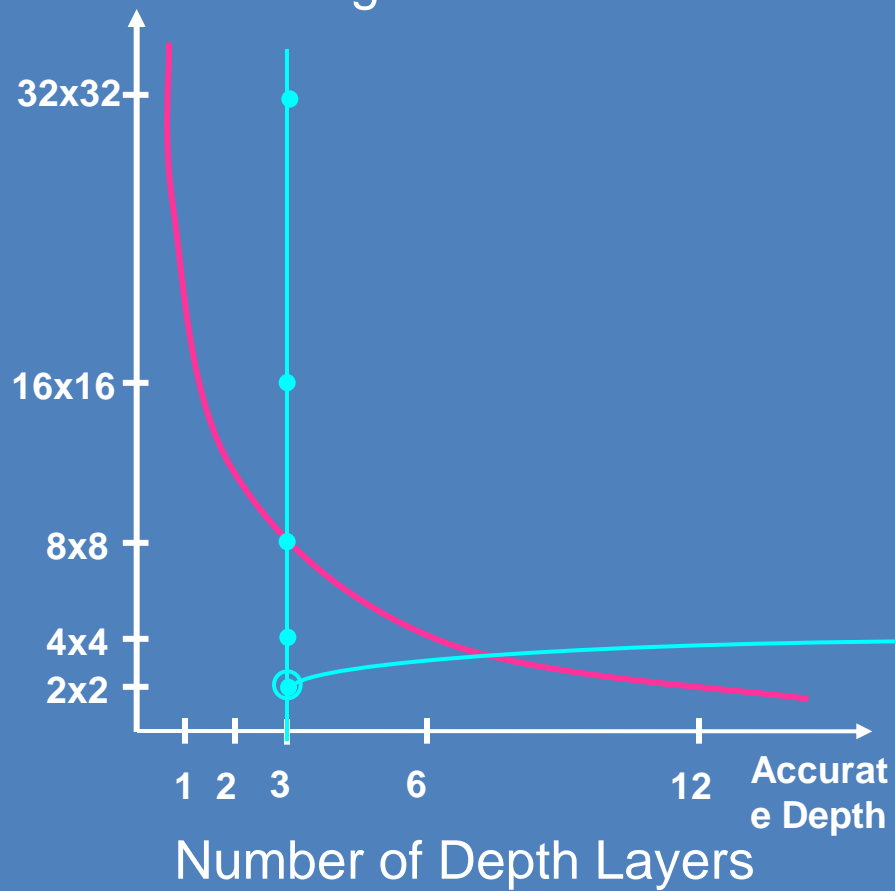






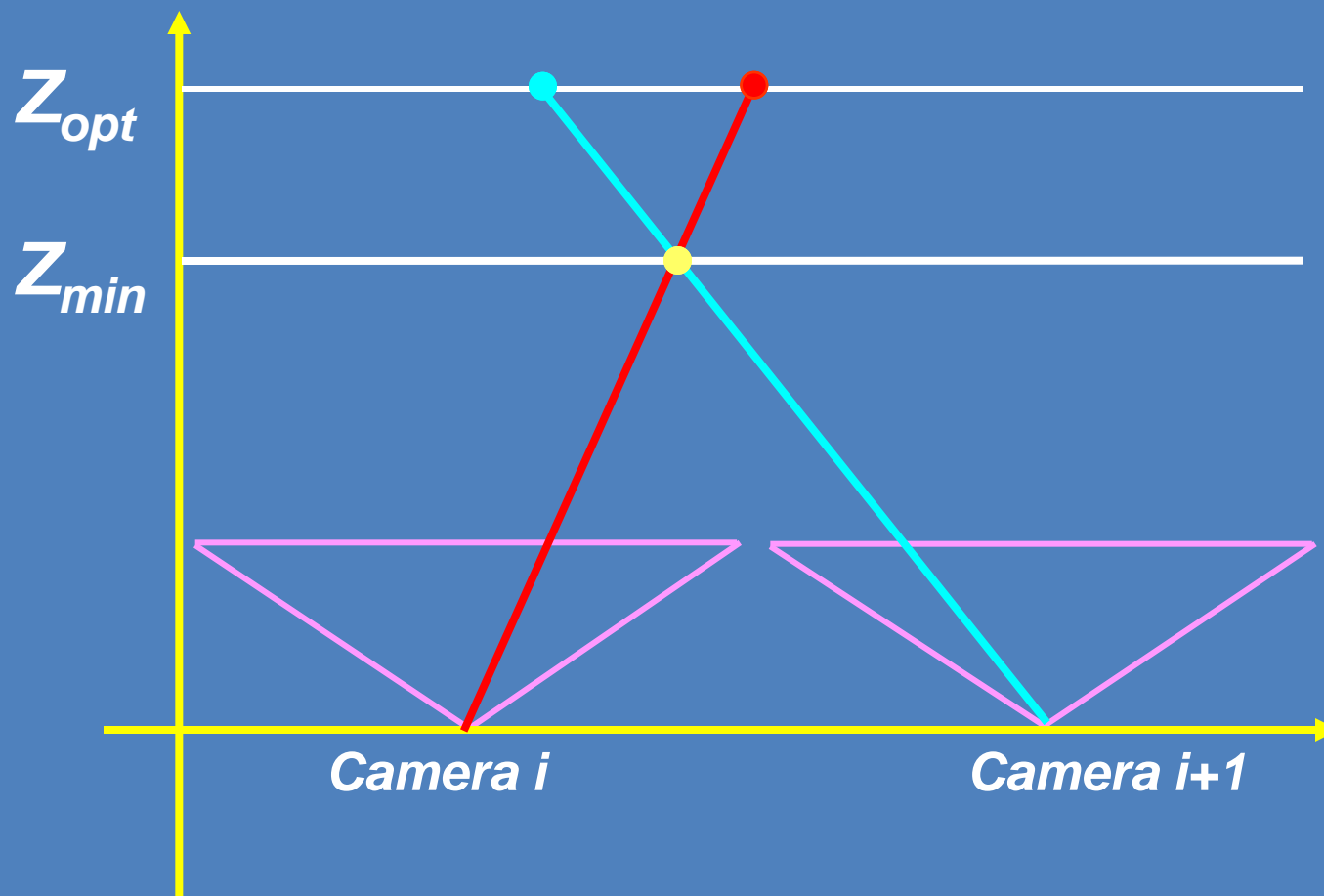
# 3 Layers

Number of Images



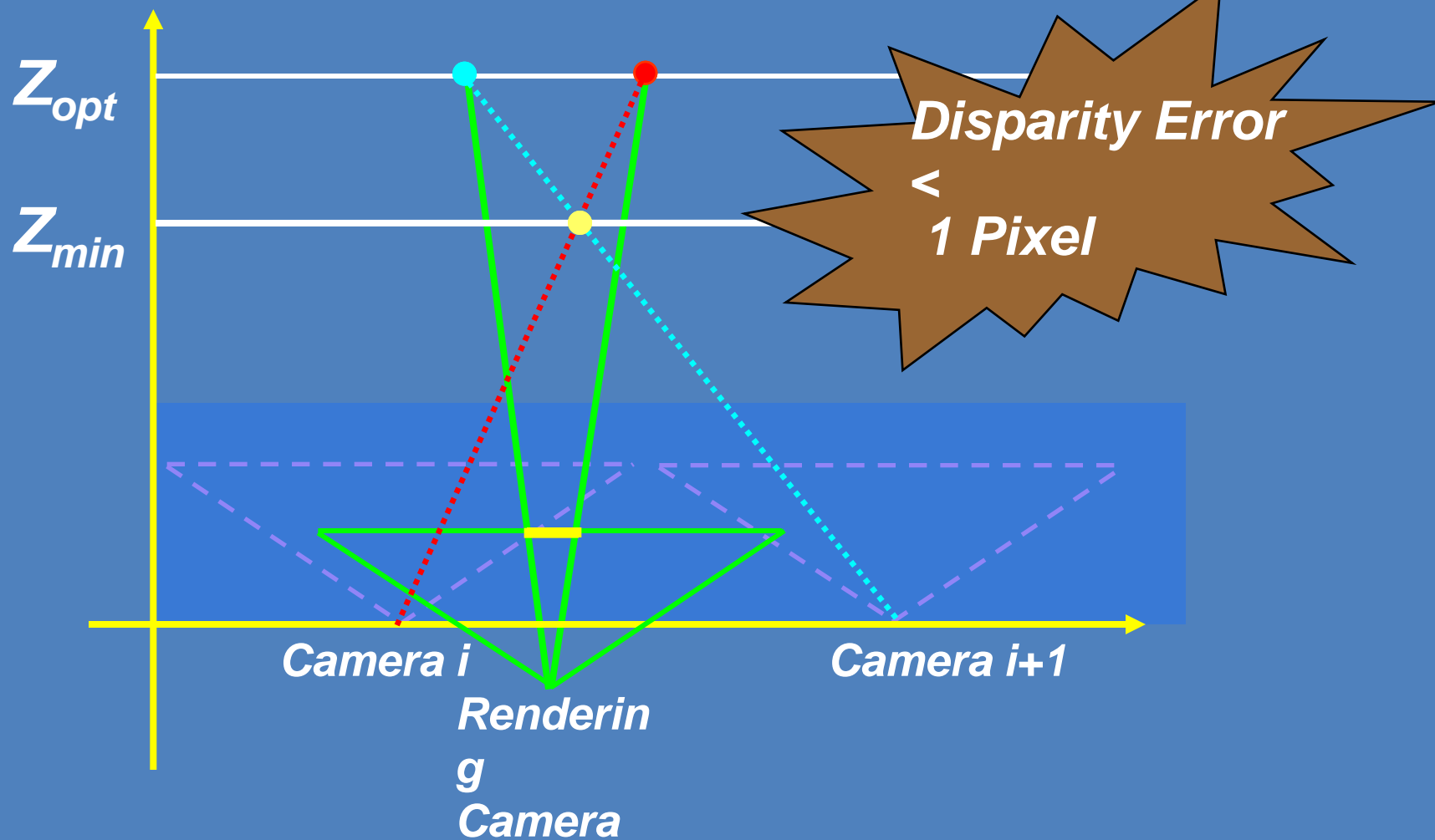


# A Geometrical Intuition



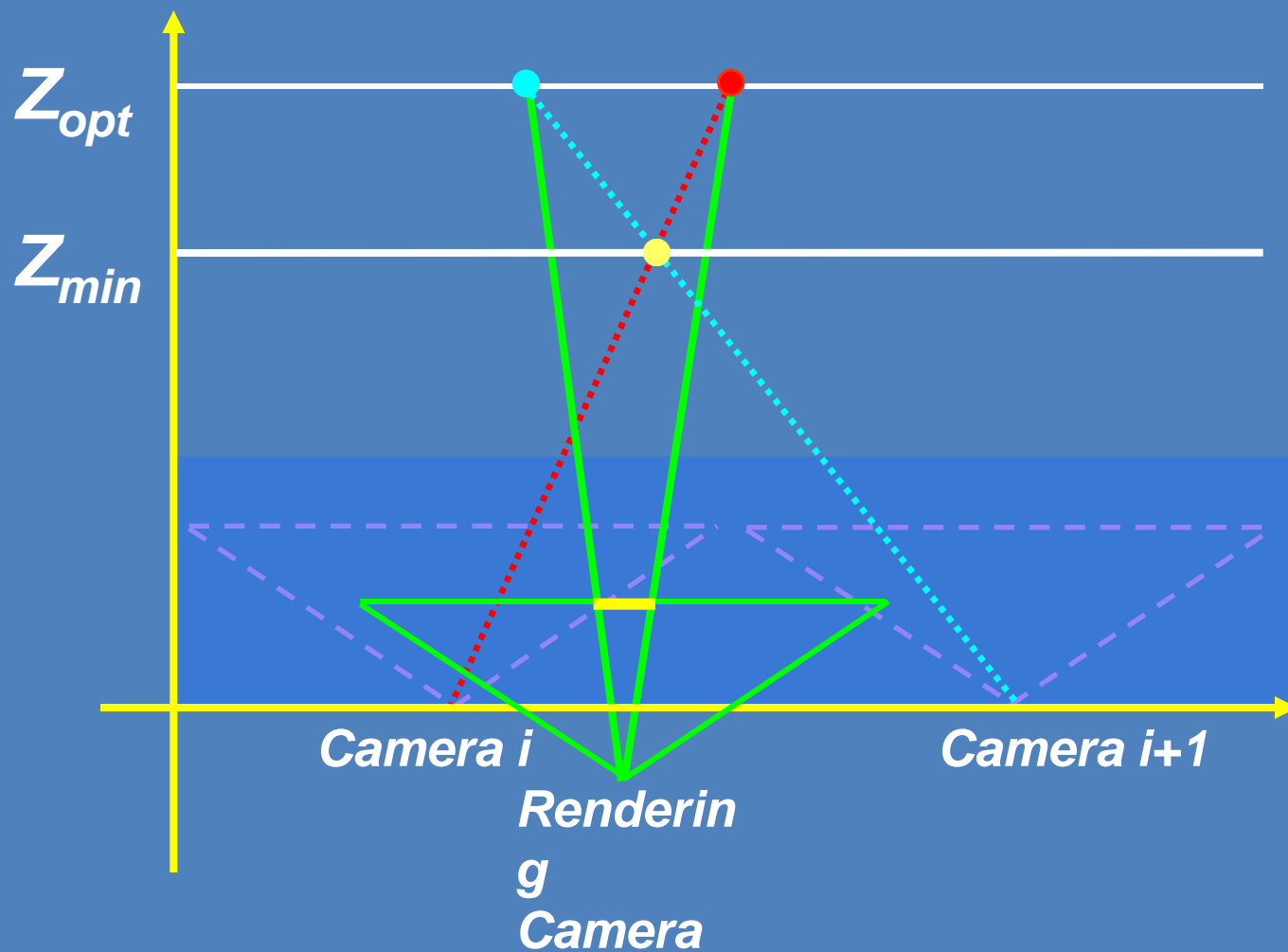


# A Geometrical Intuition



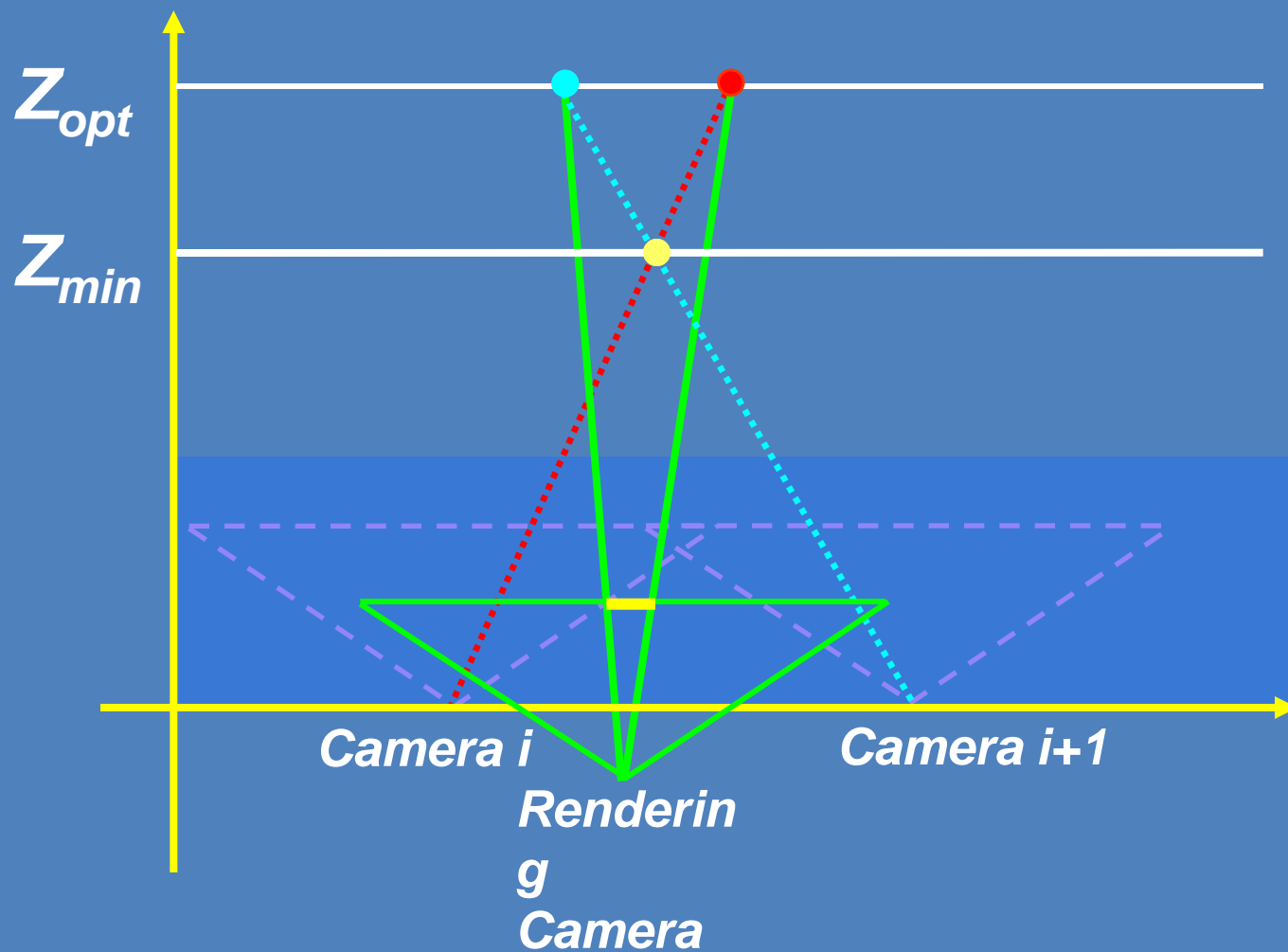


# A Geometrical Intuition



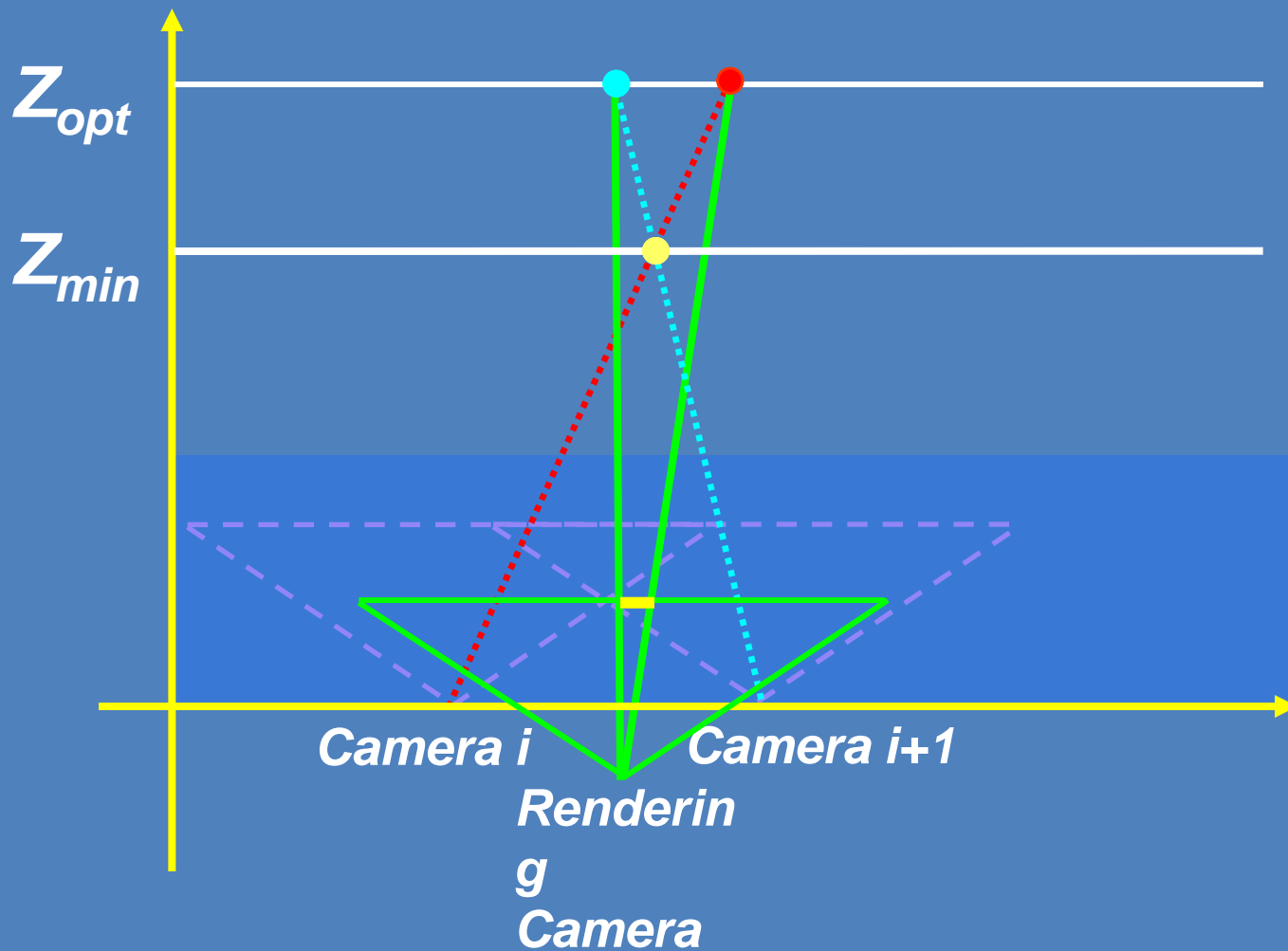


# A Geometrical Intuition



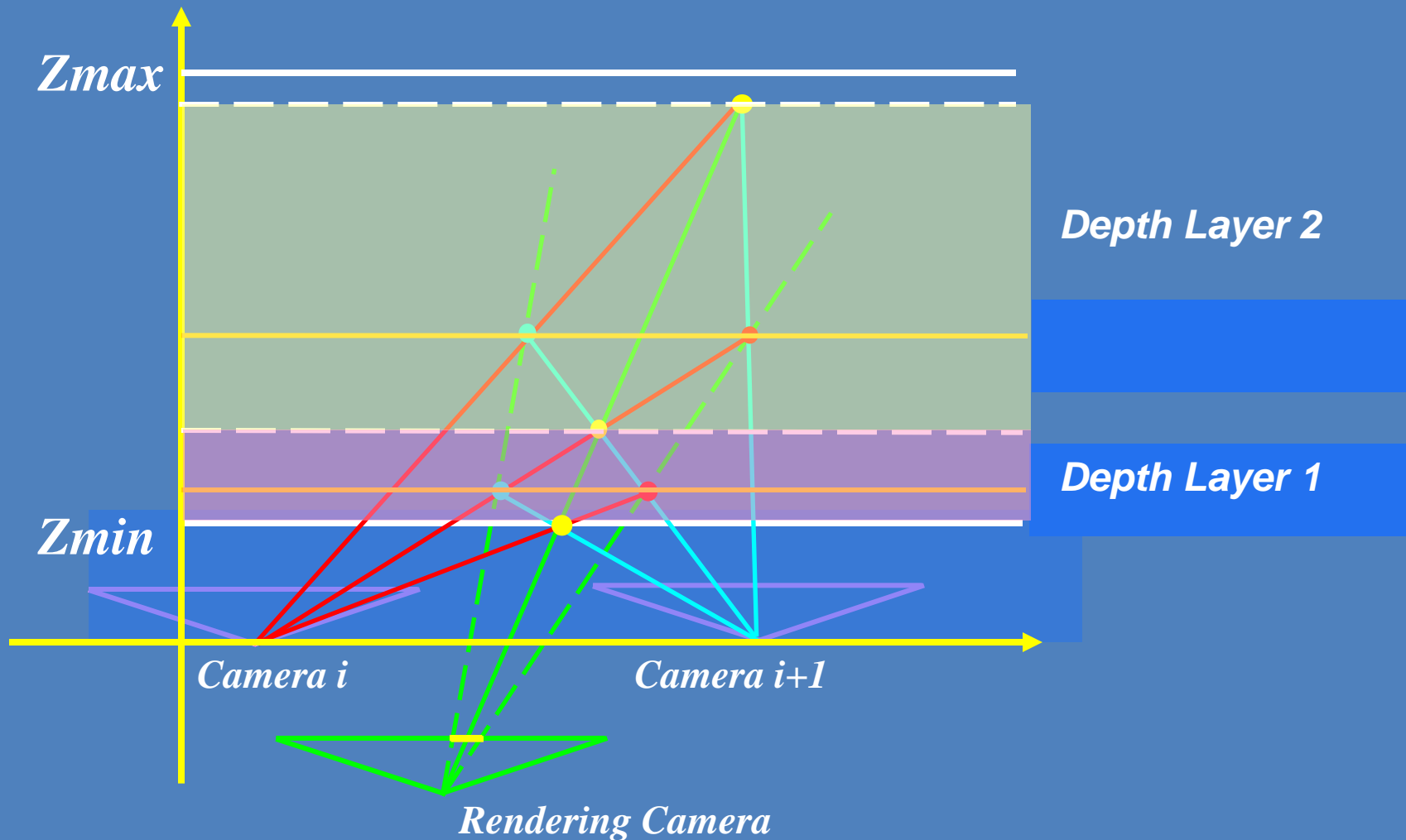


# A Geometrical Intuition





# A Geometrical Intuition





# Plenoptic Sampling



**48X48 Images**  
**No Depth**



**16X16 Images**  
**3Bits Depth**





# Plenoptic Sampling

48X48 Images without Depth

24X24 Images with 7Bits Depth



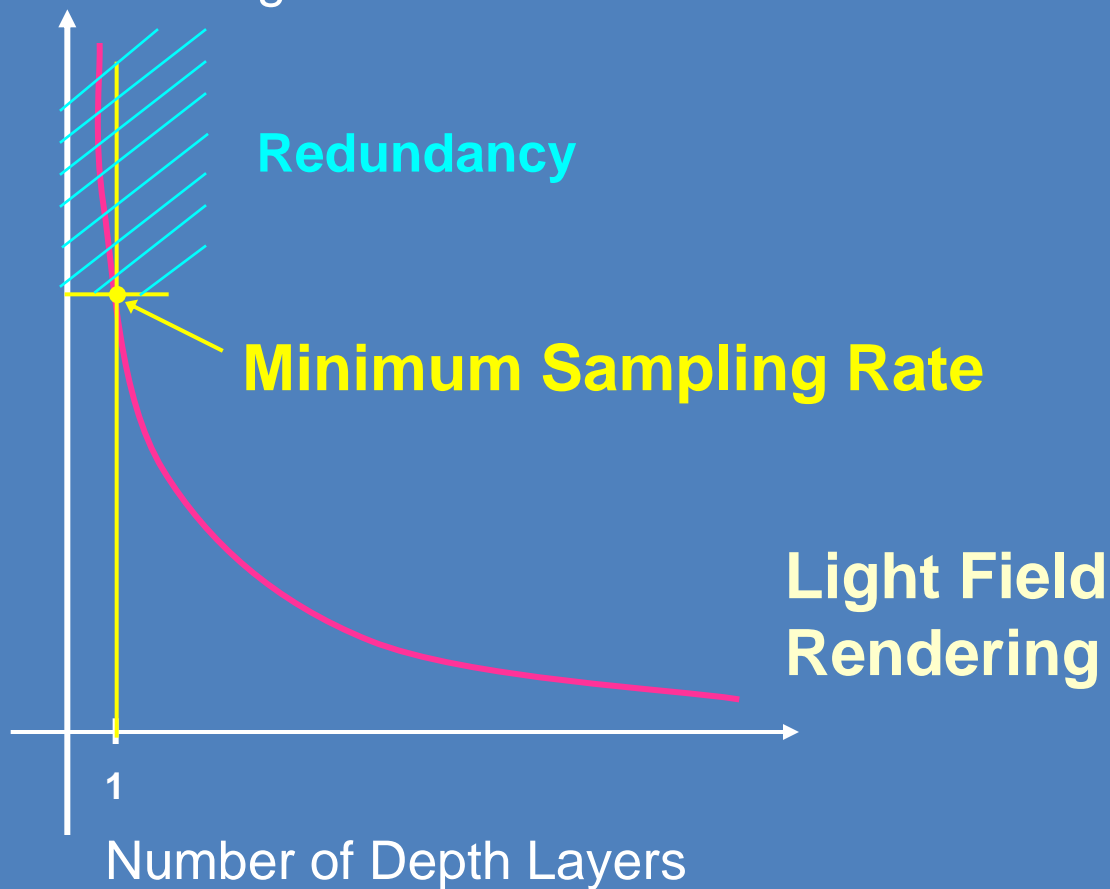
Antialiasing Rendering Needs  
2930X2930 images = **5,000GB**

Antialiasing Rendering Needs  
24X24 RGBD images = **0.5GB**



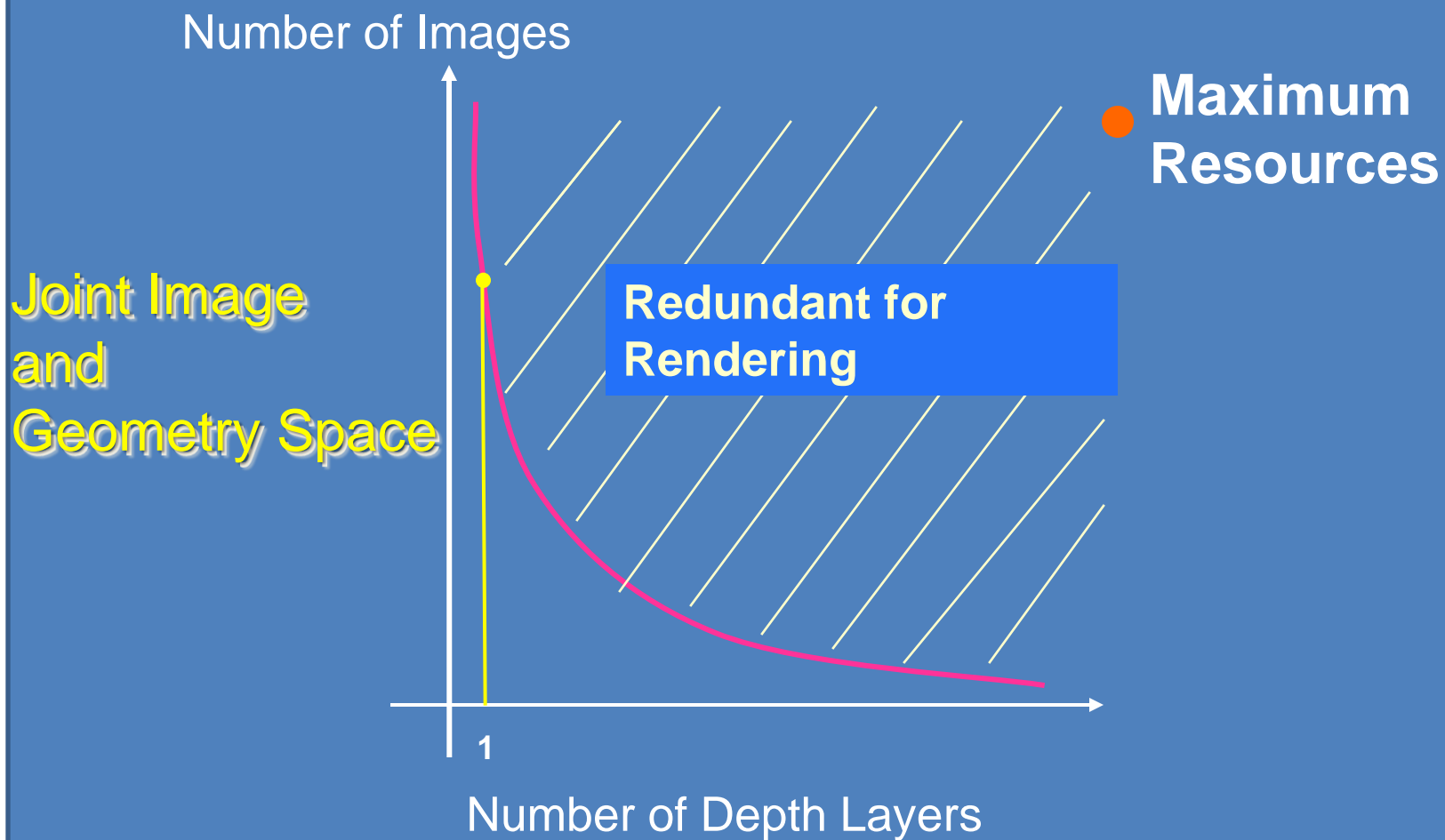
# Plenoptic Sampling

Number of Images





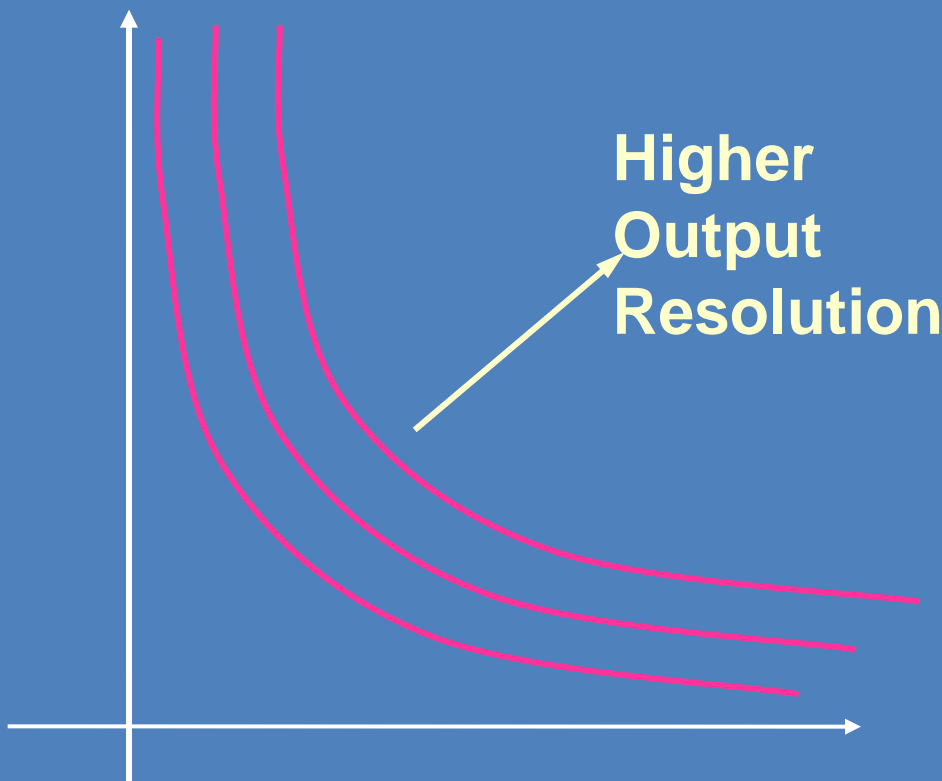
# Plenoptic Sampling



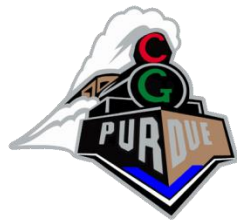


# Plenoptic Sampling

Number of Images



Number of Depth Layers



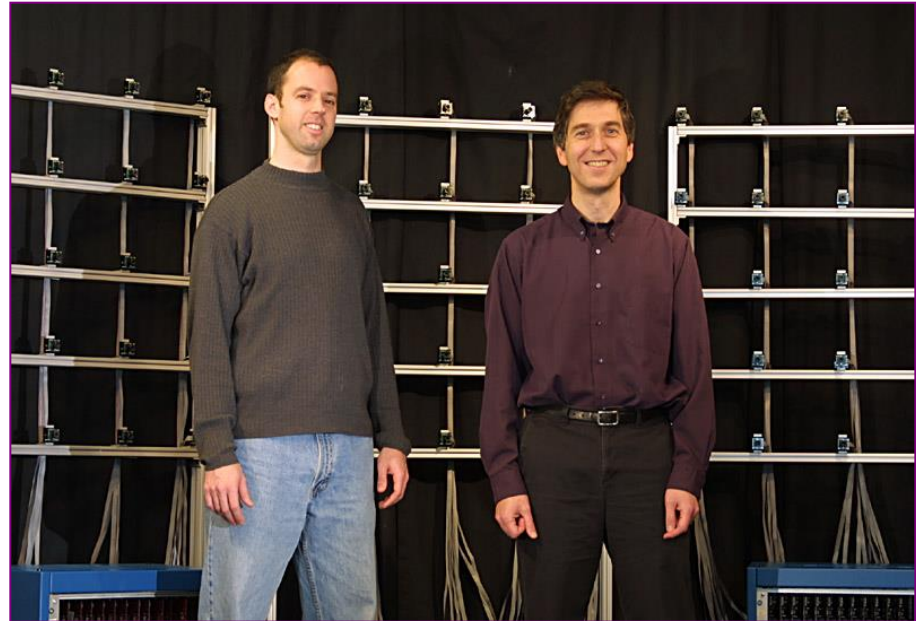
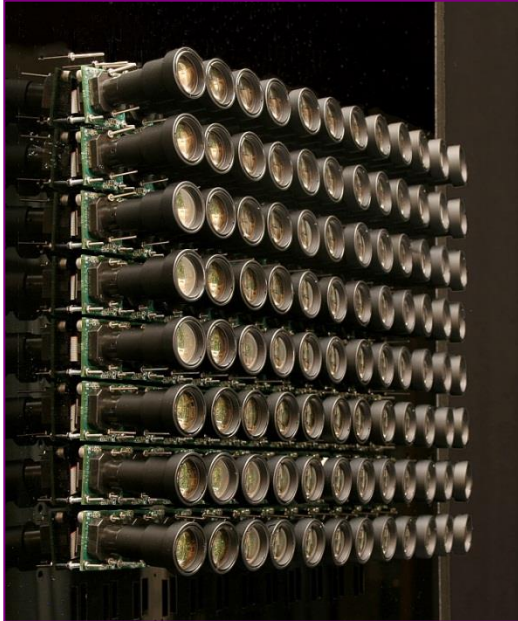
# List of projects

- high performance imaging using large camera arrays
- light field photography using a handheld plenoptic camera
- dual photography

# High performance imaging using large camera arrays



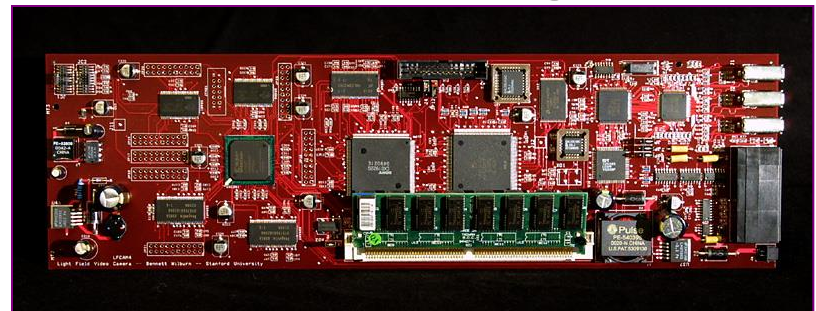
Bennett Wilburn, Neel Joshi, Vaibhav Vaish, Eino-Ville Talvala,  
Emilio Antunez,  
Adam Barth, Andrew Adams, Mark Horowitz, Marc Levoy



# Stanford multi-camera array



- $640 \times 480$  pixels  $\times$   
30 fps  $\times$  128 cameras
- synchronized timing
- continuous streaming
- flexible arrangement





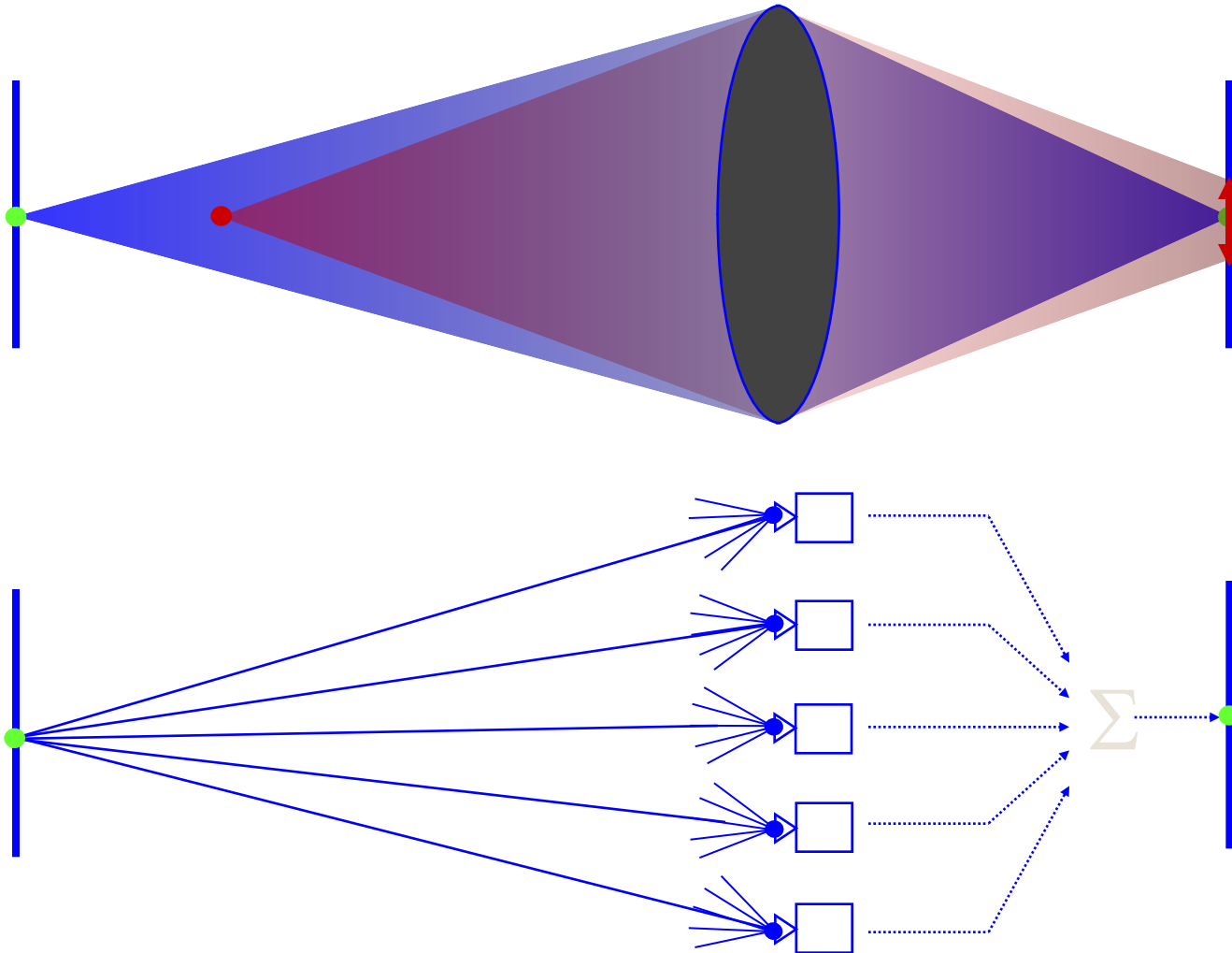
# Ways to use large camera arrays

- widely spaced → light field capture
- tightly packed → high-performance imaging
- intermediate spacing → synthetic aperture photography



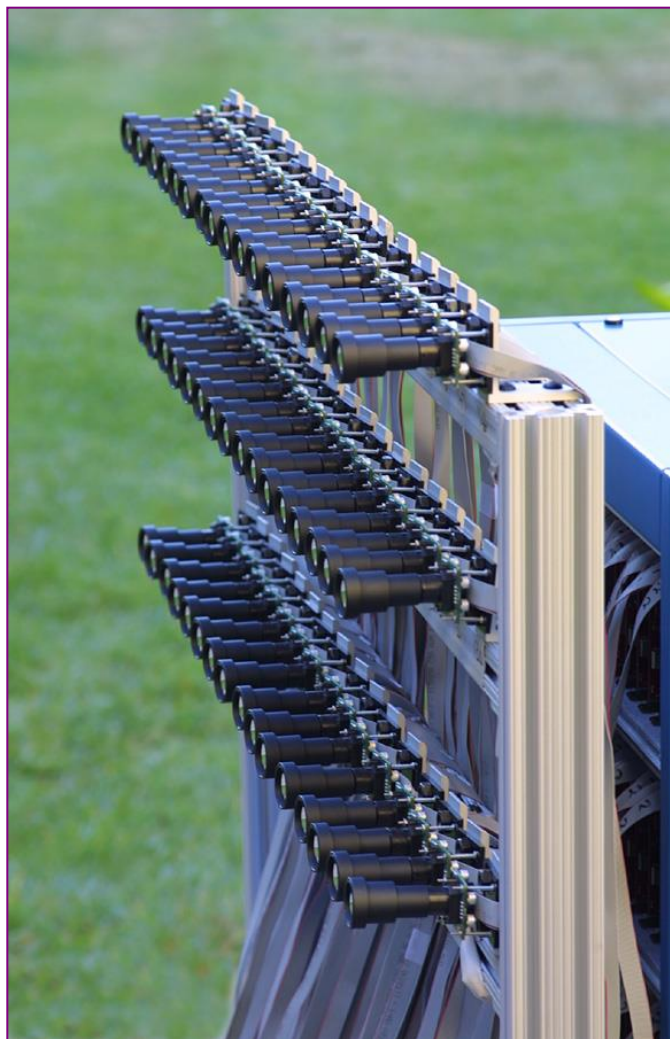


# Intermediate camera spacing: synthetic aperture photography



# Example using 45 cameras

[Vaish CVPR]

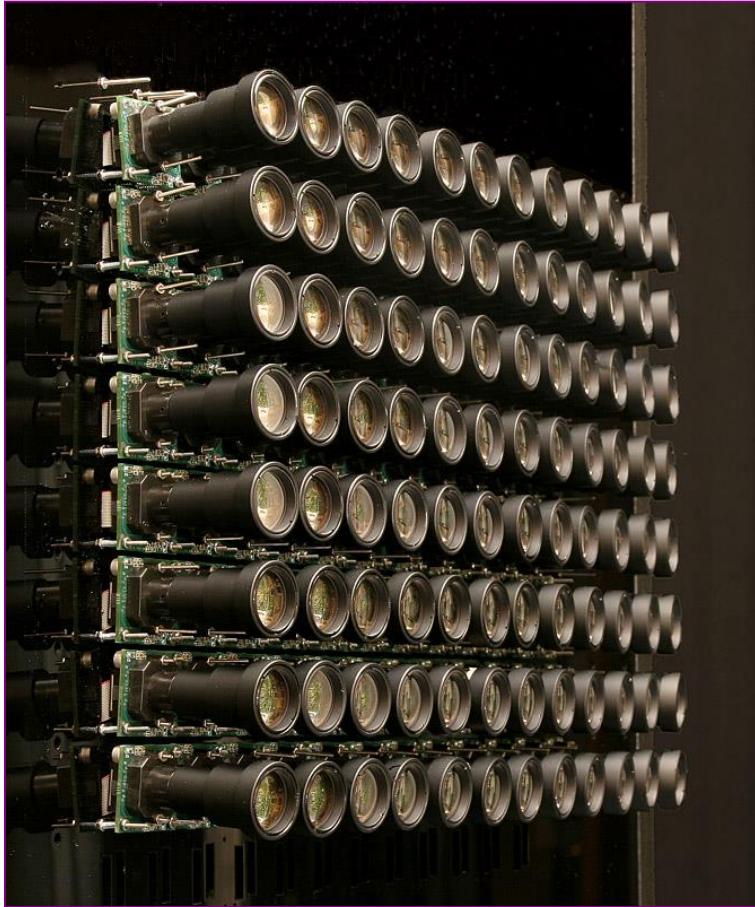






# Tiled camera array

Can we match the image quality of a cinema camera?



- world's largest video camera
- no parallax for distant objects
- poor lenses limit image quality
- seamless mosaicing isn't hard

# Tiled panoramic image (before geometric or color calibration)



# Tiled panoramic image (after calibration and blending)





# Tiled camera array

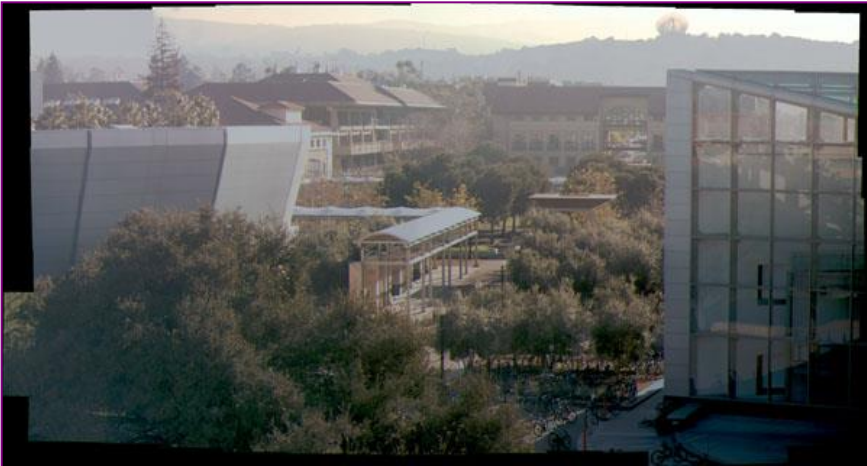
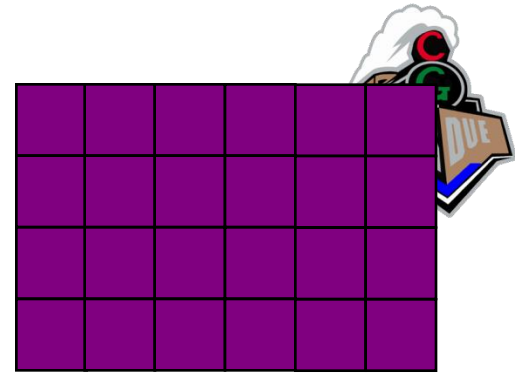
Can we match the image quality of a cinema camera?



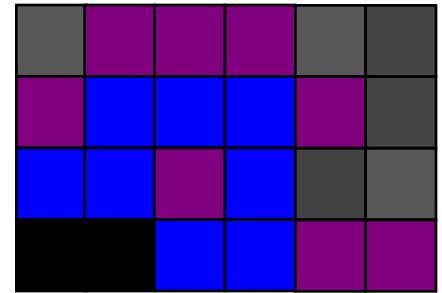
- world's largest video camera
- no parallax for distant objects
- poor lenses limit image quality
- seamless mosaicing isn't hard
- per-camera exposure



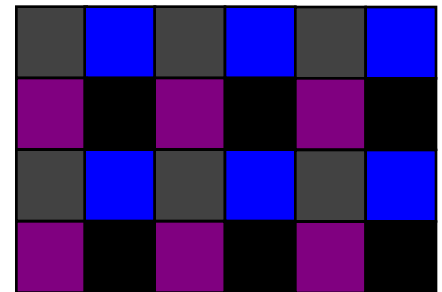
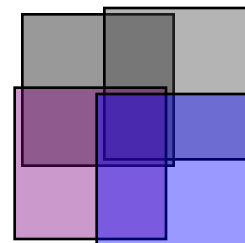
same  
exposure in  
all cameras



individually  
metered



checkerboard  
of exposures



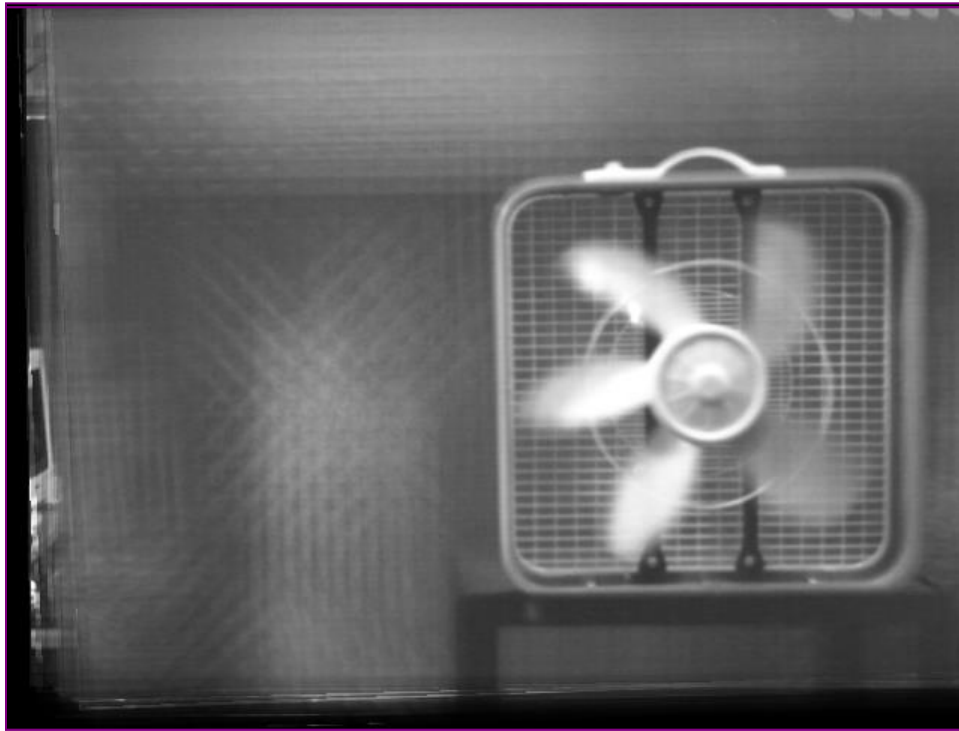


# High-performance photography as multi-dimensional sampling

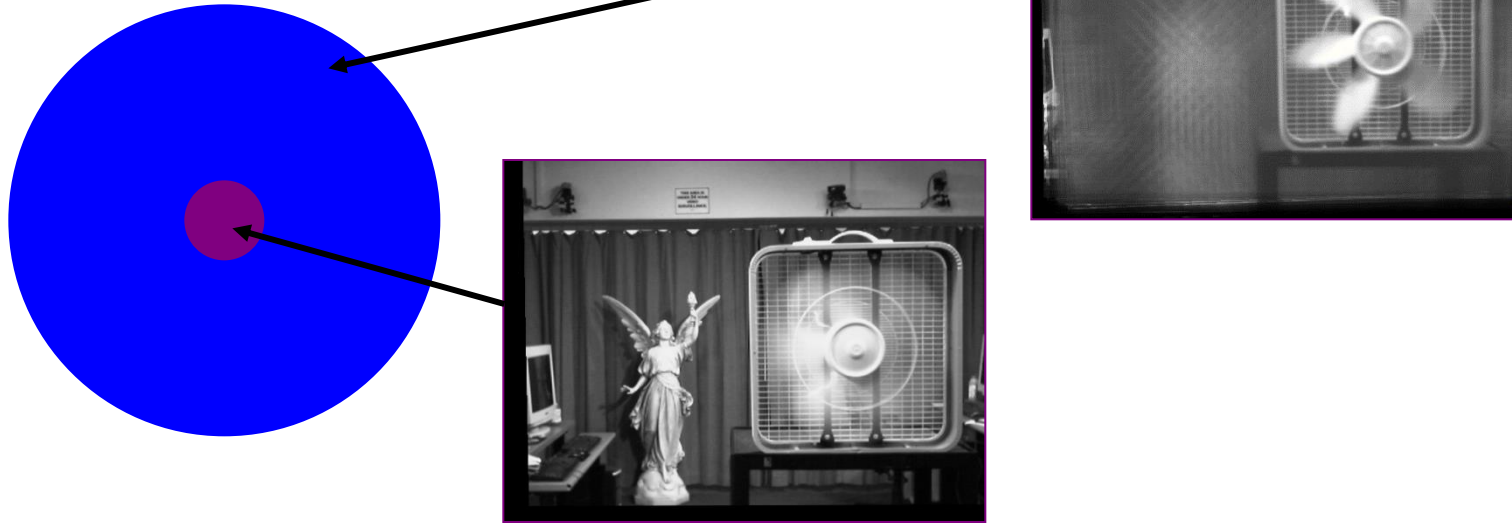


- spatial resolution
- field of view
- frame rate
- dynamic range
- bits of precision
- depth of field
- focus setting
- color sensitivity

# Spacetime aperture shaping

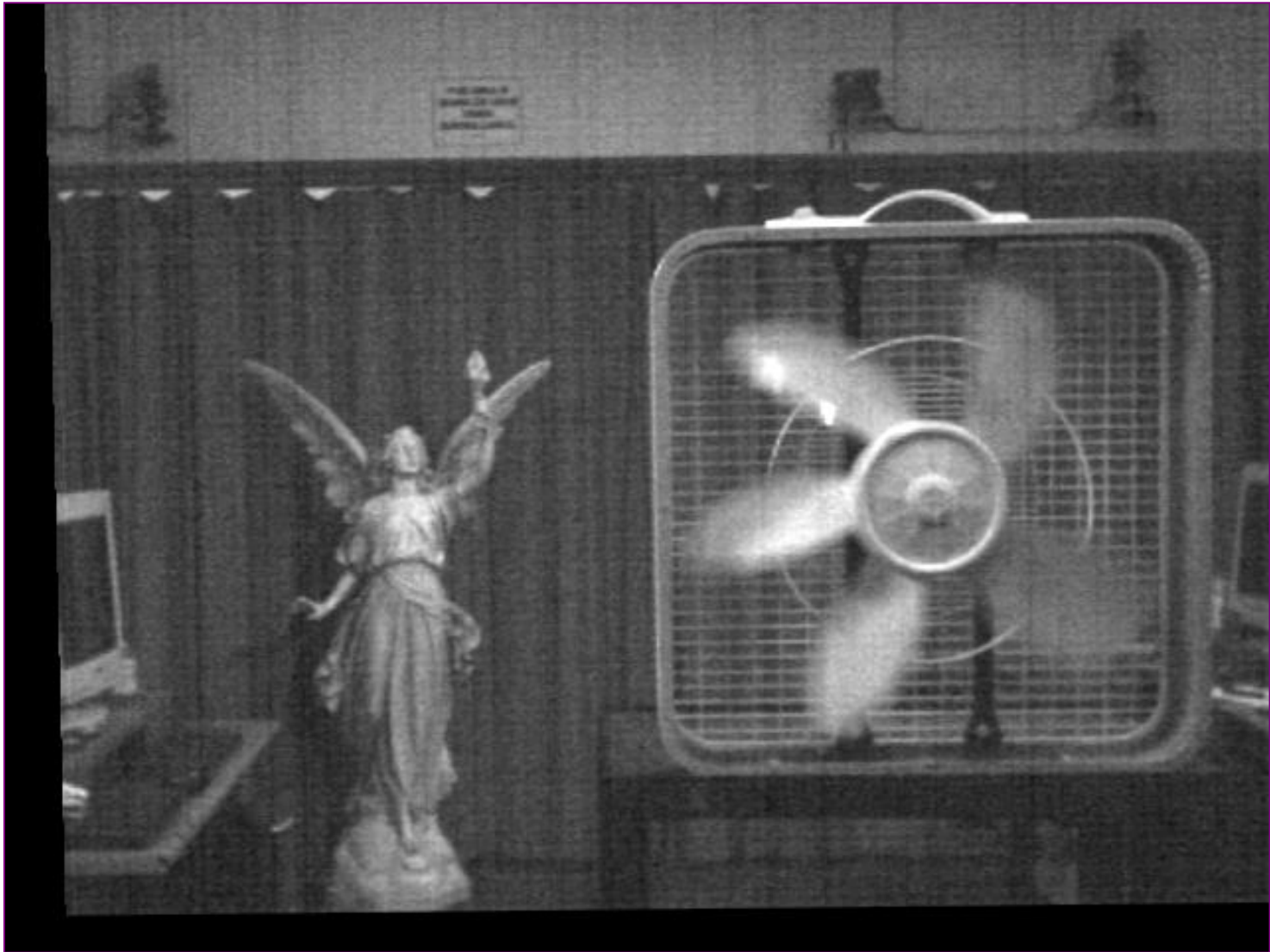


- shorten exposure time to freeze motion → dark
- stretch contrast to restore level → noisy
- increase (synthetic) aperture to capture more light → decreases depth of field



- center of aperture: few cameras, long exposure → high depth of field, low noise, but action is blurred
- periphery of aperture: many cameras, short exposure → freezes action, low noise, but low depth of field

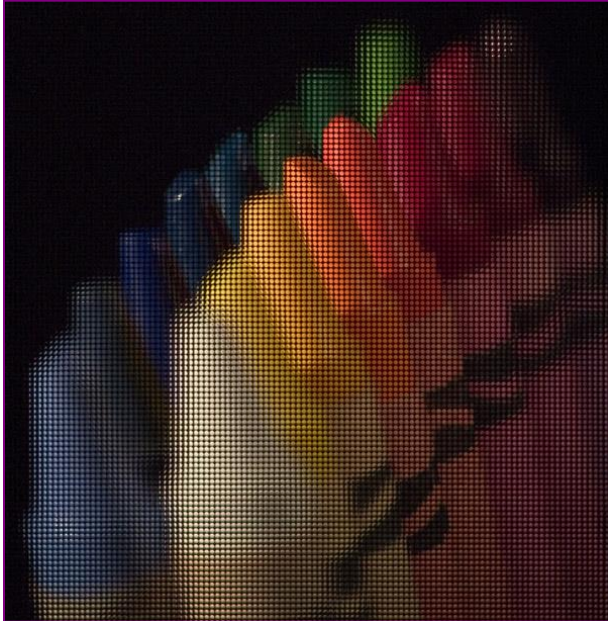




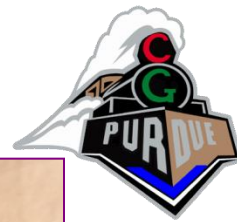
# Light field photography using a handheld plenoptic camera



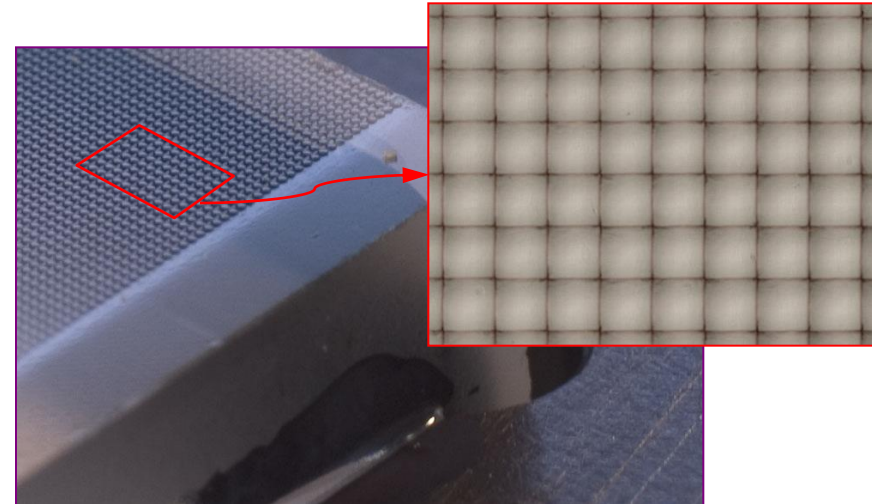
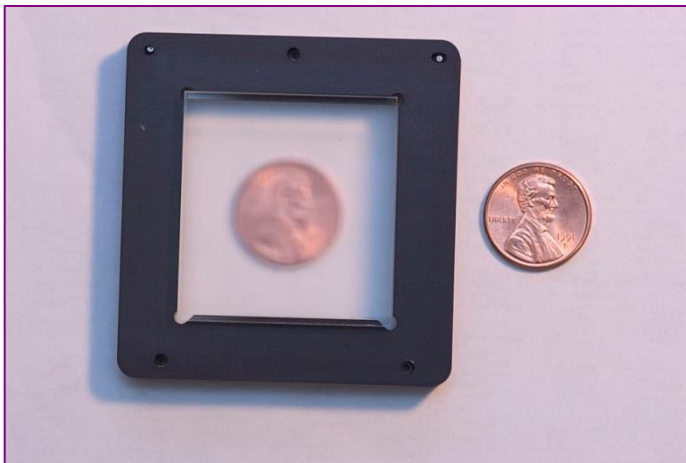
Ren Ng, Marc Levoy, Mathieu Brédif,  
Gene Duval, Mark Horowitz and Pat  
Hanrahan



# Prototype camera



Contax medium format camera Kodak 16-megapixel sensor



Adaptive Optics microlens array  $125\mu$  square-sided microlenses

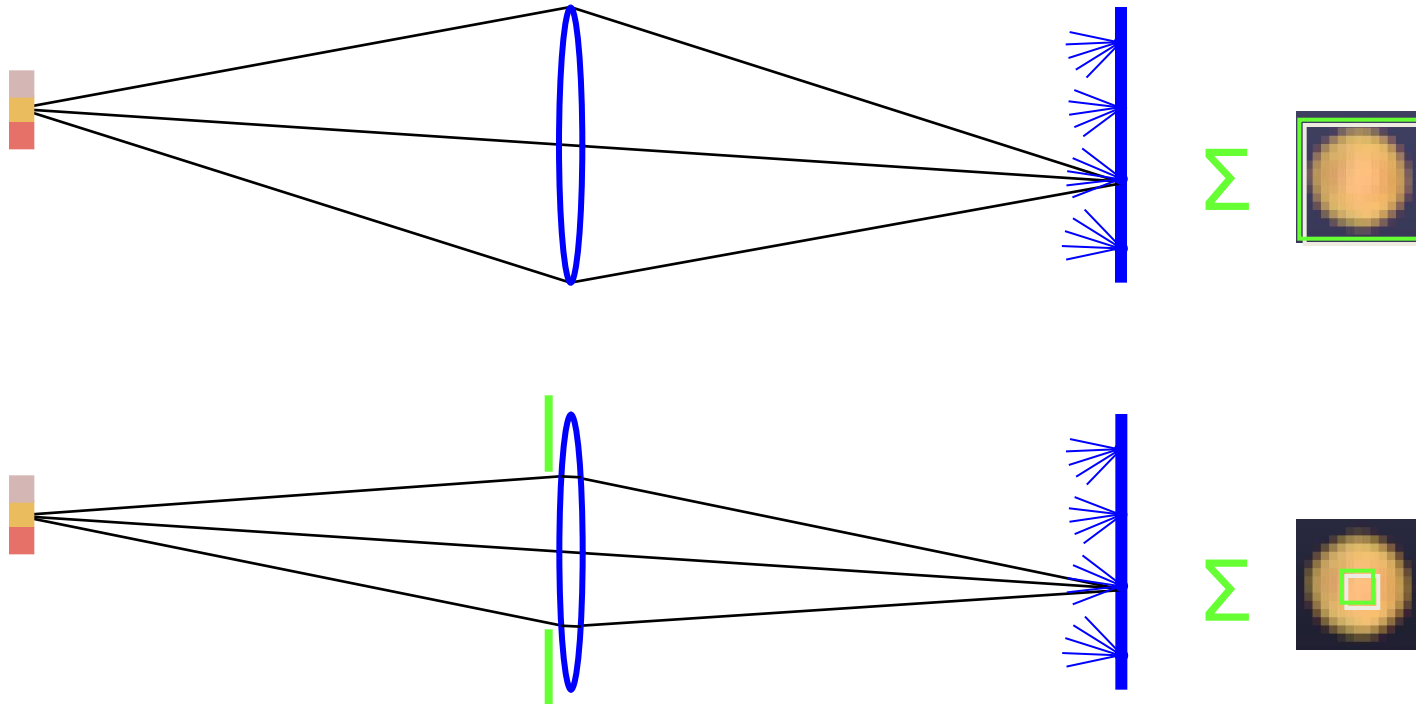
$$4000 \times 4000 \text{ pixels} \div 292 \times 292 \text{ lenses} = 14 \times 14 \text{ pixels per lens}$$







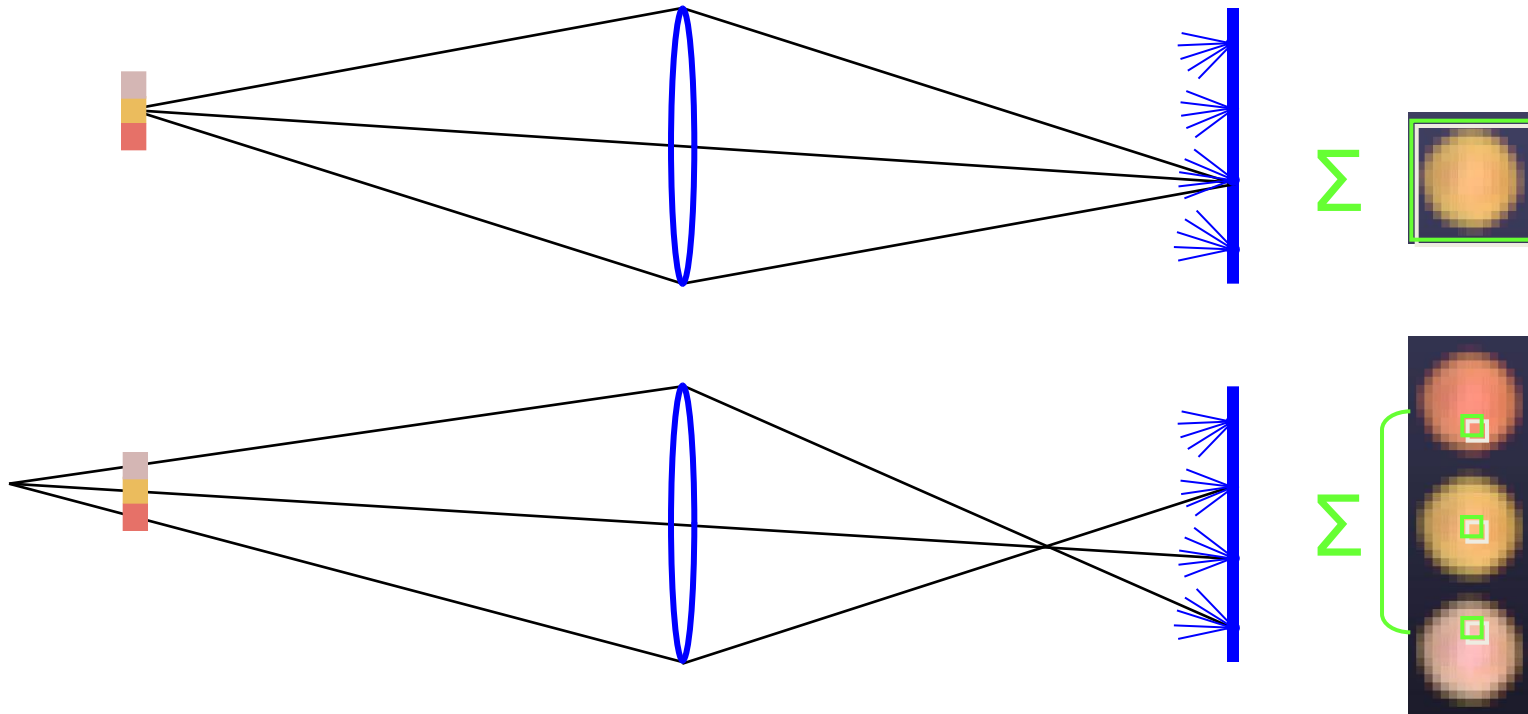
# Digitally stopping-down



- stopping down = summing only the central portion of each microlens



# Digital refocusing



- refocusing = summing windows extracted from several microlenses

# A digital refocusing theorem

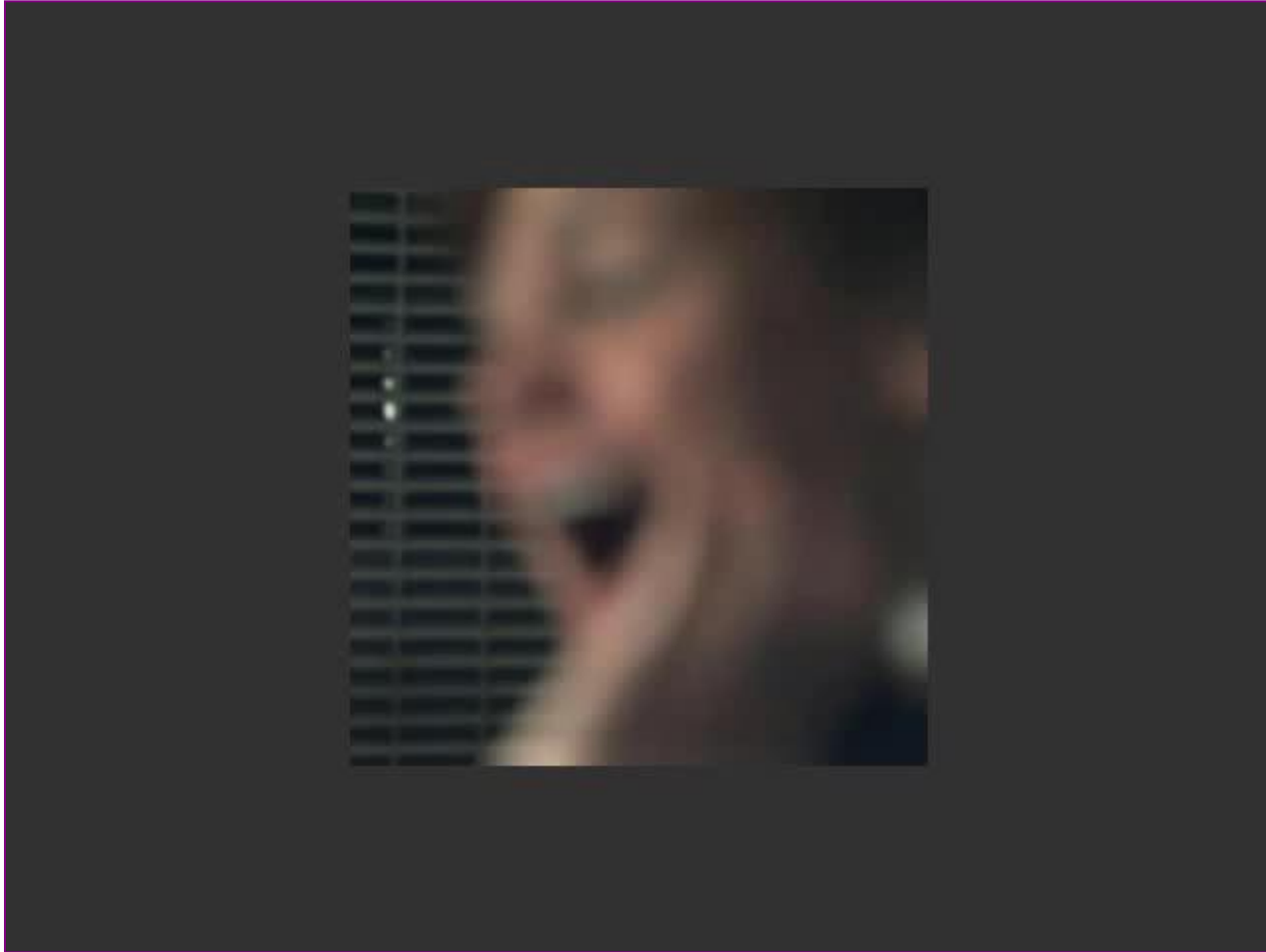


- an  $f / N$  light field camera, with  $P \times P$  pixels under each microlens, can produce views as sharp as an  $f / (N \times P)$  conventional camera
  - or –
- it can produce views with a shallow depth of field ( $f / N$ ) focused anywhere within the depth of field of an  $f / (N \times P)$  camera

# Example of digital refocusing

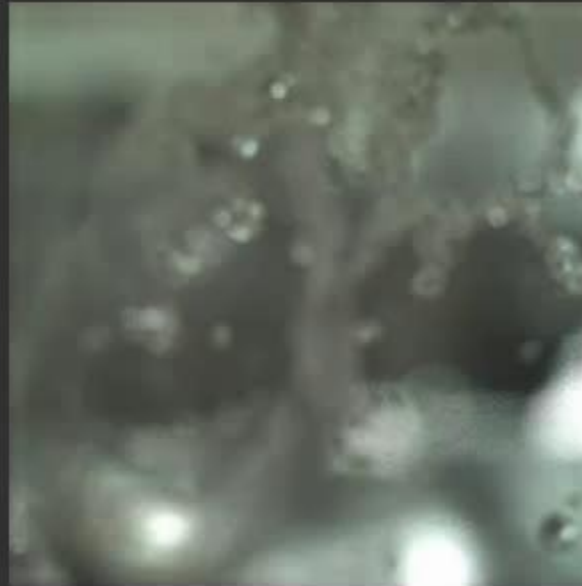


# Refocusing portraits



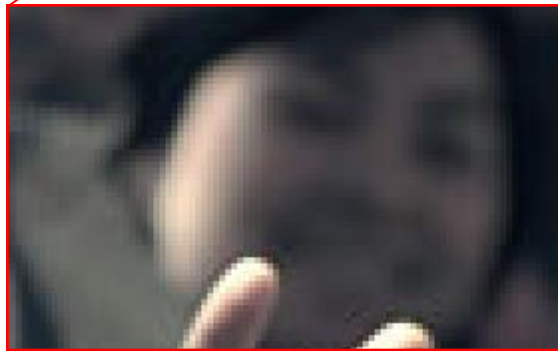


# Action photography



**Focusing through a splash of water**

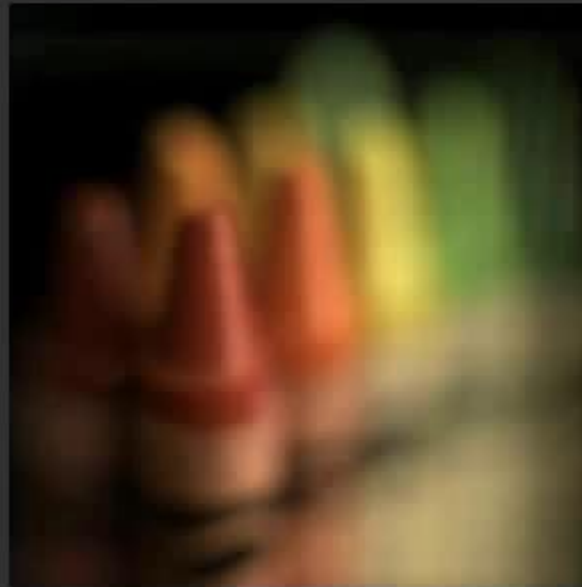
# Extending the depth of field



conventional photograph, main lens at  $f/4$     conventional photograph, main lens at  $f/22$     after all-focus algorithm

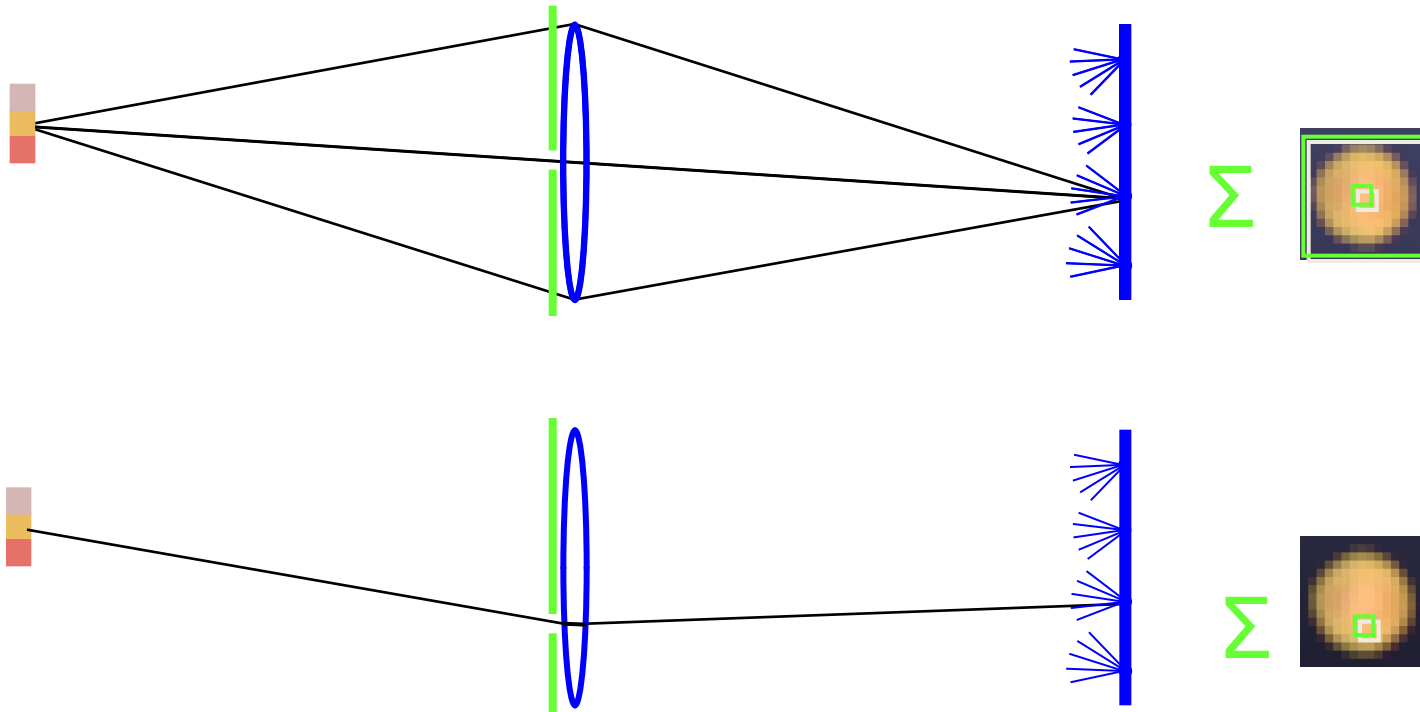
[Agarwala 2004]

# Macrophotography





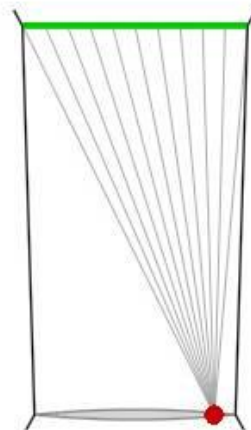
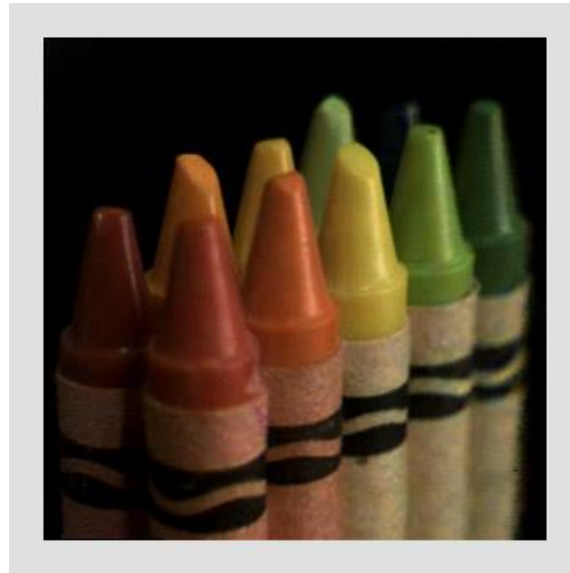
# Digitally moving the observer



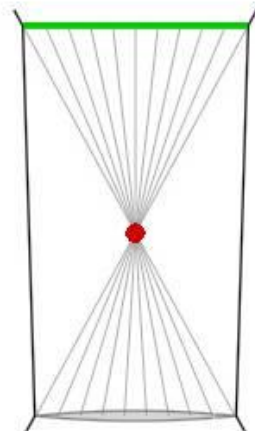
- moving the observer = moving the window we extract from the microlenses



# Example of moving the observer



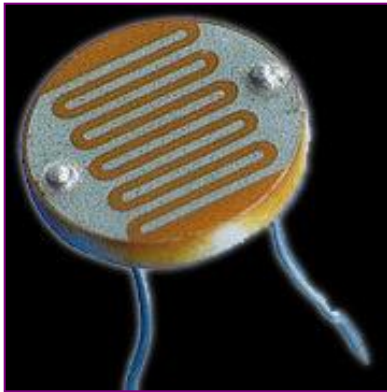
# Moving backward and forward



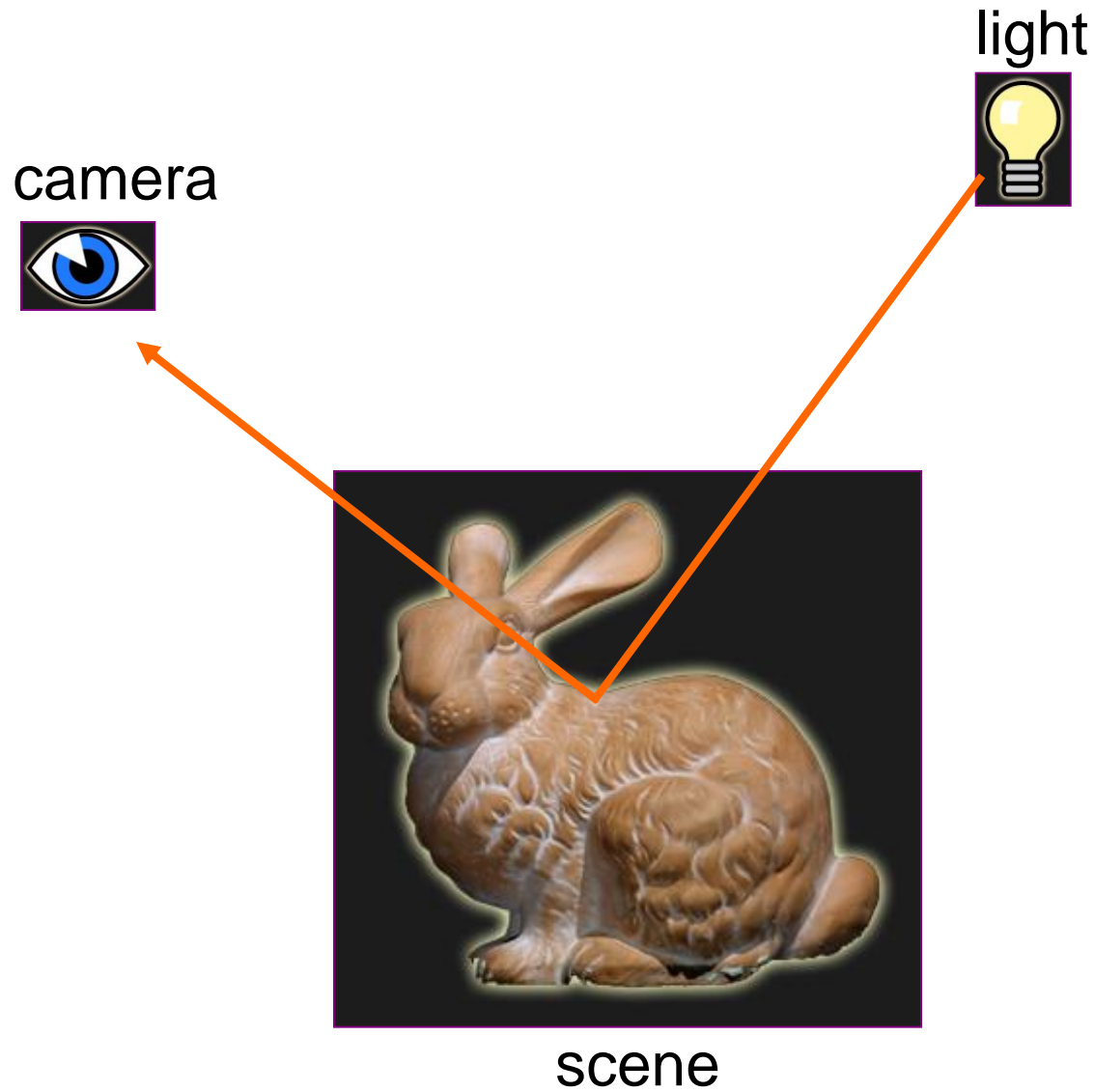
# Dual Photography



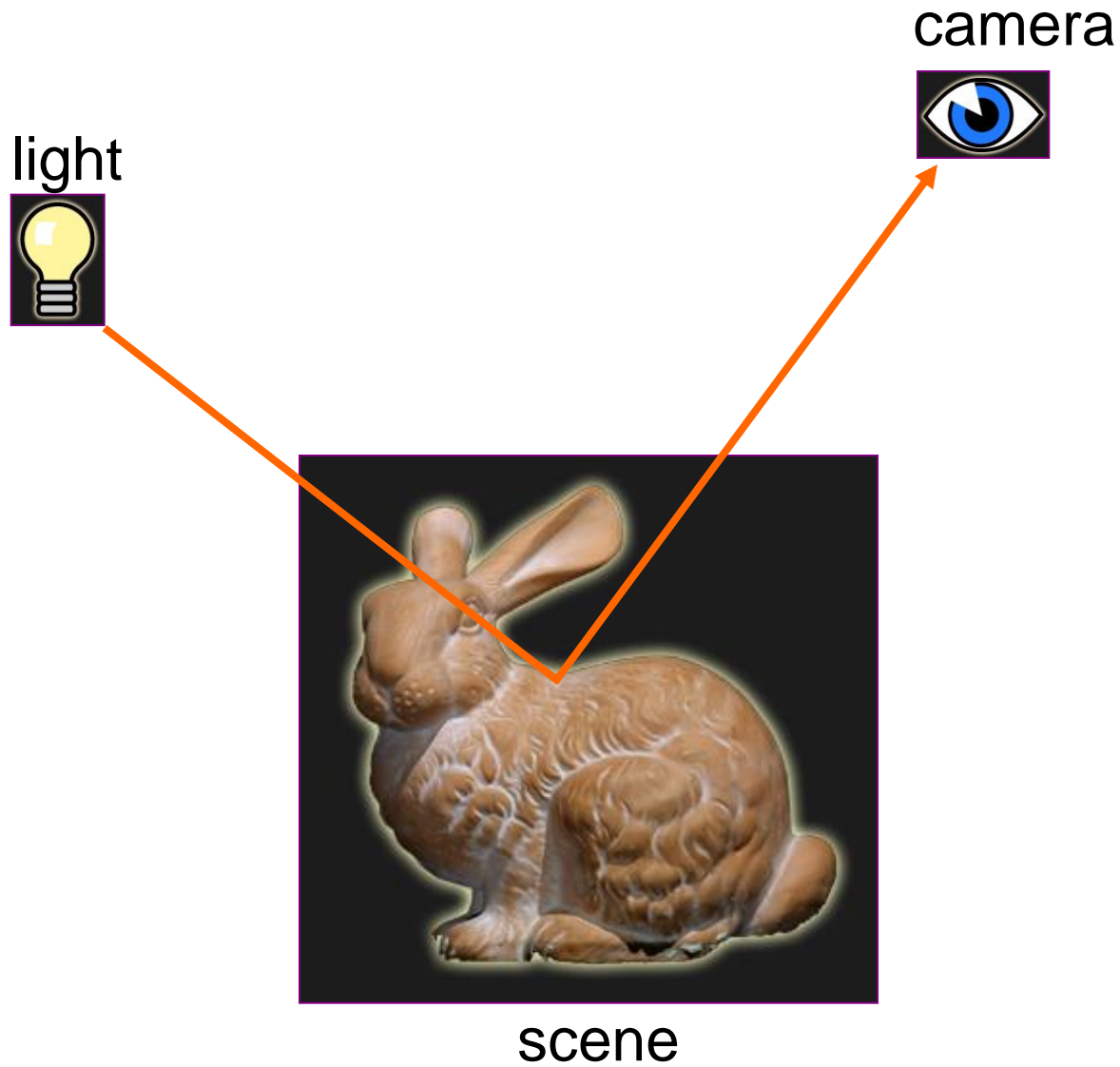
Pradeep Sen, Billy Chen, Gaurav Garg, Steve Marschner,  
Mark Horowitz, Marc Levoy, Hendrik Lensch



# Helmholtz reciprocity



# Helmholtz reciprocity



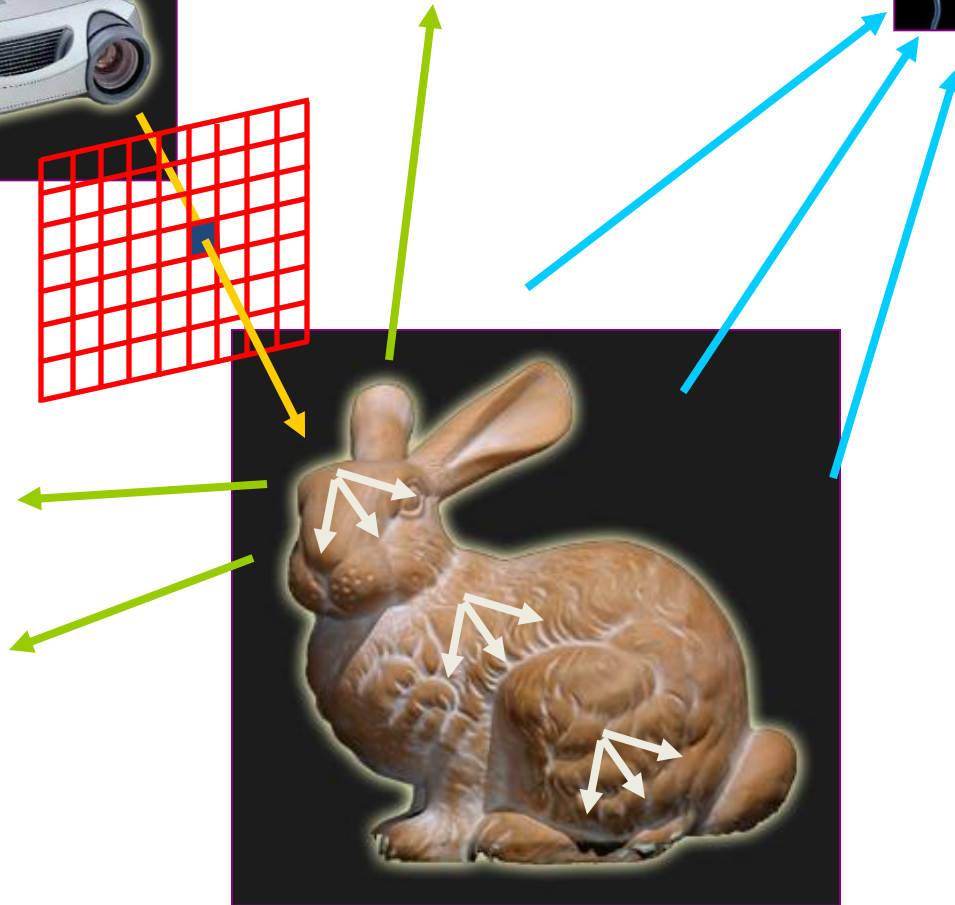
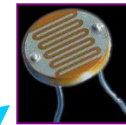
# Measuring transport along a set of paths



projector



photocell

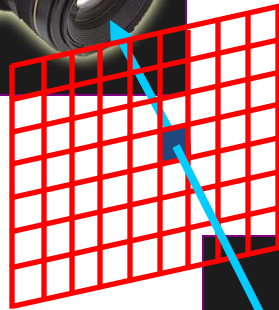


scene

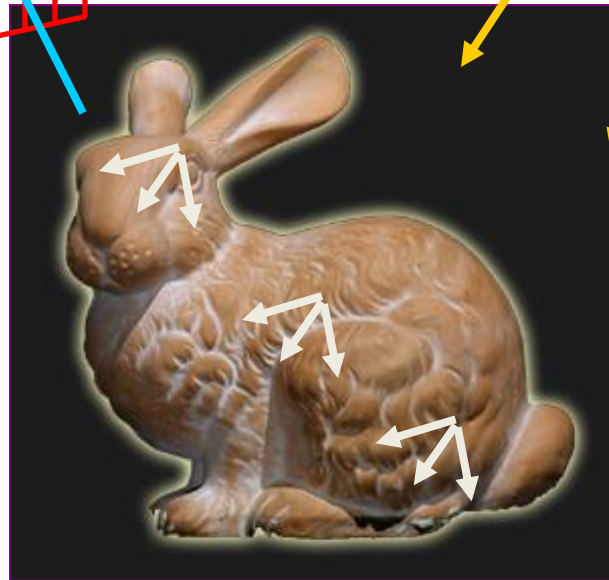
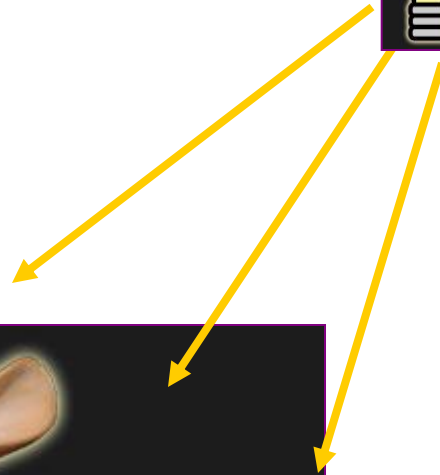
# Reversing the paths



camera



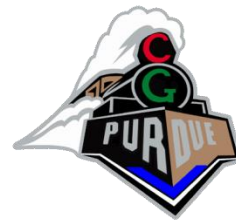
point light



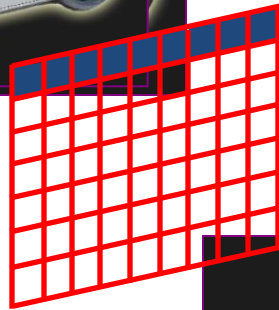
scene



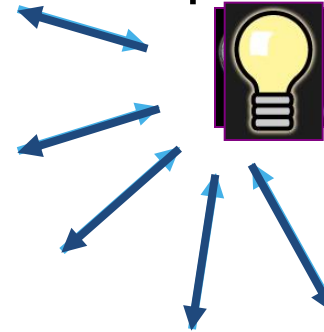
# Forming a dual photograph



“dual” camera  
projector



“dual” light  
projector



scene



# Forming a dual photograph



“dual” camera

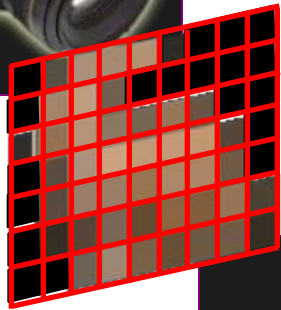
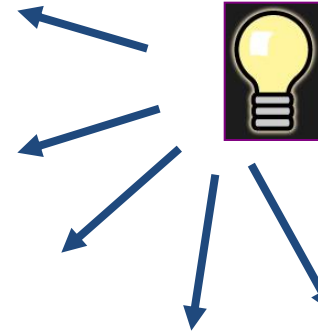


image of scene



scene

“dual” light





# Physical demonstration

- light replaced with projector
- camera replaced with photocell
- projector scanned across the scene



conventional photograph,  
with light coming from right



dual photograph,  
as seen from projector's position  
and as illuminated from photocell's position

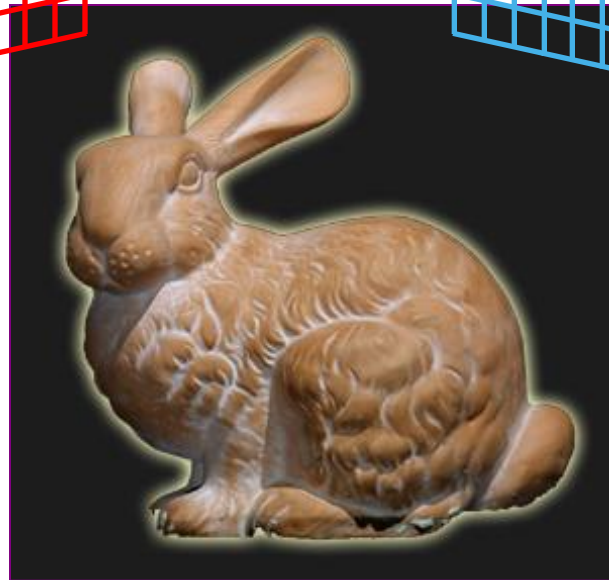
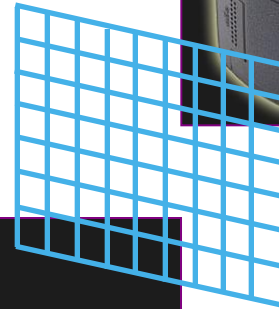
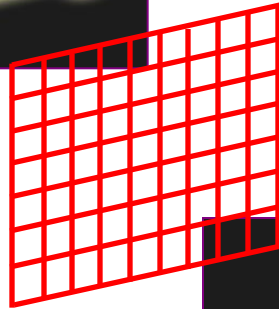
# The 4D transport matrix



projector



photocell

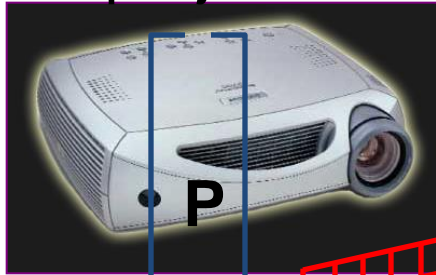


scene

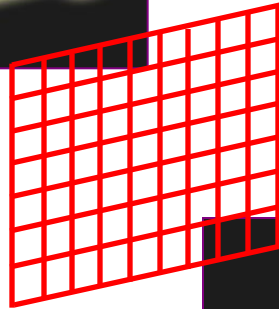
# The 4D transport matrix



projector



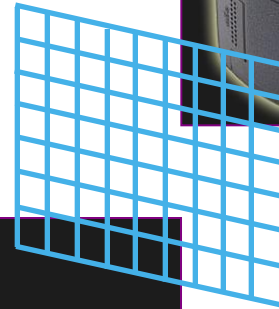
$pq \times 1$



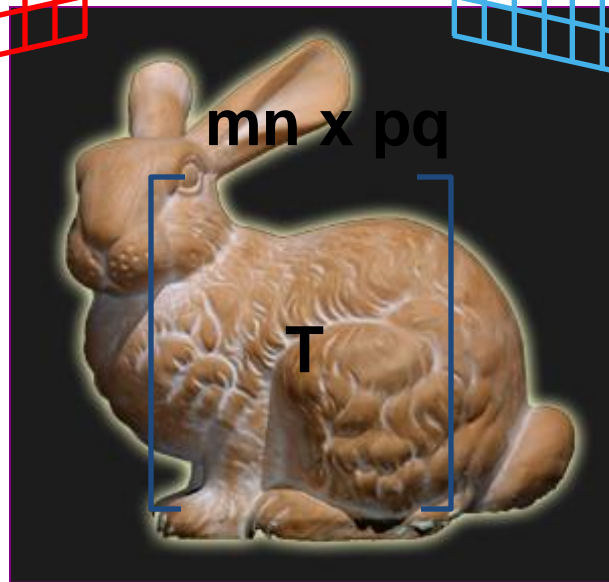
camera



$mn \times 1$



$mn \times pq$



scene

# The 4D transport matrix



$$\begin{array}{c} \left[ \begin{array}{c} \mathbf{C} \\ \hline \end{array} \right] \\ mn \times 1 \end{array} = \begin{array}{c} mn \times pq \\ \left[ \begin{array}{c} \mathbf{T} \\ \hline \end{array} \right] \end{array} \begin{array}{c} \left[ \begin{array}{c} \mathbf{P} \\ \hline \end{array} \right] \\ pq \times 1 \end{array}$$

# The 4D transport matrix



$$\begin{array}{c} \left[ \begin{array}{c} \\ \\ \\ \\ \end{array} \right] \\ \text{mn} \times \mathbf{1} \end{array} = \begin{array}{c} \text{mn} \times \text{pq} \\ \left[ \begin{array}{c} \\ \\ \\ \\ \end{array} \right] \\ \mathbf{T} \end{array} \begin{array}{c} \left[ \begin{array}{c} 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{array} \right] \\ \text{pq} \times \mathbf{1} \end{array}$$

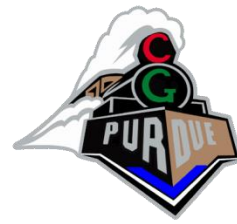
# The 4D transport matrix



$$\begin{array}{c} \left[ \begin{array}{c} \mathbf{C} \end{array} \right] \\ mn \times 1 \end{array} = \begin{array}{c} mn \times pq \\ \left[ \begin{array}{c} \text{light orange bar} \\ \text{orange bar} \end{array} \right] \mathbf{T} \end{array} \begin{array}{c} \left[ \begin{array}{c} 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{array} \right] \\ pq \times 1 \end{array}$$

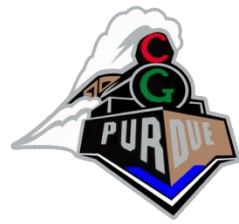


# The 4D transport matrix



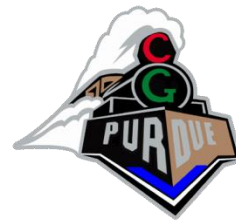
$$\begin{array}{c} \left[ \begin{array}{c} \mathbf{C} \end{array} \right] \\ \mathbf{mn} \times \mathbf{1} \end{array} = \begin{array}{c} \mathbf{mn} \times \mathbf{pq} \\ \left[ \begin{array}{c} \text{orange bar} \\ \text{orange bar} \\ \text{orange bar} \end{array} \right] \mathbf{T} \end{array} \begin{array}{c} \left[ \begin{array}{c} 0 \\ 0 \\ 1 \\ 0 \\ 0 \end{array} \right] \\ \mathbf{pq} \times \mathbf{1} \end{array}$$

# The 4D transport matrix



$$\begin{array}{c} \left[ \begin{array}{c} \mathbf{C} \\ \hline \end{array} \right] \\ mn \times 1 \end{array} = \begin{array}{c} mn \times pq \\ \left[ \begin{array}{c} \mathbf{T} \\ \hline \end{array} \right] \end{array} \begin{array}{c} \left[ \begin{array}{c} \mathbf{P} \\ \hline \end{array} \right] \\ pq \times 1 \end{array}$$

# The 4D transport matrix



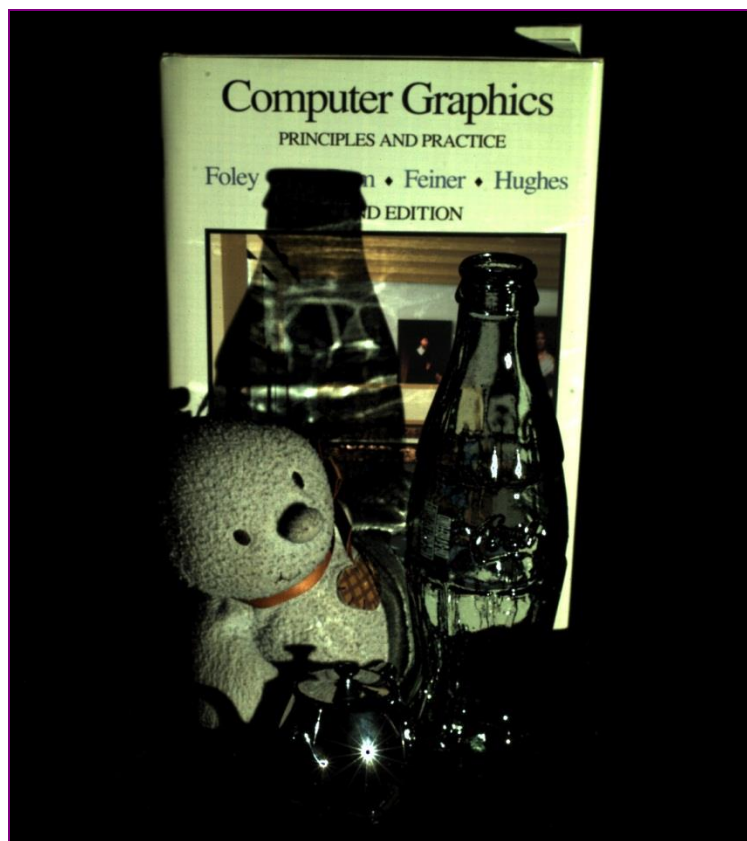
$$\begin{array}{c} \left[ \begin{array}{c} \mathbf{C} \end{array} \right] \\ \mathbf{mn} \times \mathbf{1} \end{array} = \begin{array}{c} \mathbf{mn} \times \mathbf{pq} \\ \left[ \begin{array}{c} \mathbf{T} \end{array} \right] \end{array} \begin{array}{c} \left[ \begin{array}{c} \mathbf{P} \end{array} \right] \\ \mathbf{pq} \times \mathbf{1} \end{array}$$

applying Helmholtz reciprocity...

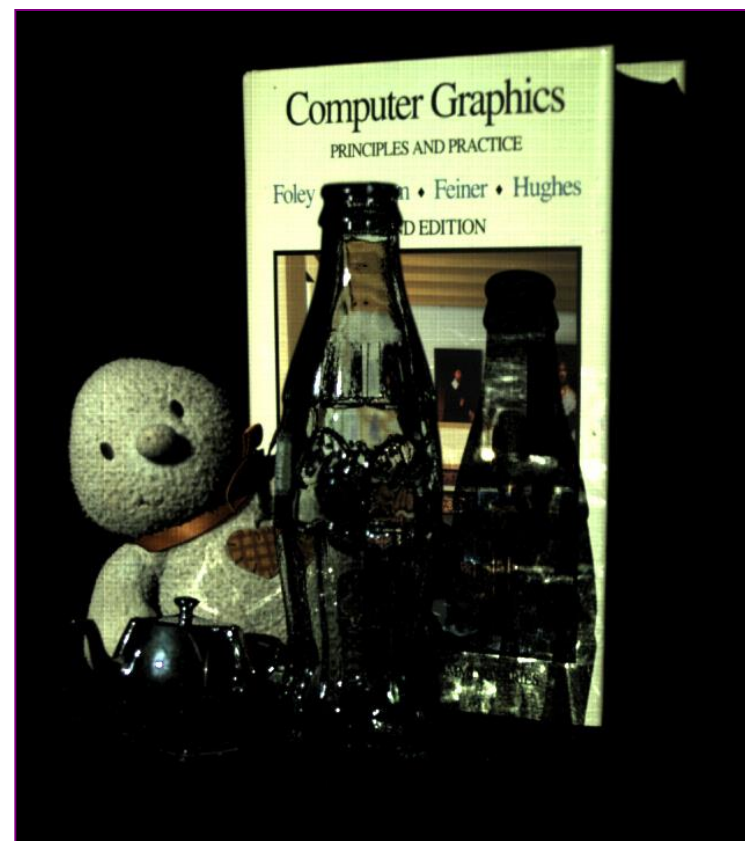
$$\begin{array}{c} \left[ \begin{array}{c} \mathbf{C}' \end{array} \right] \\ \mathbf{pq} \times \mathbf{1} \end{array} = \begin{array}{c} \mathbf{pq} \times \mathbf{mn} \\ \left[ \begin{array}{c} \mathbf{T}^T \end{array} \right] \end{array} \begin{array}{c} \left[ \begin{array}{c} \mathbf{P}' \end{array} \right] \\ \mathbf{mn} \times \mathbf{1} \end{array}$$



# Example



conventional photograph  
with light coming from right



dual photograph  
as seen from projector's position

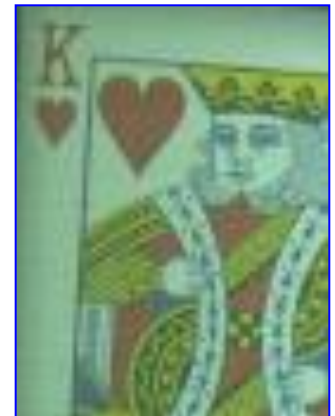
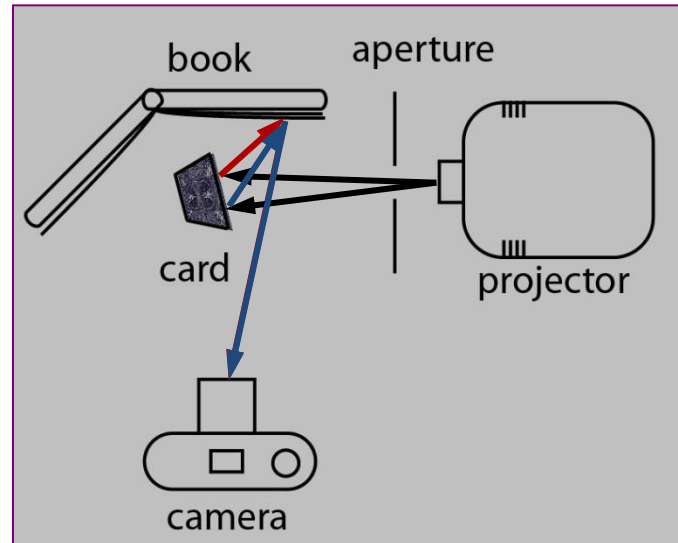
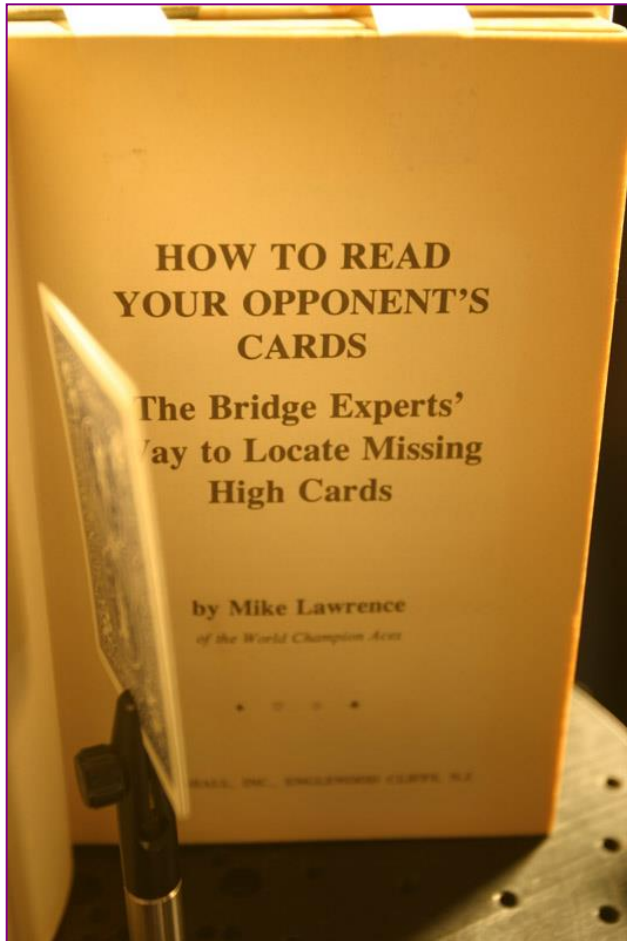
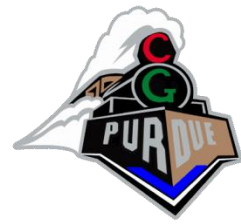
# Properties of the transport matrix



- little interreflection  $\rightarrow$  sparse matrix
- many interreflections  $\rightarrow$  dense matrix
- convex object  $\rightarrow$  diagonal matrix
- concave object  $\rightarrow$  full matrix

Can we create a dual photograph entirely from diffuse reflections?

# Dual photography from diffuse reflections



the camera's view



# The relighting problem

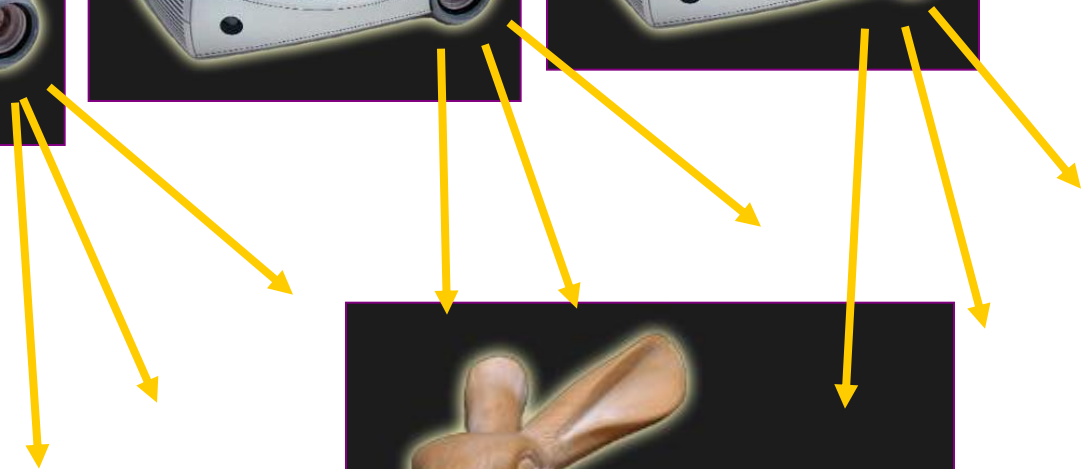


Paul Debevec's  
Light Stage 3

- subject captured under multiple lights
- one light at a time, so subject must hold still
- point lights are used, so can't relight with cast shadows



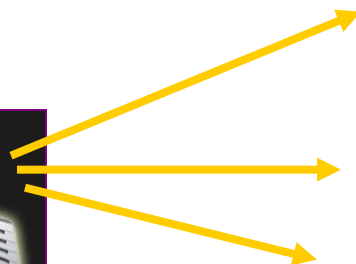
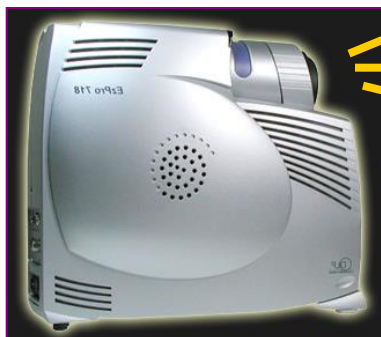
# The 6D transport matrix







# The 6D transport matrix



# The advantage of dual photography



- capture of a scene as illuminated by different lights cannot be parallelized
- capture of a scene as viewed by different cameras can be parallelized

# Measuring the 6D transport matrix



projector



camera array



scene



# Relighting with complex illumination



projector



camera array



scene



$$\begin{matrix} & & pq \times mn \times uv \\ \left[ \begin{matrix} C' \end{matrix} \right] & = & \left[ \begin{matrix} T^T \end{matrix} \right] \left[ \begin{matrix} P' \end{matrix} \right] \\ pq \times 1 & & mn \times uv \times 1 \end{matrix}$$

- step 1: measure 6D transport matrix T
- step 2: capture a 4D light field
- step 3: relight scene using captured light field

# Running time

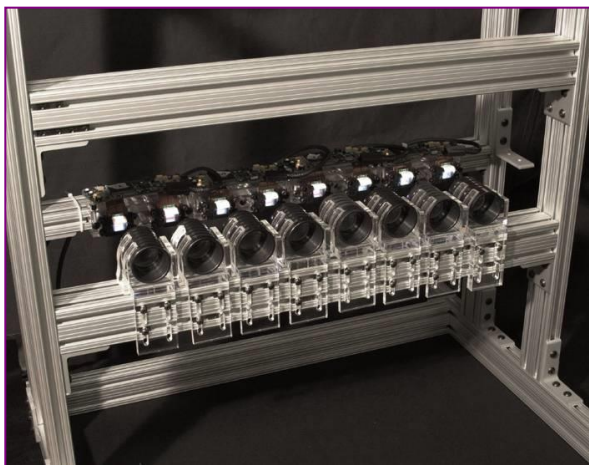


- the different rays within a projector can in fact be parallelized to some extent
- this parallelism can be discovered using a coarse-to-fine adaptive scan
- can measure a 6D transport matrix in 5 minutes

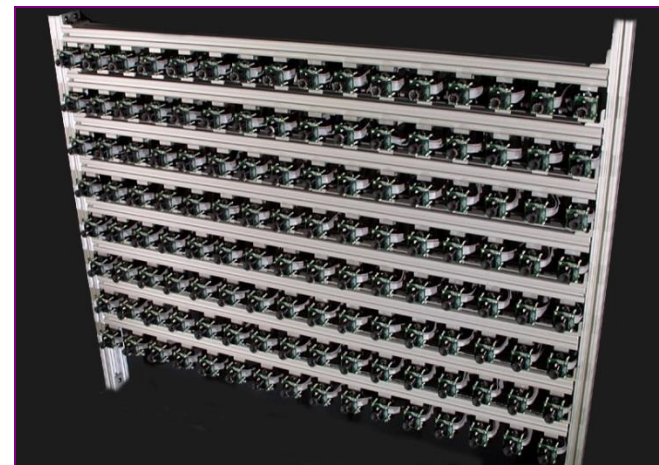
# Can we measure an 8D transport matrix?



projector array



camera array



scene



# Update

- Google, AR/VR, and Lightfields:
  - <https://www.youtube.com/watch?v=IRKOMtlyj0U>
- Seeing through things with lightfields:
  - [http://graphics.stanford.edu/papers/plane+parallax\\_calib/](http://graphics.stanford.edu/papers/plane+parallax_calib/)
- Microscope Lightfields
  - <http://graphics.stanford.edu/projects/lfmicroscope/>
- Stanford New Lightfield Archive
  - <http://graphics.stanford.edu/data/LF/lfs.html>
    - e.g., “[http://graphics.stanford.edu/data/LF/chess\\_lf/preview.zip&zoom=1](http://graphics.stanford.edu/data/LF/chess_lf/preview.zip&zoom=1)”
  - Old: <http://graphics.stanford.edu/software/lightpack/lifs.html>



# Deep Learning Lightfields

- Learning-Based View Synthesis for Light Field Cameras
  - <https://www.youtube.com/watch?v=RCD2B5o1K8U>
- Light Field Video Capture Using a Learning-Based Hybrid Imaging System
  - <https://www.youtube.com/watch?v=TqVKcssYfAo>