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¹ 3D Reconstruction Enables High-Throughput Phenotyping and ² Quantitative Genetic Analysis of Phyllotaxy

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Abstract

Differences in canopy architecture play a role in determining both the light and water use 14 efficiency. Canopy architecture is determined by several component traits, including leaf length, 15 width, number, angle, and phyllotaxy. Phyllotaxy may be among the most difficult of the leaf 16 canopy traits to measure accurately across large numbers of individual plants. As a result, in 17 simulations of the leaf canopies of grain crops such as maize and sorghum, this trait is frequently 18 approximated as alternating 180° angles between sequential leaves. We explore the feasibility of 19 extracting direct measurements of the phyllotaxy of sequential leaves from 3D reconstructions 20 of individual sorghum plants generated from 2D calibrated images and test the assumption 21 of consistently alternating phyllotaxy across a diverse set of sorghum genotypes. Using a 22 voxel-carving-based approach, we generate 3D reconstructions from multiple calibrated 2D 23 images of 366 sorghum plants representing 236 sorghum genotypes from the sorghum association 24 panel. The correlation between automated and manual measurements of phyllotaxy is only 25 modestly lower than the correlation between manual measurements of phyllotaxy generated 26 by two different individuals. Automated phyllotaxy measurements exhibited a repeatability of 27 $R^2 = 0.41$ across imaging timepoints separated by a period of two days. A resampling based 28 genome wide association study (GWAS) identified several putative genetic associations with 29 lower-canopy phyllotaxy in sorghum. This study demonstrates the potential of 3D reconstruction 30 to enable both quantitative genetic investigation and breeding for phyllotaxy in sorghum and 31 other grain crops with similar plant architectures. 32

33 1 Introduction

Increases in crop productivity and water use efficiency are required due to increases in the world population and decreasing access to fresh water for agriculture [1]. In the past, increasing the tolerance of crops to high planting densities has improved crop productivity [2].

The increased tolerance of high planting densities in modern maize hybrids is explained at least 37 in part by a shift in the distribution of light throughout the canopy [2], a distribution determined by 38 plant canopy architecture. Photoinhibition in the upper canopy is decreased, and the photosynthetic 39 capabilities of the leaves in the lower canopy are more effectively utilized when light is distributed 40 more evenly throughout the canopy, increasing the overall radiation use efficiency of the crop [3]. 41 Furthermore, shifting a larger proportion of photosynthesis into the lower canopy reduces the water 42 loss via transpiration. Stomata lower in the canopy are less exposed to wind and thus have a stronger 43 boundary layer; the water concentration gradient driving transpiration is additionally decreased as a 44 consequence [4]. 45

Interest in optimizing crop canopy architecture has motivated the study of genes and genomic loci 46 determining variation in many of the individual components of canopy architecture, including the 47 vertical leaf angle [5-8], internode length [9-12], and plant height [13-16]., and it also contributes to 48 light distribution throughout plant canopies. Extreme phyllotaxic deviations and their inheritance 49 have long fascinated geneticists [17]. However, relative to other canopy architecture traits, phyllotaxy 50 has been subject to comparatively fewer quantitative genetic investigations. This absence may be 51 explained, at least in part, by the difficulty of collecting large numbers of accurate measurements 52 of phyllotaxy manually. As a result of the limited investigation of this trait, it has been unclear 53 how much, if any, quantitative genetic variation in phyllotaxy exists in grain crops relative to the 54 expectation of perfectly alternating -180° degree angles between sequential leaves – phyllotaxy for 55 these species. 56

On a developmental level, phyllotaxy (Figure 1) is initially determined by the spacing of the 57 newest leaf primordium, P0, in the shoot apical meristem (SAM), relative to the previous leaf 58 primordium. The first molecular markers of the development of a new leaf primordium are an 59 auxin maximum around the point of the new leaf primordium formed by PIN1 convergence and a 60 subsequent down-regulation of KNOTTED-LIKE HOMEOBOX (KNOX) genes [19]. However, the 61 final orientation of mature leaves appears to also be under a degree of environmental control. A range 62 of environmental factors influence the orientation of leaves in maize, including wind, planting density, 63 seed orientation, and water stress [20–25]. Some, but not all, maize genotypes have also exhibited 64 the ability to reorient the axis of their leaves to avoid overlaps between neighboring plants [21, 25, 65 26]. Specific genes and genomic loci governing variation in this capacity have been mapped via 66 GWAS [25]. However, this reorientation typically shifts the orientation of leaves on both sides of 67 the plant reciprocally rather than modifying the alternating pattern of phyllotaxy that is typically 68 exhibited by maize and other related plant species. Genetic variation and control of mean phyllotaxy 69 has not been evaluated in depth via quantitative genetic methods, although several large effect single 70 gene mutations that alter phyllotaxy have been characterized in maize [27, 28]. 71

Perhaps the best-known of these phyllotaxy mutants is the recessive *abphyl1* mutant in maize,



Figure 1: Phyllotaxy is the arrangement of the leaves around the stem in the plane. Created in Biorender.com [18]. A) The top view of a sorghum plant exhibiting the expected alternating phyllotaxy with 180° angles between each pair of sequential leaves. B) The top view of a sorghum plant exhibits deviations from the expected phyllotaxic angles. Note that the angle captured will vary depending on the side of the plant measured. The two possible angles measured for a given pair of sequential leaves are conjugate to each other, *e.g.*, their sum is equal to 360°. C) The side view of a sorghum plant and two examples of the phyllotaxic angle φ in the plane.

described by Jackson and Hake in 1999 [27]. This mutant typically exhibits an opposite phyllotaxy 73 wherein one node produces two leaf blades with the midribs separated by approximately 180° , with 74 occasional switches to the wild-type pattern of alternate phyllotaxy occurring partway through 75 growth following an intermediate transition node wherein two leaf blades adjacent to one another 76 are partially fused [27]. The authors also describe alternate phenotypes of the mutant wherein the 77 shoot splits into two shoots with alternate phyllotaxy or a dwarfed plant with what appeared to 78 resemble spiral phyllotaxy. Giulini et al. [29] cloned the gene underlying this mutant and found 79 it a cytokinin-inducible response regulator controlling SAM size. The described opposite or spiral 80 phenotypes of the *abphyl1* mutant in comparison to the wild-type alternate phyllotaxy may predispose 81 us to conclude that phyllotaxy only varies qualitatively, but not quantitatively. 82

Previous methods of quantitatively measuring phyllotaxy can largely be divided into purely manual methods, top down imaging based methods, and approaches based on 3D reconstruction (Figure 1A). Protocols for manual measurements include the use of a circular protractor to measure

the change in angle between sequential leaves [30], using a compass aligned with leaf midribs to 86 measure the angle of each leaf with respect to magnetic north [22], a wooden panel marked with 87 angles [21, 26, 31], or simple visual assessment of the angle of individual leaves relative to the axis 88 of planting [24, 32]. These approaches tend to be relatively low throughput, with measurements 89 collected from dozens to hundreds of plants representing less than ten genotypes per experiment. 90 Top down imaging, whether from a UAV or from an elevated ground based camera, can increase the 91 throughput of phyllotaxy measurements [23, 25, 32, 33]. Estimates of phyllotaxy can be obtained 92 from these top-down images through a range of approaches including manual scoring [23, 25], fitting 93 bounding boxes to individual leaves [33] or detecting the positions of midribs [32]. These methods 94 are limited to measurements of the azimuth angle in the upper canopy, which is the deviation of 95 the leaves from the row line (direction of planting). Other studies utilize electromagnetic 3D plant 96 digitizers to reconstruct the plant in silico [30, 34]. While these methods offer precise measurements 97 throughout the canopy, they are relatively low-throughput, as each plant required approximately 20 98 minutes of labor [32]. Daviet et al. [35] utilize skeletonized 3D reconstructions of maize to measure 99 the azimuth angle, in a method similar to the one presented here, but do not evaluate the efficacy of 100 the method for the measurement of phyllotaxy. 101

We use 3D reconstructions of sorghum plants from a diversity panel [36] to enable high-throughput phenotyping of phyllotaxy in the lower canopy and identify genetic markers associated with this trait. We identify heritable variation in sorghum phyllotaxy as well as three genetic markers associated with the median phyllotaxic angle in the lower 5 leaves. Application of this method to larger populations with additional replication will likely increase the number of marker trait associations for phyllotaxy in sorghum, providing a basis for both functional characterization of candidate genes and marker assisted selection.

¹⁰⁹ 2 Materials and Methods

Figure 2 shows an overview of the workflow employed in this study. We describe each step in more 110 detail below, but briefly: photos were taken from six different views (five side views and one top 111 view) of 366 plants at three timepoints. The images were used as input to a 3D voxel carving 112 algorithm described in [37]. The 3D voxels were skeletonized and segmented into the stem and leaves. 113 Leaf angles are extracted by measuring the principal directions of the stem and leaves. We then 114 normalized the angles, transforming them into the same coordinate system, and determined the 115 angle difference in the xy-plane between successive leaves to estimate phyllotaxy. These values were 116 then used to estimate the heritability of automated phyllotaxy measurements and conduct a GWAS 117 analysis. Below, we describe each step in detail. 118

¹¹⁹ 2.1 Plant growth conditions, image acquisition, and manual measurements

A total of 366 sorghum plants, representing 236 genotypes from the sorghum association panel [36] with partial replication (40 replicated genotypes), were grown at the automated phenotyping facility of the University of Nebraska-Lincoln and imaged on April 11th, April 13th, and April 16th, 2018



Figure 2: An overview of the workflow used in this paper and examples of output from each stage.

(47, 49, and 52 days after planting, respectively). The growth and imaging protocols were followed as 123 described in Tross et al. [5]. In 2023, an additional set of 10 sorghum plants were grown at the same 124 facility and imaged on February 1, 2023, 76 days after planting. In 2024, a third set of 10 sorghum 125 plants was grown at the same facility and manually measured and imaged on March 5, 2024, 47 days 126 after planting. Between 2018 and 2023, the RGB camera used at the facility was upgraded from 127 a Basler pia2400-17gc camera equipped with a c6z1218m3-5 Pentax TV zoom lens to a Prosilica 128 GT6600 camera to improve resolution (from $2,454 \times 2,056$ pixels to $4,384 \times 6,576$ pixels) and image 129 quality. 130

Manual phyllotaxy measurements were conducted by using the Compass application on either an 131 iPhone 13 Pro Max or iPhone 14 [38] to measure the direction of each measured leaf. Differences 132 between sequential leaves were calculated as was done for the automated phyllotaxy measurements. 133 The left edge of the long side of the iPhone was aligned with the midrib of each leaf of interest and 134 the phone was rotated along the z-axis (Figure 1C) until the short side of the screen was flush to the 135 stem. This process was performed for each collared leaf on each plant of interest. Measurements of 136 individual plants were repeated independently by two members of the research team to quantify the 137 repeatability of manual phyllotaxy measurements. 138

¹³⁹ 2.2 Phyllotaxy measurement from 3D skeletons

3D reconstructions of sorghum plants from 2D calibrated images were derived using methods described 140 in Gaillard et al. [37, 39], and Tross et al. [5]. The images collected in 2018 were taken from five 141 side views collected at equidistant angles $(0^{\circ}, 72^{\circ}, 144^{\circ}, 216^{\circ}, 288^{\circ})$ around the plant. In 2023 and 142 2024, side view images were collected at 10 equidistant side views $(0^{\circ}, 36^{\circ}, 72^{\circ}, 90^{\circ}, 108^{\circ}, 144^{\circ}, 216^{\circ}, 108^{\circ}, 1$ 143 252°, 288°, 324°). The images were calibrated to correct for potential misalignment between the 144 pots and the turntable's axis of rotation, as well as the camera's optical center with the rotation 145 axis. The calibrated images were then processed using a voxel carving algorithm producing a 512^3 146 voxel resolution representation of the sorghum plant [37]. A skeletonization algorithm was applied 147 to this voxel representation of the sorghum plant, iteratively removing voxels from the plant until 148 only the skeleton structure remained. To eliminate any gaps in the skeleton caused by disconnected 149

¹⁵⁰ components, a joining process was implemented as part of the skeletonization process [39].

A Support Vector Machine (SVM) classifier [40] was employed to identify and discard portions of 151 the skeleton that did not correspond to actual plant organs, for instance, spurious branches present 152 from noise in the data. Post-processing techniques were used to classify voxels as either leaf or stem 153 by computing paths from the ground to the leaves and labeling a voxel as part of the stem if it 154 belonged to more than two paths. The separated leaves were then assigned numerical labels based 155 on the attachment height to the stem within the skeleton structure. Using Principal Component 156 Analysis (PCA), the stem voxels' first and second principal axes were computed. Additionally, PCA 157 was used to extract the principal axes for the first 20 voxels (about 6 cm) of each leaf, starting from 158 the junction of the leaf with the stem. By using these two coordinate frames, the angles $0^{\circ} \leq \theta < 180^{\circ}$ 159 and $0^{\circ} \leq \phi \leq 360^{\circ}$ of each leaf were calculated in the stem coordinate frame, given by the PCA 160 principal directions 3. 161



Figure 3: Rendering of a 3D reconstructed plant from the validation dataset, with the principal directions of the stem and leaves marked. The green wireframe shows the hull of the 3D reconstructed plant, and the solid blue lines show the principal directions of the stem and leaves of the plant. The supplemental material associated with this manuscript contains video animations showing the 3D reconstructions and leaves' principal directions for each of the ten plants grown in 2023. We highly recommend the reader to watch the video animations to get a better sense of the angles in 3D.

Accuracy and topology correctness were assessed as described in detail in Gaillard et al. [37, 39]. 162 In brief, the accuracy scores were determined using the Dice coefficient based on the proportion 163 of plant pixels in the 2D images represented by re-projected voxels in the 3D reconstruction. A 164 topology was considered to be incorrect if the final plant skeleton did not exhibit a tree topology. 165 Reconstructions with an accuracy score below 0.70 or an incorrect topology were removed from the 166 dataset. Reconstructions containing only one ϕ value (i.e., only one leaf was identified in the skeleton) 167 were also removed from downstream analyses as phyllotaxy relies on the angle between two leaves. 168 This filtering criteria resulted in the exclusion of 115 reconstructions. Next, the differences between 169 sequential leaves' ϕ values were represented as $\varphi_i = \phi_{i+1} - \phi_i$. Each φ value was then normalized to 170 a range of $\varphi \in [0^\circ, 360^\circ)$ by applying the modulo of 360. 171

172 2.3 Method reliability measures and validation

173 2.3.1 Reliability of 3D-reconstruction and manual measurements

The lower five φ values generated for a plant from the 3D reconstructions were compared pair-wise between the three days of imaging (April 11th, April 13th, and April 16th, 2018) to estimate the reliability of 3D-reconstruction measurements of phyllotaxy. As it is rare for a healthy sorghum plant to have an angle less than a right angle and angles less than 90° could result from a leaf being missed during reconstruction or skeletonization, φ values less than 90° degrees or greater than 270° were removed.

There is no inherent structural difference between a phyllotaxy leaf angle of 160° or 200° with 180 which of these two angles is reported by our method depending solely on the side of the plant 181 measurement begins upon. To remove the arbitrary effect of side of the plant in comparisons between 182 different measurements, we first determined if measurement began on the same side of the plant 183 for both sets of measurements being compared. If the Pearson correlation coefficient on a per-plant 184 basis was greater than or equal to zero, measurement began on the same side of the plant in both 185 sets of measurements, and no transformation was applied to either set of measurements for that 186 plant. In the cases where measurement began on different sides of the plant between the two sets of 187 measurements for a given plant, we transformed the angles for this plant in one set of measurements 188 (shown on the y-axes of plots in Figures 4 and S1) using: 189

$$\varphi_{i,Conjugate} = 360 - \varphi_i. \tag{1}$$

¹⁹⁰ On a per-plant basis, this produces the same absolute value for the correlation between the two sets ¹⁹¹ of measurements.

¹⁹² 2.3.2 Comparison of 3D-reconstructions with manual measurements

The initial step of our voxel-carving and 3D reconstruction pipeline was segmentation of 2D input 193 images into plant and non-plant pixels. For the 2018 images this step was performed using a 194 convolutional neural network [37] trained specifically on manual annotations of the 2018 image 195 dataset. For the 2023 and 2024 images taken with a different and higher resolution camera, we 196 retrained a neural network with the same published architecture using 18 images collected from three 197 plants imaged in 2023 and manually segmented using Paintbrush 2.6 [41] as well as an additional 198 67 images which were initially segmented using the older model trained on images from 2018 and 199 then manually corrected and updated by human annotators. The segmented images output by the 200 re-trained neural network were then used to reconstruct the sorghum plants. As the neural network 201 was re-trained with images from the new camera, the reconstructions were visually checked. All 202 360° -normalized φ_i were obtained for the manual and 3D reconstruction measurements. 203

204 2.4 Quantitative genetic analyses

For the purposes of quantitative genetic analysis, phyllotaxy values were transformed into the 205 absolute difference between observed angle between two leaves and the expected angle for perfectly 206 alternating phyllotaxy (180°): Φ , denoted as $\Phi_i = |\varphi_i - 180^\circ|$. Due to previous evidence [5] that 207 heritability of measurements from the 3D reconstructions decreased at higher leaves due to movement 208 of the upper canopy during rotation in the imaging process, we limited our analysis to the lower 209 four phyllotaxic angles from five leaves. The 2D images of plants with a median Φ_i value greater 210 than 1.5 times the interquartile range $(136.1 - 167.0^{\circ})$ for one of the first 4 phyllotaxic angles were 211 visually examined to determine if these images supported the extreme phyllotaxic values. In 55% of 212 cases, the images could not definitively support the extreme phyllotaxic angles. Because it is rare 213 for a healthy sorghum plant to have an angle less than a right angle and we could not verify the 214 majority of extreme phyllotaxic angles visually examined, $\Phi_i > 90$ were removed from downstream 215 analyses. As lower-canopy phyllotaxy had not been extensively studied in previous literature, we 216 evaluated 25 quantitative summaries of lower-canopy phyllotaxy to summarize across the three 217 timepoints and/or multiple phyllotaxic angles, detailed in Supplementary Table 1. In aggregate, the 218 criteria for reconstruction accuracy, skeleton topology, and Φ_i value resulted in the exclusion of 52 219 sorghum plants, leaving a total of 314 plants representing 223 unique genotypes for downstream 220 quantitative genetic analyses. Data analysis and data visualization was conducted using R 4.2.2 [42] 221 using the libraries lme4 [43], tidyverse [44], readxl [45], cowplot [46], MoMAColors [47], BiocIO [48], 222 GenomicRanges [49], Gviz [50], ggrepel [51], scales [52], viridis [53], stringi [54], and car [55]. 223

224 2.4.1 Heritability

²²⁵ The linear model

$$Y = \mu + \delta_i + \varepsilon_{i,j},\tag{2}$$

was fit using the R package lme4 [43], where Y is the response variable, μ is the overall mean, δ_i is the random effect of the *i*th genotype, and $\varepsilon_{i,j}$ is the residual error for the *j*th plant of the *i*th genotype. Variance components were then extracted, and broad sense heritability was calculated as

$$H = \frac{\sigma_G^2}{\sigma_G^2 + \frac{1}{n}\sigma_R^2},\tag{3}$$

where σ_G^2 is the genotypic variance and σ_R^2 is the residual variance and n = 2, the minimum number of replications per genotype. When there were more than 2 replications per genotype, all replicates were used in the estimation except in the case of the reference genotype PI656058, which was replicated 8 times, 2 more than any other genotype. 2 random replications of PI656058 were used in the estimation.

234 2.4.2 GWAS

Genome-wide association studies reported here were conducted for the 13 quantitative summaries of phyllotaxy with a broad-sense heritability ≥ 0.20 from 218 sorghum varieties which were phenotyped

as part of this study, passed the quality control steps described above, and were present in a set of 237 4,693,810 genetic markers scored for the same population via whole genome resequencing. Five of the 238 223 genotypes that passed the quality control steps described above were not present in the larger 239 set of genetic markers called for the sorghum association panel [56] aligned to the Sorghum bicolor 240 v3.1.1 reference genome [57] which was filtered to generate the genetic marker set used in this study. 241 These five genotypes were excluded from the GWAS. The marker set from Boatwright et al. [56] was 242 filtered to exclude those markers which were not biallelic, indels, or missing in > 30%, heterozygous 243 in > 10%, or with a minor allele frequency <5% of the 218 genotypes present in both the phenotype 244 and genotype data using VCFtools v0.1.16 [58] and BCFtools 1.17 [59]. The number of effective 245 markers was estimated to be 1,088,251.19 using GEC v0.2 [60]. The dataset was analyzed one 246 hundred times using the FarmCPU algorithm as implemented in rMVP v1.0.6 [61], with a threshold 247 of 0.21 for iteration in the FarmCPU algorithm, corresponding to approximately 0.05 divided by the 248 ratio of estimated effective markers to total markers. In each interation, 10% of phenotypic records 249 were randomly masked and genetic markers with a p-value of less than 4.59×10^{-8} , corresponding 250 to a Bonferroni corrected p-value of 0.05 applied to the estimated effective independent genetic 251 markers, were considered to be significantly associated with the phenotype. For each marker which 252 exceeded this threshold in at least one of the one hundred iterations, a resampling model inclusion 253 probability (RMIP) was calculated based on the number of interations in which the marker exceeded 254 the significance threshold divided by the total number of interations. Markers that exceeded an 255 RMIP of 0.1 were considered of greatest interest for downstream analysis. Linkage disequilibrium 256 estimates within a chromosome were estimated using plink v1.90 [62]. 257

258 **3** Results

²⁵⁹ 3.1 Reliability of automated 3D phyllotaxy measurements

Measuring each leaf angle for a single plant took one person between ten and twenty minutes to 260 complete. After removing extreme values and transforming conjugate angles as described in , the 261 correlation of ground truth measurements of phyllotaxy between different individuals measuring the 262 same pairs of leaves on the same plants was $R^2 = 0.55$ (n = 46 angles), based on data from five 263 pairs of leaves per plant measured on ten plants by two individuals (Figure 4A). This was modestly 264 higher than the correlation between measurements of the first five pairs of leaves generated from 3D 265 reconstructed plants imaged at two time points separated by two days $(R^2 = 0.41, n = 961 \text{ angles},$ 266 Figure 4B) after applying the same filtering criteria and transformations to the data. When the 267 same comparison was made between automated measurements of phyllotaxy generated using images 268 collected either three days apart or five days apart, the correlation between measurements declined 269 to $R^2 = 0.33$ and $R^2 = 0.24$, respectively (Figure 4B, Supplementary Figure 1). We also found a 270 moderate correlation ($R^2 = 0.48$, n = 75 angles, Figure 4C) between 3D reconstruction measurements 271 and manual measurements when comparing across the combined set of manual measurements taken 272 by Individual 1 and Individual 2 and the corresponding conjugate angles from the reconstructions. 273



Figure 4: Both manual and reconstruction-based methods generate moderately repeatable measurements of phyllotaxic angles in the lower canopy. A) Correlation between manual measurements of lower five phyllotaxic angles (φ) for ten plants by two different people after removing φ values less than 90° or greater than 270°, with $R^2 = 0.55$. B) Correlation of lower five φ values measured by 3D reconstructions of the sorghum plants when imaged on April 11, 2018 (Timepoint 1) and April 13, 2018 (Timepoint 2) after removing φ values less than 90° or greater than 270°, with $R^2 = 0.41$. In cases when the measurements for a single plant were negatively correlated between the two days, the values from the Timepoint 2 reconstruction measurements of lower five φ values after removing φ values less than 90° or greater than 270°, with $R^2 = 0.48$. In cases where the 3D reconstruction and manual measurements were negatively correlated for a single plant, the 3D reconstruction measurements were transformed to their conjugate angles.

²⁷⁴ 3.2 Variation in sorghum phyllotaxy

An initial assessment of phyllotaxy in 336 plants (236 genotypes) of the sorghum association panel 275 using the 3D reconstruction method described above identified plants with deviations from the 276 expectation of perfectly alternating phyllotaxy between the second and third extant leaves in sorghum 277 plants ranging from $\Phi_2 = 1.05^{\circ}$ (nearly perfectly alternating phyllotaxy between leaves 2 and 3, 278 Figure 5A, D) to $\Phi_2 = 170.4^{\circ}$ (leaves 2 and 3 emerging one on top of the other, Figure 5C, F). 279 Absolute variations from the expected angle of 180° in the lower 4 phyllotaxic angles across all plants 280 and all timepoints ranged from $\Phi_i = 0.01^\circ$ to $\Phi_i = 179.97$ (Figure 5G). In some cases, extreme 281 phyllotaxy values could be validated by manual examination of the source images (Figure 5B, C, E, 282 F). However, in 55% of cases visually examined, manual examination of source images for sorghum 283 plants that deviated from the expected phyllotaxy by $>90^{\circ}$ could not definitively support these 284 extreme values. In some cases, specific issues were identified to which the incorrect measurements 285 could be attributed including the presence of one or more tillers, fallen plants, or leaves senescing in 286 an unexpected order (Supplemental Figure 2), as well as errors in the ordering of leaves. Given the 287 difficulty even trained subject matter experts experienced in accurately assessing phyllotaxy from 2D 288 images and the high rate of errors among manually checked phyllotaxy angles in the $>90^{\circ}$ bin, the 289 decision was made to exclude these values from downstream analysis. 290



Figure 5: Variation of phyllotaxic angles among sorghum plants of different genotypes. **A-F)** Side (A-C) and top (D-F) views of three sorghum plants with minimal (A, D, PI533866), moderate (B, E, PI533852), and extreme (C, F, PI533915) levels of deviation from the expected value of 180° for Φ_2 .**G)** The distributions of median Φ_{1-4} values before (gold, 366 plants) and after removing extreme values (blue, 308 plants).

²⁹¹ 3.3 Quantitative genetic analysis

As we had measurements for multiple phyllotaxic angles in the lower canopy per plant across the 292 three timepoints, we evaluated 25 quantitative metrics of lower canopy phyllotaxy to summarise 293 across multiple timepoints and/or angles after removing extreme values, which are described in 294 Supplemental Table 1. Thirteen of 25 quantitative metrics were estimated to have broad-sense 295 heritabilities greater than or equal to 0.2 (Supplemental Table 1). We detected stable (RMIP > 0.1) 296 marker-trait associations for 7 of these 13 quantitative summaries of lower canopy phyllotaxy via 297 GWAS (Figure 6, Supplementary Table 1, Supplementary Figure 3). Six of the seven markers which 298 exceeded an RMIP of 0.1 for at least one trait were also identified across four or more total traits 200 when the RMIP threshold was reduced to 0.02. These six genetic markers and their associated traits 300 are detailed in Supplementary Table 2. The repeated signals associated with the same markers 301 indicate that multiple phyllotaxy summary metrics capture similar information content about the 302 properties of the lower canopy in sorghum. 303

The marker-trait association with the highest stability was identified for the median Φ_{1-4} value 304 with the genetic marker Chr05:12,109,370 (RMIP= 0.26, Figure 6). This trait captures the median 305 phyllotaxic angle measured in the lower four phyllotaxic angles across all three timepoints for a 306 plant, and had a relatively normal phenotypic distribution (Figure 6A). Two additional markers, 307 Chr05:65,733,791 and Chr06:41,390,777, were also identified to have stable associations with this 308 trait (RMIP=0.19, 0.11, respectively; Figure 6B). Genotypes carrying the minor allele at each of 309 these sites have significantly higher (p < 0.05) median deviations from the expected phyllotaxic 310 angle of 180° than genotypes carrying the major allele at the same site (Figure 6C–E). Figure 6F– 311 G shows the annotated gene models within 100 kb of the identified genetic markers in order of 312 descending RMIP, and all annotated gene models within this region and their functional annotations 313 are described in Supplementary Table 3. The nearest gene model to the first genetic marker on 314 chromosome 5, Sobic.005G086700, which encodes a zinc finger transcription factor, is located 24.5 kb 315 from the trait associated marker. Linkage disequilibrium (LD) decays quickly in this region, with 316 the maximum LD between the identified genetic marker and genetic markers within the nearest 317 gene model being $R^2 = 0.18$. Within 100kb of this trait associated marker, there is also a gene 318 encoding an O-methyltransferase (Sobic.005G086600) and three gene models with no functional 319 annotation. The second trait associated marker on chromosome 5 is located in the tyrosine kinase 320 related to salt stress and antifungal responses. The trait associated marker on chromosome 6 is in 321 LD $(R^2 > 0.6)$ with genetic markers in two gene models, Sobic.006G061000 and Sobic.006G061100 322 (Figure 6G). The closer of these two, Sobic.006G061100 located 18.8 kb from the GWAS hit, encodes 323 an AMP-activated protein kinase. The second encodes a protein belonging to the pentatricopeptide 324 repeat (PPR) family. 325

326 4 Discussion

We present a high-throughput method of measuring phyllotaxy in the lower canopy that achieves 327 near-human repeatability. The imaging process for each plant requires little human intervention 328 and can be completed in approximately 2 minutes, and the reconstruction and skeletonization steps 329 each run in less than one minute, making it far more high-throughput than the manual method we 330 employed which requires 10 - 20 minutes per plant to produce data with comparable repeatability. 331 The more rapid methodology enables application to a large panel of plants. Daviet et al. [35] used 332 a similar technique as presented here of reconstruction and skeletonization and show its ability to 333 measure the azimuth positions of maize leaves. However, this method requires additional data for 334 camera calibration [63], and they do not extend their study to characterize the position of subsequent 335 leaves relative to each other, a key factor in the process of leaf initiation, nor do they perform 336 quantitative genetic studies to illuminate potential genetic mechanisms of this under-studied trait. 337 We evaluate the reliability of the method we present here and find it moderately stable ($R^2 = 0.41$ 338 for the same plants imaged on different days) after removing extreme values. This is modestly less 330 repeatable than manual measurements ($R^2=0.55$ for the same plants measured by different people). 340 It is possible that a portion of the residual value in correlations of phyllotaxy measurements collected 341 at different time points is associated with subtle changes in plant growth or the senescence of leaves, as 342

the repeatability of automated phyllotaxy measurements decreases when comparing images collected with larger time intervals (see Supplementary Figure 1). We detect genetically repeatable variation in the lower 4 phyllotaxic angles of the canopy that is to some degree, robust to the specific summary metric used to summarise across timepoints and/or multiple angles. Thirteen of the 25 summary metrics were estimated to have broad-sense heritabilities greater than 0.20 (Supplementary Table 1). Several of these measures of lower-canopy phyllotaxy utilize information from multiple angles, while others include information only from a single angle across timepoints.

While the method we present here represents a large step forward in the ability to illuminate 350 the genetic basis for phyllotaxy in sorghum, it is not without its limitations. First, Secondly, the 351 method has the highest accuracy in the lower canopy due to occlusion of the point of attachment by 352 other leaves in the middle and upper canopy or significant movement of the upper plant during the 353 imaging process, which makes accurate reconstruction difficult. While phyllotaxy in the upper canopy 354 can be estimated using methods similar to He et al. [33], the middle canopy remains a challenge to 355 measure, and evidence exists that different levels of the canopy have different genetic determinants 356 of architecture [5, 6]. Third, the method discussed here, and may generate extreme values when 357 tillers are present (Supplementary Figure 2) Fourth, the method is highly dependent on camera 358 calibrations and high-quality image segmentations to train and improve the convolutional neural 359 network to segment the RGB images that serve as input to the pipeline for this method. Fourth, 360 this initial study was done using a relatively small population (218 genotypes) for association studies, 361 limiting the statistical power available to detect genes controlling the trait of interest while sufficiently 362 controlling for false positives. 363

Despite the limited statistical power provided by the small population employed, we identified 364 marker-trait associations a total of 14 significant GWAS signals representing 7 unique markers linked 365 to variation in one or more phyllotaxy summary metrics at $RMIP \ge 0.1$ (Figure 6, Supplementary 366 Figure 3, Supplementary Table 1). Further examination of the marker-trait associations detected for 367 the median Φ_{1-4} value, which had the most strongly supported marker trait association (RMIP= 0.26) 368 showed that the genotypes with the minor allele at any of these sites have significantly higher median 369 Φ_{1-4} values than genotypes with the major allele, indicating greater deviations from the expected 370 alternating phyllotaxy of sorghum (Figure 6C–E). As rare alleles tend to be deleterious [64], this may 371 indicate that deviations from alternating phyllotaxy are detrimental to overall fitness. The genomic 372 regions surrounding the genetic markers associated with the median Φ_{1-4} value include several 373 transcription factors, osmotic stress response genes, protein kinases, and calcium binding proteins, as 374 well as several gene models with no functional annotations (Supplementary Figure 3). In the future, 375 the method we present here could be employed to score phyllotaxy in larger association panels, such 376 as the Sorghum Diversity Panel (SbDiv) [65] and/or to score more replicated plants per genotype, 377 both of which should improve our statistical power to identify specific genomic intervals associated 378 with variation in phyllotaxy. As maize and sorghum share highly similar plant architectures prior to 379 the reproductive stage, we anticipate our method should also be applicable to this crop without the 380 need for extensive modification or fine tuning. We demonstrate the feasibility of high-throughput 381 measurements of lower-canopy phyllotaxy, enabling quantitative genetic analysis to improve our 382 understanding of its genetic control. 383

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³⁹¹ Declaration of competing interest

James C. Schnable has equity interests in Data2Bio, LLC and Dryland Genetics LLC and has performed paid work for Alphabet. The authors declare no other conflicts of interest.

³⁹⁴ Data Availability

³⁹⁵ The code for reconstruction and skeletonization is available at GitHub: https://github.com/ ³⁹⁶ cropsinsilico/SorghumVoxelCarving

The raw images analyzed in this study are available at Zenodo: Mathieu Gaillard, Chenyong Miao, James C. Schnable, & Bedrich Benes. (2021). Voxel Carving Based 3D Reconstruction of Sorghum [Data set]. Zenodo. https://doi.org/10.5281/zenodo.4426620.

The phenotypic data, GWAS result files and code for main figures and analysis are available at Github: https://github.com/jdavis-132/phyllotaxy.git

402 CRediT authorship contribution statement

Jensina M. Davis: Conceptualization, Formal analysis, Investigation, Data Curation, Writing Original Draft, Visualization Mathieu Gaillard: Methodology, Software, Investigation. Michael C.
Tross: Methodology. Nikee Shrestha: Validation, Investigation, Data Curation. Ian Ostermann:
Methodology, Software, Investigation. Ryleigh J. Grove: Validation, Data Curation. Bosheng
Li: Methodology, Software, Investigation. Bedrich Benes: Conceptualization, Resources, Writing
- Review & Editing, Supervision, Funding acquisition. James C. Schnable: Conceptualization,
Resources, Writing - Review & Editing, Supervision, Funding acquisition.

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563 Supplementary Materials

⁵⁶⁴ Supplementary File 1. Videos of reconstructed plants grown in 2023. https://github.com/

 ${\tt jdavis-132/phyllotaxy/blob/f02e6b9ed52723510a78490d34153699266837c5/SupplementalVideos-Phyllotaxy.}$

```
566 zip
```

Summary of	Description	Broad-	Number
phyllotaxy		sense	genetic
r J the J		heritabil-	markers
		itv	with
		0	RMIP
			≥ 0.1
Median of Φ_{1-4}	Median of lower 4 phyllotaxic angles	0.25	3
Mean of Φ_{1-4}	Mean of lower 4 phyllotaxic angles	0.30	5
Mean of Median	Mean of the medians of each of the lower 4	0.27	2
Φ_{1-4}	phyllotaxic angles		
Median of Φ_{1-3}	Median of lower 4 phyllotaxic angles	0.27	1
Median of Φ_2	Median of the second phyllotaxic angle	0.34	1
Mean of Φ_2	Mean of the second phyllotaxic angle	0.34	1
Median of Φ_3	Median of the third phyllotaxic angle	0.32	1
Mean of Φ_{1-3}	Mean of the lower 3 phyllotaxic angles	0.30	0
Mean of Φ_3	Mean of the third phyllotaxic angle	0.24	0
Mean of Median	Mean of the medians of each of the lower 3	0.28	0
Φ_{1-3}	phyllotaxic angles		
Mean of Mean Φ_{1-3}	Mean of the means of each of the lower 3	0.28	0
	phyllotaxic angles		
Mean of Mean Φ_{1-4}	Mean of the means of each of the lower 4	0.33	0
	phyllotaxic angles		
Mean GLM BLUE	Mean of fitted values for lower 4 phyllotaxic	0.28	0
Fitted Φ_{1-4}	angles from GLM BLUE model		
Mean of Means	Mean of the means of each of the lower 2	0.16	
Φ_{1-2}	phyllotaxic angles		
Mean of Φ_{1-2}	Mean of first 2 phyllotaxic angles	0.15	
Mean of Medians	Mean of the medians of each of the lower 2	0.14	
Φ_{1-2}	phyllotaxic angles		
Median of Means	Median of the means of each of the lower 4	0.05	
Φ_{1-4}	phyllotaxic angles		
Median of Φ_1	Median of first phyllotaxic angle	0.03	

Supplementary Table 1: Multiple quantitative summaries of phyllotaxy captured heritable variation.

Summary of	Description	Broad-	Number
phyllotaxy		sense	genetic
		heritabil-	markers
		ity	with
			RMIP
			≥ 0.10
Median of Means	Median of the means of each of the lower 3	0.02	
Φ_{1-3}	phyllotaxic angles		
Median of Φ_4	Median of fourth phyllotaxic angle	0.00	
Mean of Φ_1	Mean of first phyllotaxic angle	0.00	
Mean of Φ_4	Mean of fourth phyllotaxic angle	0.00	
Median of Medians	Median of the medians of each of the lower 3	0.00	
Φ_{1-3}	phyllotaxic angles		
Median of Medians	Median of the medians of each of the lower 4	0.00	
Φ_{1-4}	phyllotaxic angles		
Median of Means	Median of the means of each of the lower 2	0.00	
Φ_{1-2}	phyllotaxic angles		

Chromosome	Position	Traits with RMIP ≥ 0.10	Traits with RMIP ≥ 0.02	Maximum RMIP
Chr05	12109370	Median of Φ_{1-4} , Mean of Φ_{1-4} , Mean of Medians Φ_{1-4}	Mean of Means Φ_{1-4} , Mean of GLM BLUE Fitted Φ_{1-4}	0.26
Chr05	65733791	Median of Φ_{1-4} , Mean of Φ_{1-4} , Mean of Medians Φ_{1-4}	Mean of Means Φ_{1-4} , Mean of GLM BLUE Fitted Φ_{1-4}	0.19
Chr03	56520108	Median of Φ_2 , Mean of Φ_2		0.12
Chr06	41390777	Median of Φ_{1-4} , Median of Φ_{1-3} , Median of Φ_3	Mean of Φ_{1-4} , Mean of Φ_{1-3} , Mean of Φ_3 , Mean of Medians Φ_{1-3} , Mean of GLM BLUE Fitted Φ_1	0.11
Chr05	5060741	Mean of Φ_{1-4}	Median of Φ_{1-4} , Median of Φ_{1-3} , Mean of Φ_{1-3} , Mean of Φ_3 , Median of Φ_3 , Mean of Means Φ_{1-4} , Mean of GLM BLUE Fitted Φ_{1-4}	0.10
Chr02	38310584	Mean of Φ_{1-4}	Median of Φ_{1-3} , Median of Φ_3 , Mean of Φ_2 , Mean of GLM BLUE Fitted Φ_{1-4}	0.10
Chr02	53403506	Mean of Φ_{1-4}	Median of Φ_{1-3} , Mean of Means Φ_{1-4} , Mean of GLM BLUE Fitted Φ_{1-4}	0.10

Supplementary Table 2: Six genetic markers identified to have a stable association with one trait were sometimes identified to have associations with other traits.

Gene model	Genetic marker	Distance from genetic marker (kb)	LD (R^2)	Functional annotation
Sobic.005G086600	Chr05:12,109,370	76.6	0.01 -	O-methyltransferase
	, ,		0.06	v
Sobic.005G086650	Chr05:12,109,370	55.6	0.00 -	None available
			0.11	
Sobic.005G086700	Chr05:12,109,370	24.5	0.01 -	Zinc finger transcription factor
			0.18	
Sobic.005G086801	Chr05:12,109,370	51.1	0.00 -	None available
			0.11	
Sobic.005G086900	Chr05:12,109,370	64.9	0.07 -	None available
			0.09	
Sobic.005G175200	Chr05:65,733,791	46.5	0.01 -	Serine/threenine protein kinase
			0.01	
Sobic.005G175300	Chr05:65,733,791	33.6	0.00 -	None available
			0.38	
Sobic.005G175400	Chr05:65,733,791	16.4	0.00 -	None available
			0.69	
Sobic.005G175500	Chr05:65,733,791	0.0	0.00 -	Protein tyrosine kinase related to
			1.00	salt stress/antifungal response
Sobic.005G175600	Chr05:65,733,791	4.3	0.00 -	Protein tyrosine kinase related to
			0.00	salt stress/antifungal response
Sobic.005G175700	Chr05:65,733,791	18.1	0.01 -	Ubiquitin-activating enzyme E1
			0.45	
Sobic.005G175800	Chr05:65,733,791	22.6	0.02 -	Calcium binding protein
			0.18	CML30-related
Sobic.005G175900	Chr05:65,733,791	26.9	0.01 -	None available
~	6 / 4		0.45	
Sobic.005G176000	Chr05:65,733,791	37.8	0.00 -	Membrane-associated zinc finger
		4 - 0	0.43	protein
Sobic.005G176100	Chr05:65,733,791	47.2	0.01 -	Mannose-6-phosphate isomerase
			0.11	.
Sobic.005G176300	Chr05:65,733,791	82.3	0.01 - 0.02	Leucine-rich repeat-containing
G 1: 000G001000	C1 00 11 000 555	22.4	0.22	protein
Sobic.006G061000	Chr06:41,390,777	32.4	0.68 -	PPR repeat family
G 1: 000C0001100	C1 06 41 900 FFF	10.0	0.76	
Sobic.006G061100	Chr06:41,390,777	18.8	0.61 - 0.71	AMP-activated protein kinase
G 1: 000G0001001	C1 00 41 000 555		0.71	NT 111
SODIC.000G001201	Unruo:41,390,777	57.8	0.12 - 0.12	INOILE AVAILADIE
Q_1::_ 00000001900	$O_{1} = O_{2} (1 + 0) O_{2} = 0$		0.12	Ormentie starse aut
2001C.000G001300	Unruo:41,390,777	65.7	0.18 -	Osmotic stress potassium
			0.20	transporter

Supplementary Table 3: Identified genetic markers for Median Φ_{1-4} are within 100kb of multiple gene models.



Figure 6: **GWAS identifies genomic regions associated with variation in the median of the lower four phyllotaxic angles. A)** Distribution of the median of the Φ_{1-4} values for each plant. The broad sense heritability of this trait was estimated to be 0.25. **B)** Results of a resampling FarmCPU GWAS conducted for median of the Φ_{1-4} value. Dashed line indicates an RMIP value of 0.10, the cutoff employed in this study. **C)** Median Φ_{1-4} values for each plant by allele (major or minor) at Chr05:12,109,370 (RMIP= 0.26). The *n* below each box indicates the number of genotypes homozygous for the allele. Genotypes with heterozygous calls at the marker were excluded. **D)** Median Φ_{1-4} values for each plant by allele (major or minor) at Chr05:65,733,791 (RMIP= 0.19). **E)** Median Φ_{1-4} values for each plant by allele (major or minor) at Chr06:41,390,777 (RMIP= 0.11). **F)** Genomic interval surrounding the trait associated marker Chr05:12,109,370 (black dot). The total region shown is 200 kilobases, 100 kilobases on either side of the trait associated marker. Colored boxes above the black line indicate the position of annotated genes. Color bar below the black line indicates linkage disequilibrium between the trait associated marker and other genetic markers within the 200 kilobase interval. **G)** Genomic interval surrounding the trait associated marker Chr05:41,390,777.



Supplementary Figure 1: Correlation between phyllotaxic angles from reconstructions of the same plant decreases as time between imaging dates increases. A) Correlation of lower five φ values measured by 3D reconstructions of the sorghum plants when imaged on April 13, 2018 (Timepoint 2) and April 16, 2018 (Timepoint 3) after removing φ values less than 90° or greater than 270°, with an R^2 value of 0.3304 (n = 820 angles). In cases when the measurements for a single plant were negatively correlated between the two days, the values from the Timepoint 3 reconstruction were transformed to their conjugate angles. B) Correlation of lower five φ values measured by 3D reconstructions of the sorghum plants when imaged on April 11, 2018 (Timepoint 1) and April 16, 2018 (Timepoint 3) after removing φ values less than 90° or greater than 270°, with an R^2 value of 0.2351 (n = 820 angles). In cases when the measurements for a single plant were negatively correlated between the two days, the values from the Timepoint 3 reconstruction were the two days, the values from the Timepoint 3 reconstruction were transformed to their conjugate angles.



Supplementary Figure 2: Tillers, lodging, or early leaf senescence in sorghum plants can cause extreme phyllotaxic values in reconstruction measurements. A) A sorghum plant with large tillers. This can cause extreme phyllotaxy values when measured via 3D reconstruction. B) A lodged sorghum plant. Lodged plants may also present as having extreme phyllotaxy values. C) A plant where the third true leaf has senesced before the first and second true leaves, resulting in an extreme phyllotaxic angle being measured as φ_2 between the second true leaf and the fourth true leaf.



Supplementary Figure 3: Resampling FarmCPU GWAS detects stable marker-trait associations for multiple quantitative summaries of lower-canopy phyllotaxy. A – L) Manhattan plot of marker-trait associations for each quantitative summary of lower canopy phyllotaxy with a broad-sense heritability ≥ 0.20 .