## TCP congestion control

#### Recall:

where

```
\label{eq:maxWindow} \begin{aligned} & \max \{ \text{ AdvertisedWindow}, \text{ CongestionWindow} \} \end{aligned}
```

Key question: how to set CongestionWindow which, in turn, affects ARQ's sending rate?

- → linear increase/exponential decrease
- $\longrightarrow$  AIMD

TCP congestion control components:

- (i) Congestion avoidance
  - → linear increase/exponential decrease
  - → additive increase/exponential decrease (AIMD)

As in Method B, increase CongestionWindow linearly, but decrease exponentially

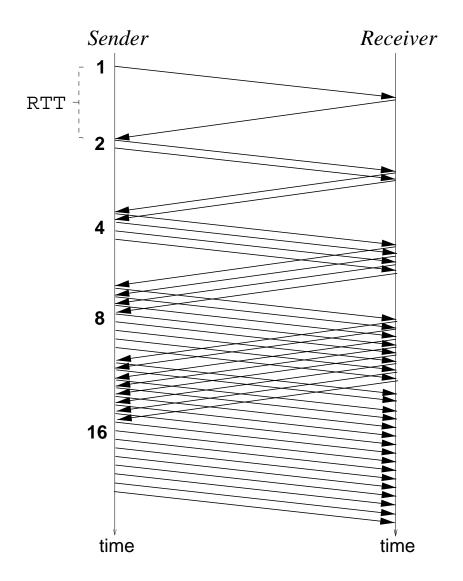
Upon receiving ACK:

 $\begin{tabular}{ll} \textbf{CongestionWindow} &\leftarrow \textbf{CongestionWindow} + 1 \\ \textbf{Upon timeout:} \\ \end{tabular}$ 

 $\texttt{CongestionWindow} \leftarrow \texttt{CongestionWindow} \, / \, 2$ 

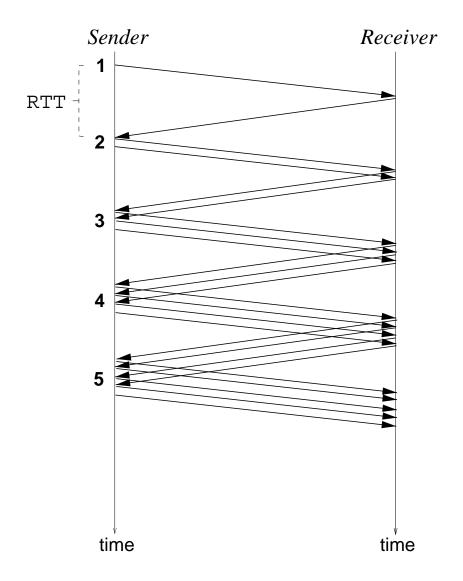
But is it correct...

"Linear increase" time diagram:



---- results in exponential increase

# What we want:



 $\longrightarrow$  increase by 1 every window

Thus, linear increase update:

Upon timeout and exponential backoff,

 ${\tt SlowStartThreshold} \leftarrow {\tt CongestionWindow} \, / \, 2$ 

(ii) Slow Start

Reset CongestionWindow to 1

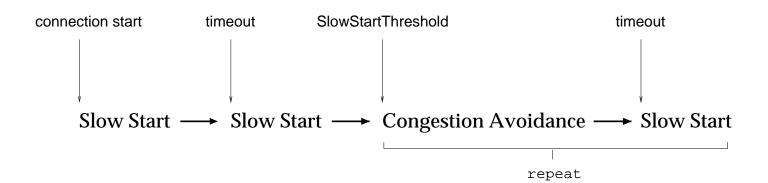
Perform exponential increase

 $\texttt{CongestionWindow} \leftarrow \texttt{CongestionWindow} + 1$ 

- Until timeout at start of connection
  - → rapidly probe for available bandwidth
- Until CongestionWindow hits SlowStartThreshold following Congestion Avoidance
  - $\rightarrow$  rapidly climb to safe level
  - → "slow" is a misnomer
  - → exponential increase is super-fast

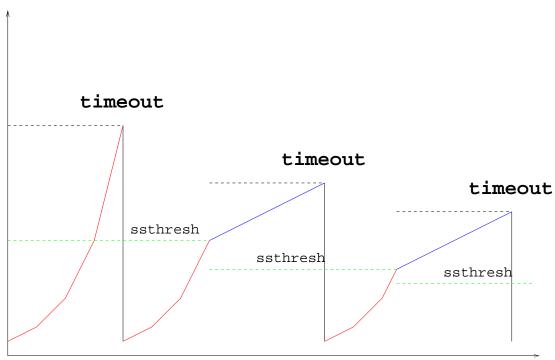
## Basic dynamics:

- $\longrightarrow$  after connection set-up
- → before connection tear-down



# CongestionWindow evolution:

### CongestionWindow



Events (ACK or timeout)

(iii) Exponential timer backoff

 $TimeOut \leftarrow 2 \cdot TimeOut$  if retransmit

(iv) Fast Retransmit

Upon receiving three duplicate ACKs:

- Transmit next expected segment
  - $\rightarrow$  segment indicated by ACK value
- Perform exponential backoff and commence Slow Start
  - → three duplicate ACKs: likely segment is lost
  - → react before timeout occurs

TCP Tahoe: features (i)-(iv)

## (v) Fast Recovery

### Upon Fast Retransmit:

- Skip Slow Start and commence Congestion Avoidance
  - $\rightarrow$ dup ACKs: likely spurious loss
- Insert "inflationary" phase just before Congestion Avoidance

TCP Reno: features (i)-(v)

→ pre-dominant form

Many more versions of TCP:

- → NewReno w/ SACK, w/o SACK, Vegas, etc.
- $\longrightarrow$  wireless, ECN, multiple time scale
- → mixed verdict; pros/cons

Given sawtooth behavior of TCP's linear increase/exponential backoff:

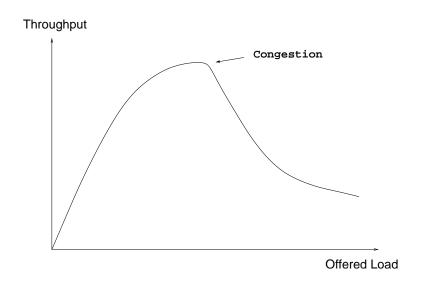
Why use exponential backoff and not Method D?

- For multimedia streaming (e.g., pseudo real-time), AIMD (Method B) is not appropriate
  - $\rightarrow$  use Method D
- For unimodal case—throughput decreases when system load is excessive—story is more complicated
  - $\rightarrow$  asymmetry in control law needed for stability

### Congestion Control and Selfishness

- $\longrightarrow$  to be or not to be selfish ...
- → noncooperative game theory
- → John von Neumann, John Nash, . . .

Ex.: "tragedy of commons," Garrett Hardin, '68



- if everyone acts selfishly, no one wins
  - $\rightarrow$  in fact, everyone loses
- can this be prevented?

Ex.: Prisoner's Dilemma game

- $\longrightarrow$  formalized by Tucker in 1950
- $\longrightarrow$  "cold war" begins
- both cooperate (i.e., stay mum): 1 year each
- both selfish (i.e., rat on the other): 5 years each
- one cooperative/one selfish: 9 vs. 0 years

When cast as congestion control game:

|       |   | Bob  |      |
|-------|---|------|------|
|       |   | C    | N    |
| Alice | C | 5, 5 | 1, 9 |
|       | N | 9, 1 | 3, 3 |

- $\longrightarrow$  (a, b): throughput (Mbps) achieved by Alice/Bob
- → what do "rational" players do?

Rational: in the sense of seeking selfish gain

- → both choose strategy "N"
- → called Nash equilibrium
- → why: strategy "N" dominates strategy "C"

Dominance: suppose Alice chooses "C"; from Bob's perspective, choosing "N" yields 9 Mbps whereas "C" yields only 5 Mbps. Similarly if Alice were to choose "N."

- → for Bob: "N" dominates "C"
- → a "no brainer" for Bob
- → by symmetry, the same logic applies to Alice

Ex.: von Neumann argued for first-strike policy based on this reasoning.

- → luckily "MAD" prevailed
- → MAD: mutually assured destruction
- → sometimes "delay" is good!

In a selfish environment, the system tends to converge to a Nash equilibrium.

A Nash equilibrium is a system state where no player has an incentive to make a **unilateral** move.

- → unilateral: only one player makes a move
- $\longrightarrow$  e.g.: (N,C) is not a Nash equilibrium
- → Bob gains by switching from "C" to "N"
- $\longrightarrow$  Bob's payoff increases from 1 to 3

A Nash equilibrium is a **stable** state of a noncooperative system.

- → stability does not imply goodness
- $\longrightarrow$  (C,C) is better than (N,N) for both Alice & Bob
- $\longrightarrow$  how to attain (C,C)?

Assumption: players cooperate

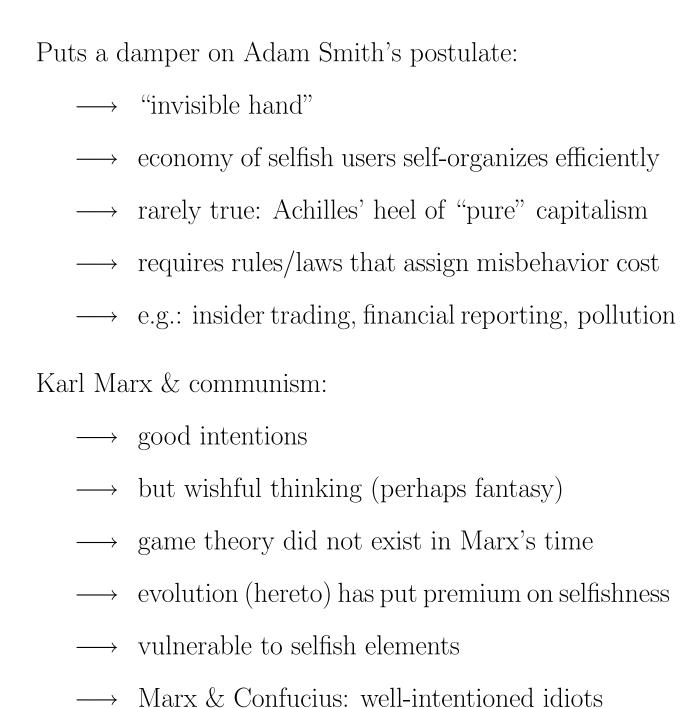
 $\longrightarrow$  this is an assumption!

Outcome of game with cooperative players:

- $\longrightarrow$  configuration (C,C) with payoff (5,5)
- $\longrightarrow$  system optimal: 5 + 5 = 10 (sum of payoffs)
- $\longrightarrow$  note: (1,9) and (9,1) are also system optimal
- → also Pareto optimal

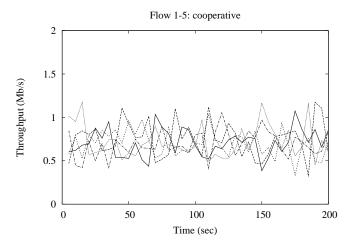
A system state is Pareto optimal if total system payoff cannot be improved without sacrificing one (or more) player's payoff.

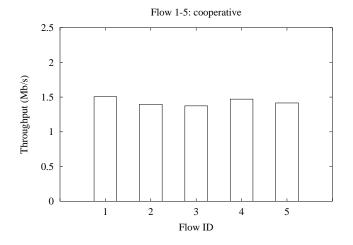
- → improvement requires "sacrificial lamb"
- → welfare notion of overall goodness
- $\longrightarrow$  (5,5), (1,9), (9,1): Pareto optimal
- $\longrightarrow$  (3,3): not Pareto optimal



5 regular (cooperative) TCP flows:

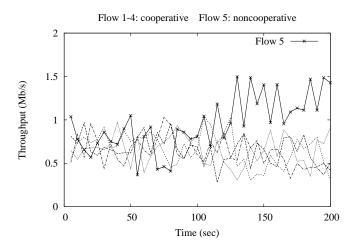
→ share 11 Mbps WLAN bottleneck link

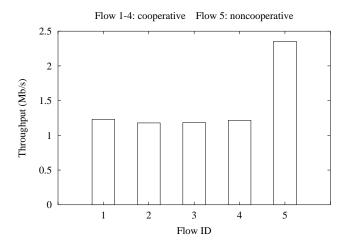




4 regular (cooperative) TCP flows and 1 noncooperative TCP flow:

→ same benchmark set-up





#### Remarks:

- a Nash equilibrium need not exist
  - $\rightarrow$  system subject to oscillation
  - → circular "chain reaction"
- Nash's main result (game theory): finite noncooperative games with **mixed** strategies—choose action probabilistically—always possess equilibrium
  - $\rightarrow$  vs. **pure** strategy (more in tune with reality)
  - $\rightarrow$  pure strategy games: hard problem
- congestion pricing
  - $\rightarrow$  penalize those who congest: e.g., usage pricing
  - $\rightarrow$  in the States: flat pricing (dominant)
  - $\rightarrow$  not skimpy like the rest of the world!

- repeated/evolutionary games
  - $\rightarrow$  e.g.: iterated Prisoner's Dilemma
  - → rob bank/get caught, again and again . . .
  - $\rightarrow$  what should the prisoners do then?
  - $\rightarrow$  "grim trigger" policy: don't forgive
  - $\rightarrow$  e.g.: cheating husband/wife leading to divorce
  - → "tit-for-tat" policy: conditionally forgive
  - → e.g.: if you cheat, I cheat; if you don't cheat, I don't cheat
  - $\rightarrow$  somewhat "flexible" morals
  - $\rightarrow$  both are optimal (in a certain sense)
  - $\rightarrow$  most relevant for greedy TCP