## Routing

Problem: Given more than one path from source to destination, which one to take?


## Features:

- Architecture
- Algorithms
- Implementation
- Performance


## Architecture

Hierarchical routing:
$\longrightarrow$ Internet: intra-domain vs. inter-domain routing $\longrightarrow$ separate decision making


## Ex.: Purdue to east coast (BU)

```
[109] infobahn:Routing % traceroute csa.bu.edu
traceroute to csa.bu.edu (128.197.12.3), 30 hops max, 40 byte packets
    1 cisco5 (128.10.27.250) 3.707 ms 0.616 ms 0.590 ms
    2 172.19.60.1 (172.19.60.1) 0.406 ms 0.431 ms 0.520 ms
3 tel-210-m10-01-campus.tcom.purdue.edu (192.5.40.54) 0.491 ms 0.600 ms 0.510 ms
4 gigapop.tcom.purdue.edu (192.5.40.134) 9.658 ms 1.966 ms 1.725 ms
5 192.12.206.249 (192.12.206.249) 1.715 ms 3.381 ms 1.749 ms
6 chinng-iplsng.abilene.ucaid.edu (198.32.8.76) 5.669 ms 8.319 ms 5.601 ms
7 nycmng-chinng.abilene.ucaid.edu (198.32.8.83) 25.626 ms 25.664 ms 25.621 ms
8 noxgs1-PO-6-0-NoX-NOX.nox.org (192.5.89.9) 30.634 ms 30.768 ms 30.722 ms
9 192.5.89.202 (192.5.89.202) 31.128 ms 31.045 ms 31.082 ms
10 cumm111-cgw-extgw.bu.edu (128.197.254.121) 31.287 ms 31.152 ms 31.146 ms
11 cumm111-dgw-cumm111.bu.edu (128.197.254.162) 31.224 ms 31.192 ms 31.308 ms
12 csa.bu.edu (128.197.12.3) 31.529 ms 31.243 ms 31.367 ms
```


## Ex.: Purdue to west coast (Cisco)

[112] infobahn:Routing \% traceroute www.cisco.com traceroute to www.cisco.com (198.133.219.25), 30 hops max, 40 byte packets
1 cisco5 (128.10.27.250) $0.865 \mathrm{~ms} \quad 0.598 \mathrm{~ms} 1.282 \mathrm{~ms}$
$2 \quad 172.19 .60 .1(172.19 .60 .1) \quad 0.518 \mathrm{~ms} \quad 0.379 \mathrm{~ms} \quad 0.405 \mathrm{~ms}$
3 tel-210-m10-01-campus.tcom.purdue.edu (192.5.40.54) $0.687 \mathrm{~ms} \quad 0.551 \mathrm{~ms} \quad 0.551 \mathrm{~ms}$
4 switch-data.tcom.purdue.edu (192.5.40.34) $3.496 \mathrm{~ms} \quad 3.523 \mathrm{~ms} 2.750 \mathrm{~ms}$
5 so-2-3-0-0.gar2.Chicago1.Level3.net ( 67.72 .124 .9 ) 8.114 ms 20.181 ms 8.512 ms
6 so-3-3-0.bbr1.Chicago1.Level3.net (4.68.96.41) 11.543 ms 9.079 ms 8.239 ms
7 ae-0-0.bbr1.SanJose1.Level3.net (64.159.1.129) 62.319 ms as-1-0.bbr2.SanJose1.Level3.net
8 ge-11-0.ipcolo1.SanJose1.Level3.net (4.68.123.41) 68.180 ms ge-7-1.ipcolo1.SanJose1.Level
9 p1-0.cisco.bbnplanet.net (4.0.26.14) 75.006 ms 72.557 ms 70.377 ms
10 sjce-dmzbb-gw1.cisco.com (128.107.239.53) $66.075 \mathrm{~ms} \quad 69.223 \mathrm{~ms} \quad 68.350 \mathrm{~ms}$
11 sjck-dmzdc-gw1.cisco.com (128.107.224.69) $65.650 \mathrm{~ms} \quad 74.358 \mathrm{~ms} \quad 69.952 \mathrm{~ms}$ $12{ }^{\text { } C}$

Three levels: LAN, intra-domain, and inter-domain

Tel-210 to HAWK



Inter-domain topology:

$\longrightarrow$ domain called autonomous system (AS)
$\longrightarrow 16$ bit identifier

Inter-domain connectivity of Purdue:

- Level3 (AS 3356) $\rightarrow$ INDIANAGIGAPOP (AS 19782)
$\rightarrow$ Purdue (AS 17)
- Internet2/Abilene (AS 11537) $\rightarrow$ INDIANAGIGAPOP (AS 19782) $\rightarrow$ Purdue (AS 17)

The Indy GigaPoP has its own AS number (19782). $\longrightarrow$ part of I-Light (Indiana state-wide project) $\longrightarrow$ located at IUPUI, connects Purdue \& IU

Level3 backbone network: www.level3.com

LEVEL 3 P BACKBCONE

$\longrightarrow 10$ Gbps backbone (same as Purdue)
$\longrightarrow$ part of backbone: OC-48 (2.488 Gbps)

## Abilene/Internet2 backbone: www.internet2.edu



Abilene International Network Peers


Granularity of routing network:

- Router
- Domain: autonomous system
$\rightarrow 16$ bit identifier ASN
$\rightarrow$ assigned by IANA along with IP prefix block (CIDR)

Network topology (i.e., map/connectivity):

- Router graph
$\rightarrow$ node: router
$\rightarrow$ edge: physical link between two routers
- AS graph
$\rightarrow$ node: AS
$\rightarrow$ edge: physical link between 2 or more border routers
$\rightarrow$ sometimes at exchange point or network

Router type:

- access router
- border router
- backbone router

AS type:

- stub AS
$\rightarrow$ no forwarding
$\rightarrow$ may be multi-homed (more than one provider)
- transit AS
$\rightarrow$ tier-1: global reachability \& no provider above
$\rightarrow$ tier-2 or tier-3: providers above

AS graph:

## Stub AS



## Transit AS

Inter-AS relationship: bilateral

- customer-provider: customer subscribes BW from provider
$\rightarrow$ most common
$\rightarrow$ customer can reach provider's reachable IP space
- peering:
$\rightarrow$ only the peer's IP address and below
$\rightarrow$ the peer's provider's address space: invisible

Common peering:

- among tier-1 providers
$\rightarrow$ ensures global reachability
$\rightarrow$ socio-economic self-organization
$\rightarrow$ less regulated than telephony
- among tier-2 providers
$\rightarrow$ regional providers
$\rightarrow$ economic factors
- among stubs
$\rightarrow$ economic factors
$\rightarrow$ e.g., content provider \& access ("eyeball") provider
$\rightarrow$ e.g., Time Warner \& AOL

Route or path: criteria of goodness

- Hop count
- Delay
- Bandwidth
- Loss rate

Composition of goodness metric:
$\longrightarrow$ quality of end-to-end path

- Additive: hop count, delay
- Min: bandwidth
- Multiplicative: loss rate


## Goodness of routing:

$\longrightarrow$ assume $N$ users or sessions
$\longrightarrow \quad$ suppose path metric is delay

- System optimal routing
$\rightarrow$ choose paths to minimize $\frac{1}{N} \sum_{i=1}^{N} D_{i}$
- User optimal routing
$\rightarrow$ each user $i$ chooses path to minimize $D_{i}$
$\rightarrow$ selfish actions

Pros/cons:

- System optimal routing:
- Good: minimizes delay for the system as a whole
- Bad: complex and difficult to scale up
- User optimal routing:
- Good: simple
- Bad: may not make efficient use of resources
$\rightarrow$ utilization

Some pitfalls of user optimal routing:
$\longrightarrow$ stemming from selfishness

- Fluttering or ping pong effect
- Braess paradox


## Algorithms

Find short, in particular, shortest paths from source to destination.

Key observation on shortest paths:

- Assume $p$ is a shortest path from $S$ to $D$
$\rightarrow S \xrightarrow{p} D$
- Pick any intermediate node $X$ on the path
- Consider the two segments $p_{1}$ and $p_{2}$
$\rightarrow S \xrightarrow{p_{1}} X \xrightarrow{p_{2}} D$
- The path $p_{1}$ from $S$ to $X$ is a shortest path, and so is the path $p_{2}$ from $X$ to $D$


## Illustration:


shortest path shortest path
$\longrightarrow$ reverse implication need not hold

Procedure: Grow a routing tree $\mathcal{T}$ rooted at source $S$
$\longrightarrow$ initially $\mathcal{T}$ only contains $S$

1. Find a node $X$ with shortest path from $S$
$\rightarrow$ there may be more than one such node
$\rightarrow$ add $X$ (and path $S \stackrel{p}{\rightsquigarrow} X$ ) to routing tree $\mathcal{T}$
2. Find node $Y \notin \mathcal{T}$ with shortest path from $S$
$\rightarrow$ update existing paths if going through $Y$ is shorter
$\rightarrow$ i.e., $\min \{d(S, Z), d(S, Y)+\ell(Y, Z)\}$
$\rightarrow$ need only check for $Z \notin \mathcal{T}$
3. Repeat step two until no more nodes left to add

Observations:
$\longrightarrow$ once node is added, it's final (no backtracking)
$\longrightarrow$ builds minimum spanning tree routed at $S$
$\longrightarrow$ Dijkstra's algorithm

## Remarks:

- Running time: $O\left(n^{2}\right)$ time complexity
$\rightarrow n$ : number of nodes
- If heap is used: $O(|E| \log |V|)$
$\rightarrow$ good for sparse graphs: $|E| \ll n^{2}$
$\rightarrow$ e.g., if linear: $O(n \log n)$
- Can also be run "backwards"
$\rightarrow$ start from destination $D$ and go to all sources
$\rightarrow$ a variant used in inter-domain routing
$\rightarrow$ forward version: used in intra-domain routing
- Source $S$ requires global link distance knowledge
$\rightarrow$ centralized algorithm (center: source $S$ )
$\rightarrow$ every router runs Dijkstra with itself as source
- Internet protocol implementation
$\rightarrow$ OSPF (Open Shortest Path First)
$\rightarrow$ link state algorithm
$\rightarrow$ broadcast protocol
- Minimum spanning tree routed at $S$ :
$\rightarrow$ multicasting: multicast tree
$\rightarrow$ standardized but not implemented on Internet


# Distributed/decentralized shortest path algorithm: 

$\longrightarrow$ Bellman-Ford algorithm
$\longrightarrow$ based on shortest path decomposition property

Key procedure:

- Each node $X$ maintains current shortest distance to all other nodes
$\rightarrow$ a distance vector
- Each node advertises to neighbors its current best distance estimates
$\rightarrow$ i.e., neighbors exchange distance vectors
- Node $X$, upon receiving an update from neighbor $Y$, performs update: for all $Z$

$$
d(X, Z) \leftarrow \min \{d(X, Z), d(Y, Z)+\ell(X, Y)\}
$$

... same criterion as Dijkstra's algorithm

Remarks:

- Running time: $O\left(n^{3}\right)$
- Each source or router only talks to neighbors
$\rightarrow$ local interaction
$\rightarrow$ no need to send update if no change
$\rightarrow$ if change, entire distance vector must be sent
- Knows shortest distance, but not path
$\rightarrow$ just the next hop is known
- Elegant but additional issues compared to Dijkstra's algorithm
$\rightarrow$ e.g., stability
- Internet protocol implementation
$\rightarrow$ RIP (Routing Information Protocol)


## QoS routing:

Given two or more performance metrics e.g., delay and bandwidth - find path with delay less than target delay $D$ (e.g., 100 ms ) and bandwidth greater than target bandwidth $B$ (e.g., 1.5 Mbps)
$\longrightarrow$ from shortest path to best QoS path
$\longrightarrow$ multi-dimensional QoS metric
$\longrightarrow$ other: jitter, hop count, etc.

How to find best QoS path that satisfies all requirements?
Brute-force

- Enumerate all possible paths
- Rank them

How many paths are there:

- If there are $n$ nodes, there can be up to

$$
\frac{n(n-1)}{2}
$$

undirected links

- Hence, from source $S$ there can be up to

$$
(n-1)(n-2) \cdots 321=(n-1)!
$$

paths

- By Stirling's formula

$$
n!\approx \sqrt{2 \pi n}\left(\frac{n}{e}\right)^{n}
$$

$\rightarrow$ superexponential
$\rightarrow$ too many for brute-force

Is there a more clever or better algorithm?
$\longrightarrow$ as of Apr. 12, 2006: unknown
$\longrightarrow$ specifically: QoS routing is NP-complete
$\longrightarrow$ strong evidence there may not exist good algorithm

In networking: several problems turn out to be NP-complete
$\longrightarrow$ e.g., scheduling, control, ...
$\longrightarrow$ "P $=$ NP" problem
$\longrightarrow$ one of the hardest problems in science ever

Doesn't matter too much for QoS routing
$\longrightarrow$ little demand for very good algorithm
$\longrightarrow$ roughly ok is fine
$\longrightarrow$ intra-domain: short paths
$\longrightarrow$ inter-domain: other factors ("policy")

Policy routing:
$\longrightarrow$ policy is not precisely defined
$\longrightarrow$ almost anything goes
Routing criteria include

- Performance
$\rightarrow$ e.g., short paths
- Trust
$\rightarrow$ what in the world is "trust"?
- Economics
$\rightarrow$ pricing
$\rightarrow$ flexibility through multiple providers
- Politics, social issues, etc.
$\longrightarrow$ no good understanding of "policy" to date
$\longrightarrow$ anecdotal

